

Angle-resolved photoemission spectroscopy (ARPES) for 2D layered structure: graphene and topological insulators

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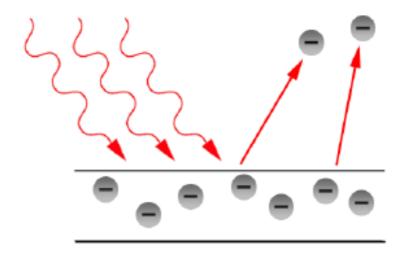
National Synchrotron Radiation Research Center

Outline

- Introduction to angle-resolved photoemission spectroscopy (ARPES)
 - The principle of ARPES
 - Synchrotron light source
 - Current status of ARPES beamline at NSRRC
 - Scientific cases
- The electronic structure of 2D layered structure
 - Surface states and quantum well states
 - Graphene (BLG)
 - Topological insulators (Tis)
- Summary



What is photoemission?



Photon in -> electron out (emission)



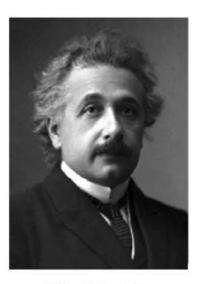
X-ray¹ Photoelectron spectroscopy, based on the photoelectric effect,^{2,3} was developed in the mid-1960's as a practical technique by Kai Siegbahn and his research group at the University of Uppsala, Sweden.⁴



Wilhelm Conrad Röntgen



Heinrich Rudolf Hertz



Albert Einstein





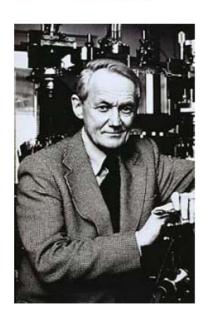
Kai M. Siegbahn



- 1. W. Röntgen, 1901 Nobel Prize in Physics "in recognition of the extraordinary services he has rendered by the discovery of the remarkable rays subsequently named after him."
- 2. H. Hertz, Ann. Physik 31,983 (1887).
- A. Einstein, Ann. Physik 17,132 (1905). 1921 Nobel Prize in Physics "for his services to Theoretical Physics, and especially for his discovery of the law of the photoelectric effect."
- 4. K. Siegbahn, Et. Al., Nova Acta Regiae Soc. Sci., Ser. IV, Vol. 20 (1967). 1981 Nobel Prize in Physics "for his contribution to the development of high resolution electron spectroscopy."

Kai Seigbahn: Development of X-ray Photoelectron Spectroscopy

C. Nordling E. Sokolowski and K. Siegbahn, Phys. Rev. 1957, 105, 1676.



Precision Method for Obtaining Absolute Values of Atomic Binding Energies

CARL NORDLING, EVELYN SOKOLOWSKI, AND KAI SIEGBAHN

Department of Physics, University of Uppsala, Uppsala, Sweden

(Received January 10, 1957)

WE have recently developed a precision method of investigating atomic binding energies, which we believe will find application in a variety of problems in atomic and solid state physics. In principle, the method

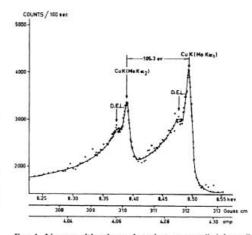


Fig. 1. Lines resulting from photoelectrons expelled from Cu by Mo $K\alpha_1$ and Mo $K\alpha_2$ x-radiation. The satellites marked D.E.L. are interpreted as due to electrons which have suffered a discrete energy loss when scattered in the source.

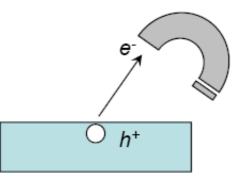
Nobel Prize in Physics 1981 (His father, Manne Siegbahn, won the Nobel Prize in Physics in 1924 for the development of X-ray spectroscopy)

What is photoemission spectroscopy? (photoelectron spectroscopy) (PES)

hv Monochromatized photons

sample

Electron energy analyzer



Initial state: ground (neutral) state

Final state: hole (excited) state

 $N(E_{\nu}$

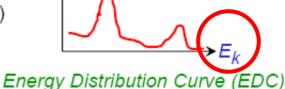
Conservation of energy

 $E_k = hv + E_i - E_f$ (most general expression)

 $\boldsymbol{E}_{\boldsymbol{k}}$: photoelectron kinetic energy

 $\boldsymbol{E_i}(N)$: total initial state system energy

 $E_f(N-1)$: total final state system energy



Energy Distribution Curve (EDC) (Spectrum)



What are the samples and probed states?

Atoms atomic orbitals (states)

Molecules molecular orbitals

core level states (atomic like)

Nanoprticles valence bands/states

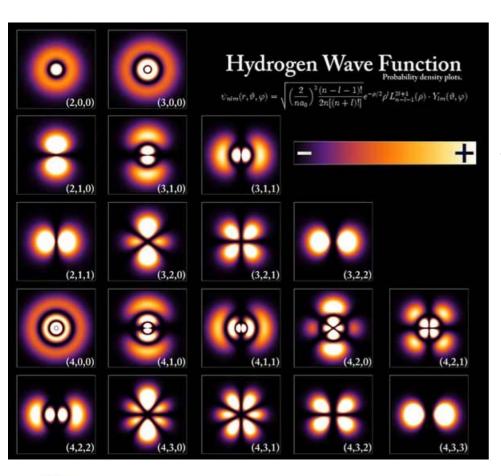
core level states (atomic like)

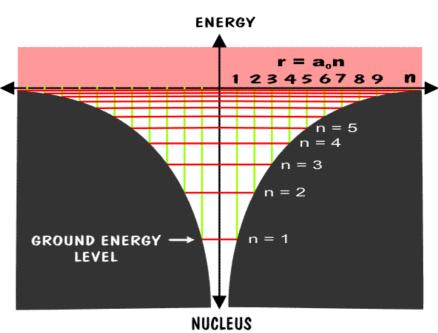
Solids valence bands

core level states (atomic like)



The energy level of hydrogen atom

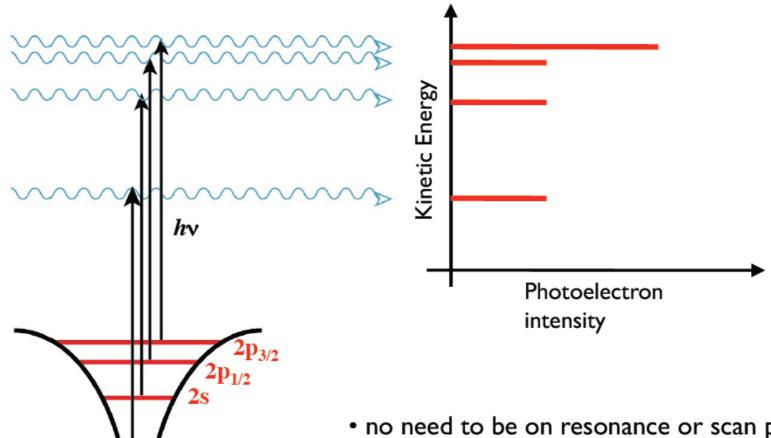






Electron ionization levels are formed from discrete levels in an atom

Energy conservation: $h\nu - E_I = KE$



 no need to be on resonance or scan photon energies (e.g. NMR, optical measurements).
 Just need photons to have high enough energy!

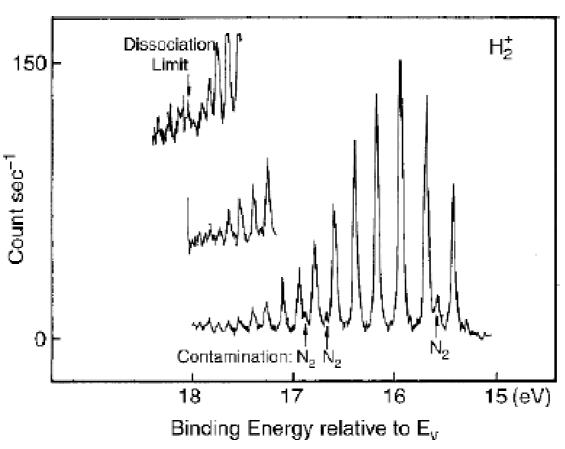


1s

Energy levels of

ionized Ne+

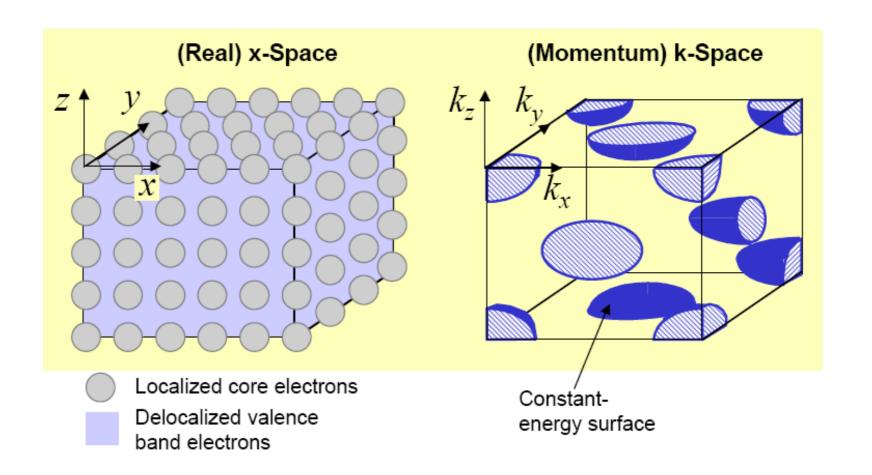
Xeon gas phase test







The crystal structure and momentum space



nickel (II) oxide

primitive vectors **a**₁, **a**₂, **a**₃
reciprocal lattice vector **b**₁,**b**₂,**b**₃

$$\vec{b}_1 = 2\pi \frac{\vec{a}_2 \times \vec{a}_3}{V}$$

$$\vec{b}_2 = 2\pi \frac{\vec{a}_3 \times \vec{a}_1}{V}$$

$$\vec{b}_3 = 2\pi \frac{\vec{a}_1 \times \vec{a}_2}{V}$$

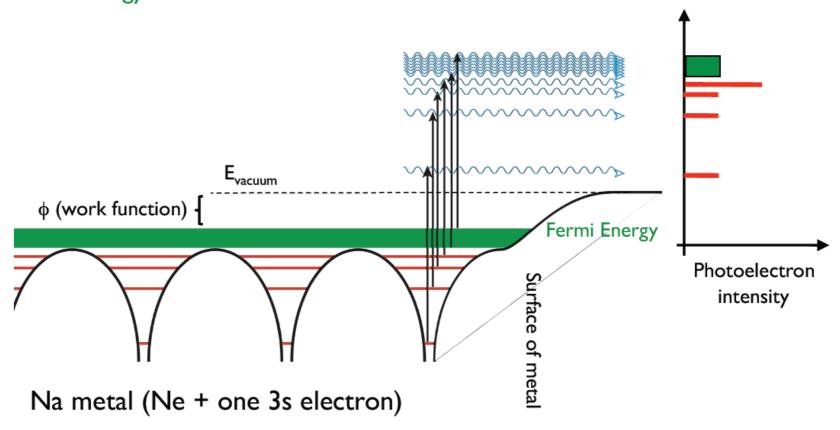
$$V = \vec{a}_1 \cdot \vec{a}_2 \times \vec{a}_3$$

reciprocal lattice G:

$$\vec{G} = l\vec{b}_1 + m\vec{b}_2 + n\vec{b}_3$$

l,m,n are any integers

- Deeply bound "core" electrons remain basically unchanged
- Outermost "valence" electrons hybridize forming continuous "energy bands"





Band theory

Two approximations

Nearly free electrons. Electrons are non-interacting in a periodic crystal potential which is relatively weak and can be treated as a perturbation. As in the free-electron-gas model, they are still subject to the Pauli exclusion principle.

Free electron gas:

The interactions between electrons and between electrons and nuclei are turned off, subject only to the Pauli exclusion principle.

Tightly-bonding approximation

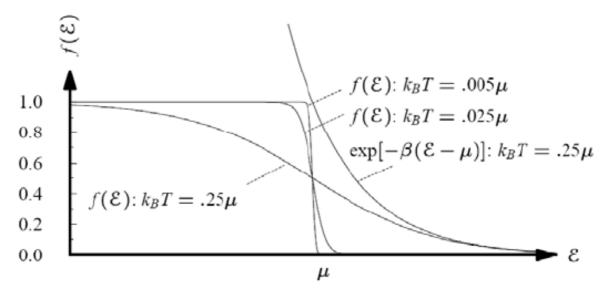
Electrons are tightly bound to particular atoms, overlapping only weakly with neighbors.



Fermi-Dirac Distribution

Thermal Properties of Free Electron Gas: Almost every electronic transport property of solids is proportional to $D(\mathcal{E}_F)$.

Fermi function
$$f(\mathcal{E}) = \frac{1}{e^{(\mathcal{E}-\mu)/k_BT} + 1}$$





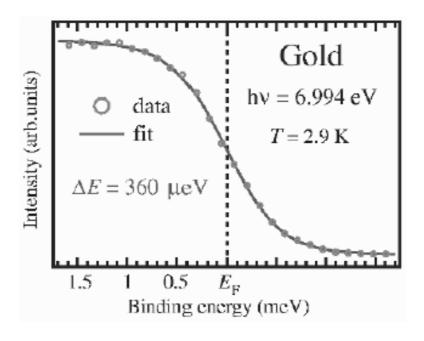
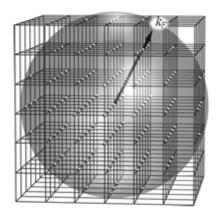


Fig. 2.3. Ultra-high resolution photoemission spectrum on a polycrystalline gold sample (evaporated Au film) for the determination of the energy resolution. The Fermi edge was measured at $T = 2.9 \,\mathrm{K}$ using a frequency tripled (KBe₂BO₃F₂ crystal, KBBF) YVO₃ laser for the photoexcitation ($h\nu = 6.994 \,\mathrm{eV}$) [15]



Density of State



In building up the ground state of very large N electrons, the ground state corresponds to setting the occupation number $f_k = 1$ for $k \le k_F$ and $f_k = 0$ for others; $k_{\rm F}$ is called the Fermi vector.

The volume of the Fermi sphere is $\frac{4\pi k_F^2}{2}$.

Electronic density
$$n = \frac{N}{V} = (\frac{4\pi k_F^3}{3}) D_{\bar{k}} = (\frac{4\pi k_F^3}{3}) \frac{2}{(2\pi)^3} = \frac{k_F^3}{3\pi^2}$$

For an energy \mathcal{E} , total numbers of states:

$$N = \mathcal{V} \frac{k^3}{3\pi^2} = V \frac{(2m\mathcal{E})^{3/2}}{3\pi^2\hbar^3} \qquad \qquad : \quad \mathcal{E} = \frac{\hbar^2 k^2}{2m} \quad k = \frac{\sqrt{2m\mathcal{E}}}{\hbar}$$

$$: \mathcal{E} = \frac{\hbar^2 k^2}{2m} \quad k = \frac{\sqrt{2m\mathcal{E}}}{\hbar}$$

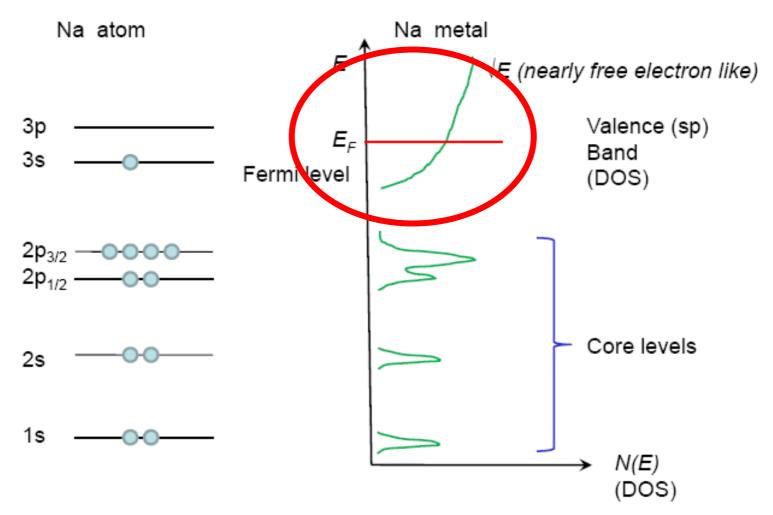
Energy density of states $D(\mathcal{E}) = \frac{1}{V} \frac{dN}{d\mathcal{E}}$

$$D(\mathcal{E}) = \frac{1}{\mathcal{V}} \frac{dN}{d\mathcal{E}} = \frac{\sqrt{2m^3 \mathcal{E}}}{\pi^2 \hbar^3}$$

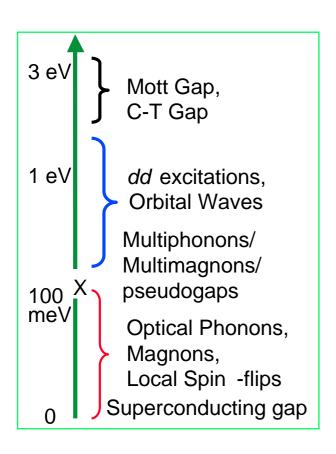
No. of states bounded between $\mathcal{E}(k)$ and $\mathcal{E}(k) + d\mathcal{E}$ per unit volume



Single particle description of energy levels (Density of States) (most convenient in PE)



Energy scale and important excitations



- ➤ Superconducting gap ~ 1 100meV
- ➤Optical Phonons: ~ 40 70 meV
- ➤ Magnons: ~ 10 meV 40 meV
- Pseudogap ~ 30-300 meV
- ➤ Multiphonons and multimagnons ~ 50-

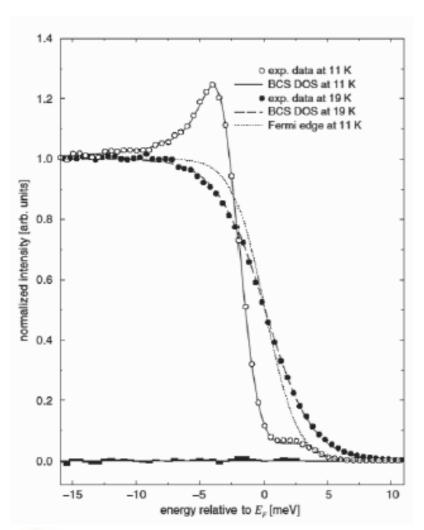
500 meV

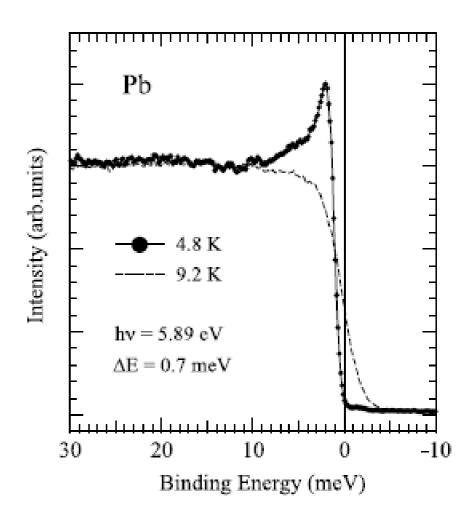
➤ Orbital fluctuations (originated from optically forbidden d-d excitations): ~ 100 meV - 1.5 eV

Requirement: High Energy Resolution with High Intensity



Superconducting gap

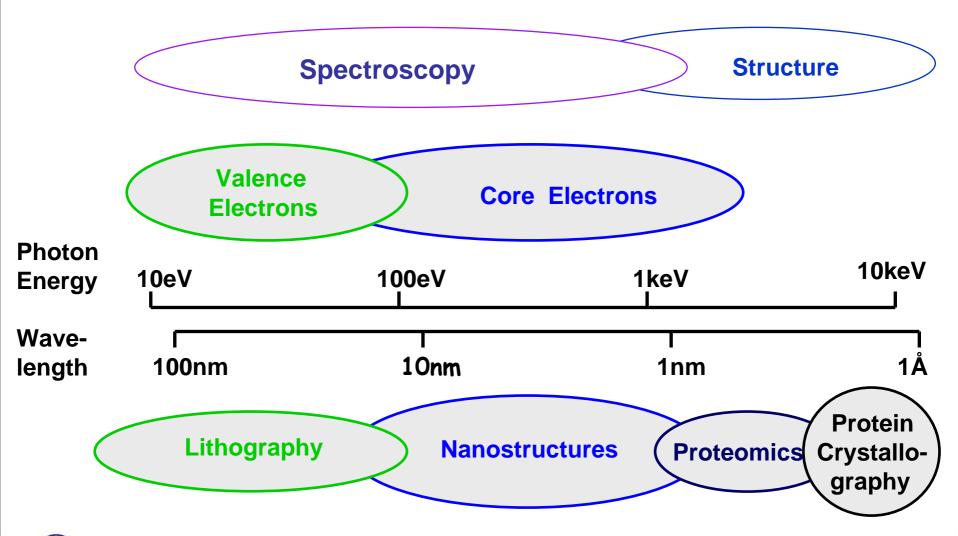






Hufner, very high resolution photoelectron spectroscopy

Science with Light Sources





Adopted from: Franz Himpsel, CMMP '07

Light sources and terminology

Ultraviolet Photoemission Spectroscopy (UPS)

- UV He lamp (21.2 eV, 40.8 eV)
- Laser (high harmonic generation): 6 eV (BBO), 8 eV (KDDP), 11 eV (gas cell)
- Valence band PES, direct electronic state info.
- X-ray Photoemission Spectroscopy (XPS)
 (Electron Spectroscopy for Chemical Analysis) (ESCA)
 - X-ray gun (Al: 1486.6 eV, Mg: 1253.6 eV)
 - core level PE, indirect electronic state info
 - chemical analysis

Synchrotron radiation

- continuous tunable wavelength
- valance band and core level



3rd Synchrotron Radiation light source

Synchrotron Radiation

DORIS 1

e-Synchrotorns and Storage Rings for High Energy Physics

SPEAR

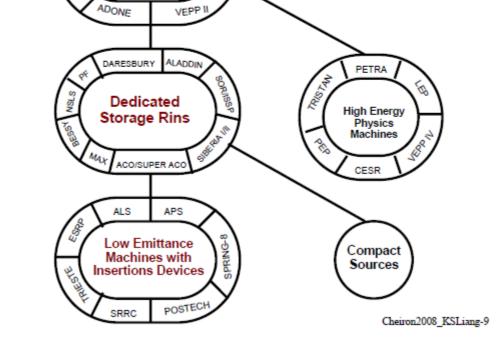
Year 1947: First Synchrotron Radiation observed in weak focusing synchrotron betatrons

1st G:1960-1970

2nd G:1970-1980

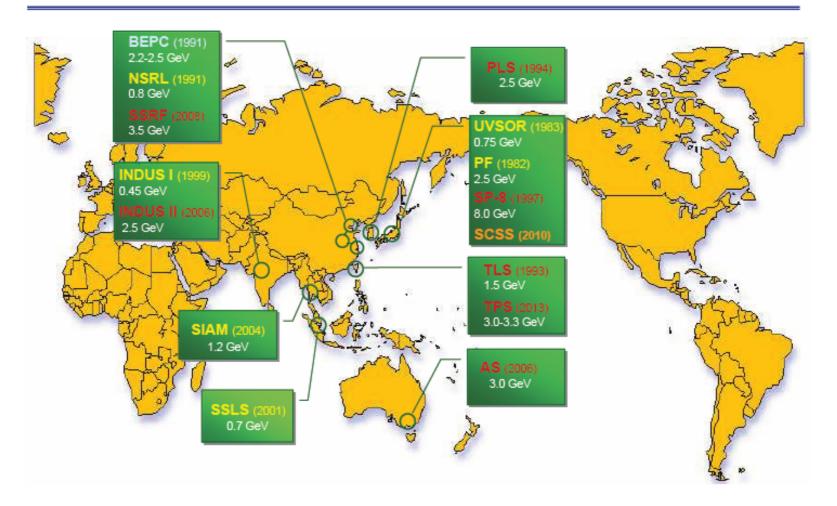
3rd G:1980-

- Straight sections for insertion devices
- Low emittance





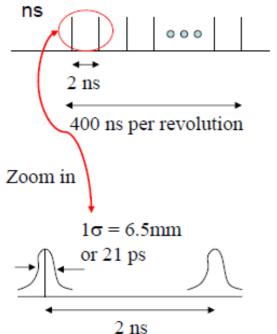
SR Facilities in Asia Oceania Region



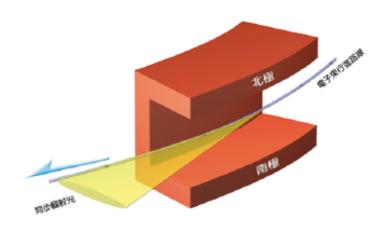


Basic Parameters of Taiwan Light Source

- Interval between bunches: 2ns
- Bunch length (1σ@1.6MV): 6.5 mm
- Bunch duration (1σ): 21 ps
- SC Cavity length: 24 cm
- Flight time through SC cavity: 0.8



 Bunch current (180/200 filling to I_{avg}=300 mA): 1.67 mA/bunch or 4.17*10⁹ electrons/bunch



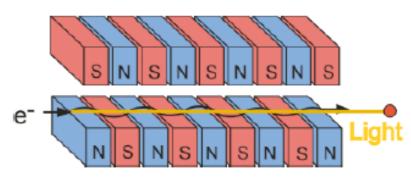
• Critical energy of SR $Ec(keV) = 0.665 E^2 (GeV) B(T)$



Light source properties vs electron beam performance(1)

Main devices to supply SR to users are "undulators", which are installed in magnet-free straight sections in 3rd-generation SR sources.







Current limiting factors(4)

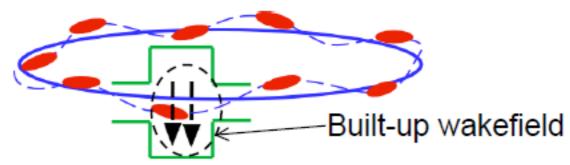
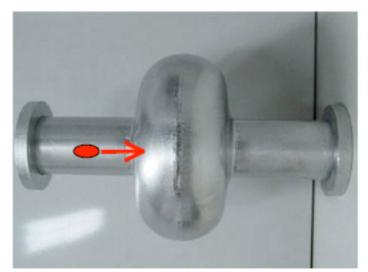
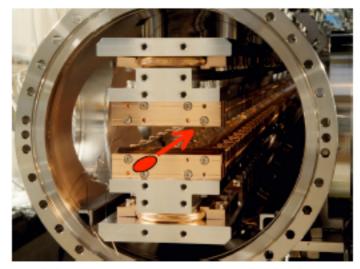


Image of the coupled bunch instability



High Q structure (RF cavity)



Narrow gap undulator

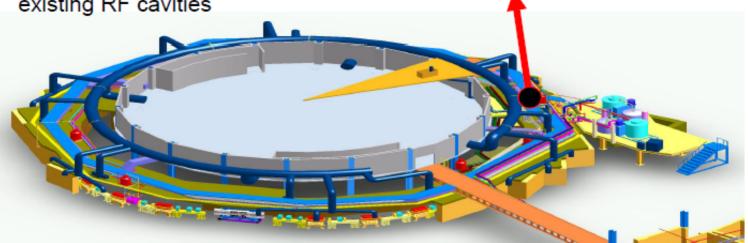


Superconducting RF Cavity

Goals:

 To increase the maximum electron beam current of the storage ring from 240 mA to 500 mA

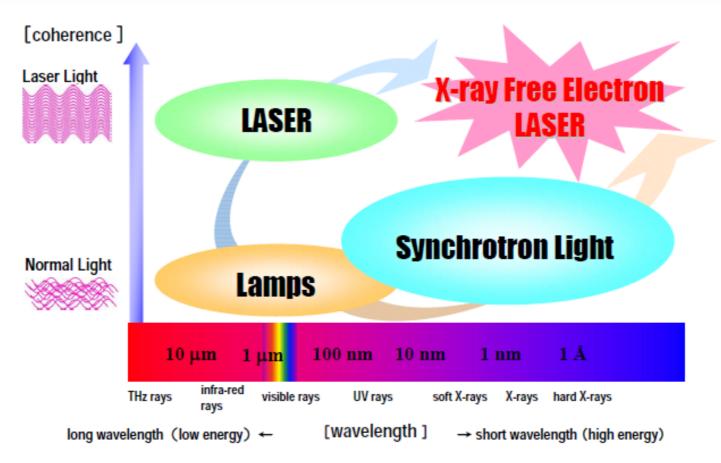
 To eliminate beam instabilities caused by the strong higherorder modes (HOMs) of the existing RF cavities





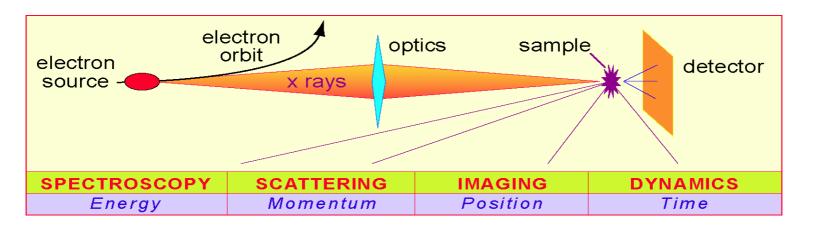
"X-ray Free Electron Laser, XFEL "

coherent light to explore nano-world





Techniques of Synchrotron Radiation (SR)



The fundamental parameters necessary for perception of physical world:

- Energy (spectroscopy, state of matter)
- Momentum (scattering)
- Position (imaging, spatial distribution)
- Time (dynamics)

numerous techniques of SR

Spectroscopy

01 Low-Energy Spectroscopy 02 Soft X-Ray Spectroscopy

03 Hard X-Ray Spectroscopy 04 Optics/Calibration/Metrology

Scattering

05 Hard X-Ray Diffraction 06 Macromolecular Crystallography 07 Hard X-Ray Scattering

08 Soft X-Ray Scattering

Imaging

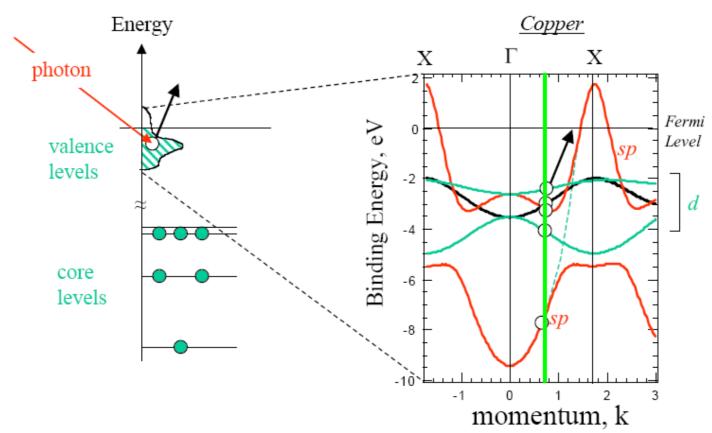
09 Hard X-Ray Imaging 10 Soft X-Ray Imaging

11 Infrared Imaging 12 Lithography



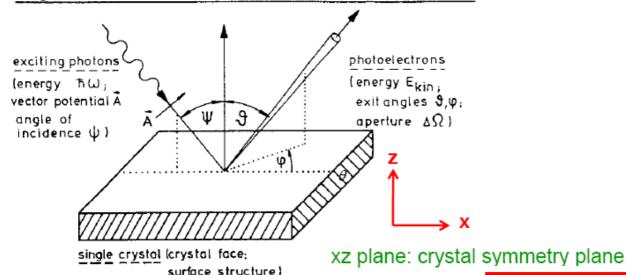


Angle-integrated photoemission (AIPES) and angle-resolved photoemission (ARPES)





Angular Resolved Photoemission Spectroscopy(ARPES)



Electron emission angle: Θ

Photon incident angle: ψ , s- and p-polarization

$$k = \sqrt{\frac{2m}{\hbar^2} E_k} \cdot \sin \theta$$

$$k_{\parallel}(\text{Å}^{-1}) = 0.5123\sqrt{E_k(eV)} \cdot \sin\theta$$

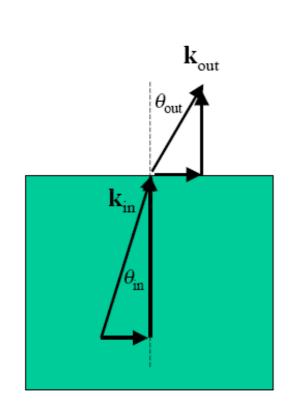
 $k_{||}(inside) = k_{||}(outside)$

Conservation of liner momentum

Important for 3D and 2D band mapping

$$k_{\perp} = 0.5123\sqrt{(E_{kin}\cos^2\theta + V_0)}$$

Conservation of linear momentum parallel to the surface



Kinematic relations

$$k_{out} = \sqrt{\frac{2m}{\hbar^2}} E_{kin}$$

$$k_{in} = \sqrt{\frac{2m}{\hbar^2}} (E_{kin} + V_0)$$

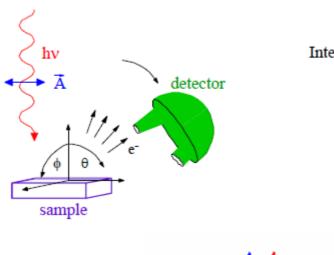
$$k_{out,\parallel} = k_{in,\parallel} \equiv k_{\parallel}$$

"Snell's Law"

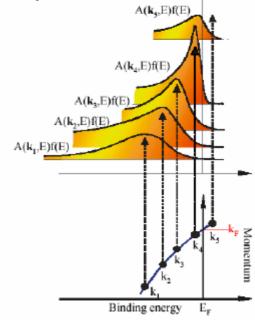
$$k_{\parallel} = \sin \theta_{out} \sqrt{\frac{2m}{\hbar^2} E_{kin}} = \sin \theta_{in} \sqrt{\frac{2m}{\hbar^2} (E_{kin} + V_0)}$$

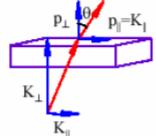
Critical angle for emission

$$\left(\sin\theta_{out}\right)_{\max} = \sqrt{\frac{E_{kin}}{E_{kin} + V_0}}$$



Intensity $\propto \sum_{i,f} \left| \left\langle f \middle| \vec{\mathbf{p}} \bullet \vec{\mathbf{A}} \middle| i \right\rangle \right|^2 A(\vec{\mathbf{k}}, E) f(E)$





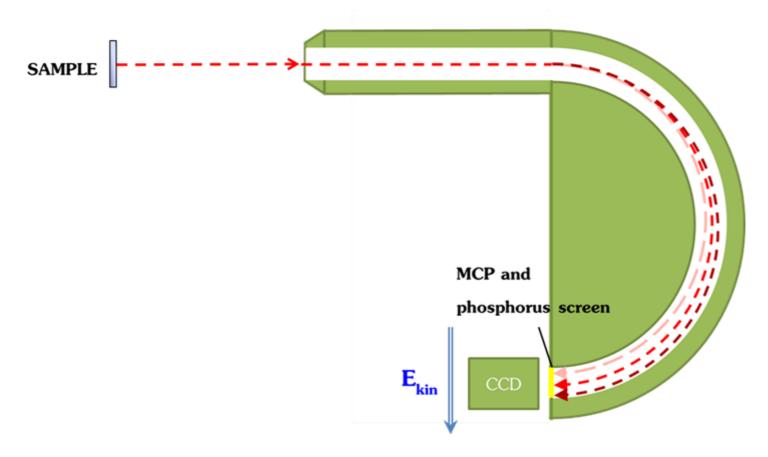
$$k_{\perp} = 0.5123\sqrt{(E_{kin}\cos^2\theta + V_0)}$$

$$k_{//} = 0.5123 \sqrt{E_{kin}} \sin \theta$$

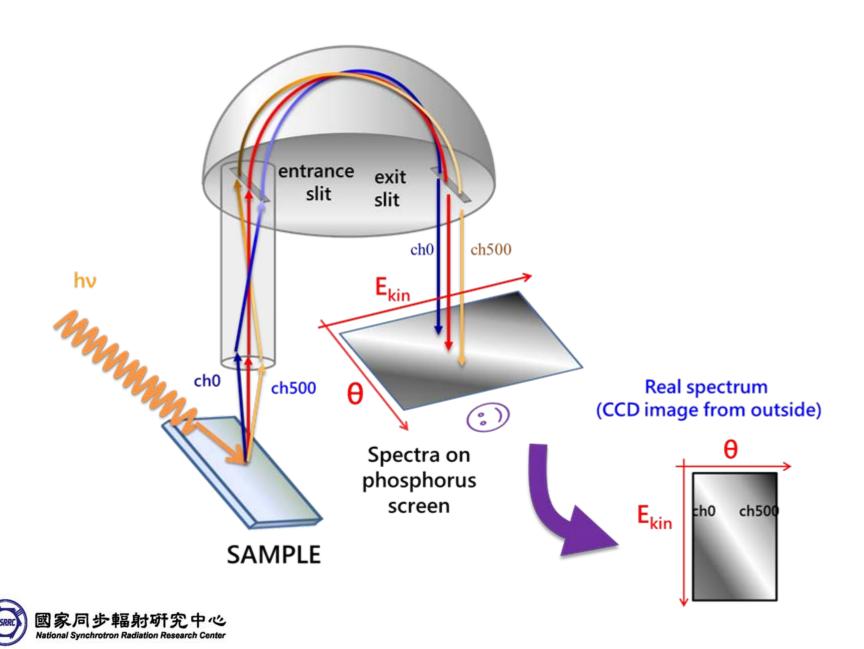


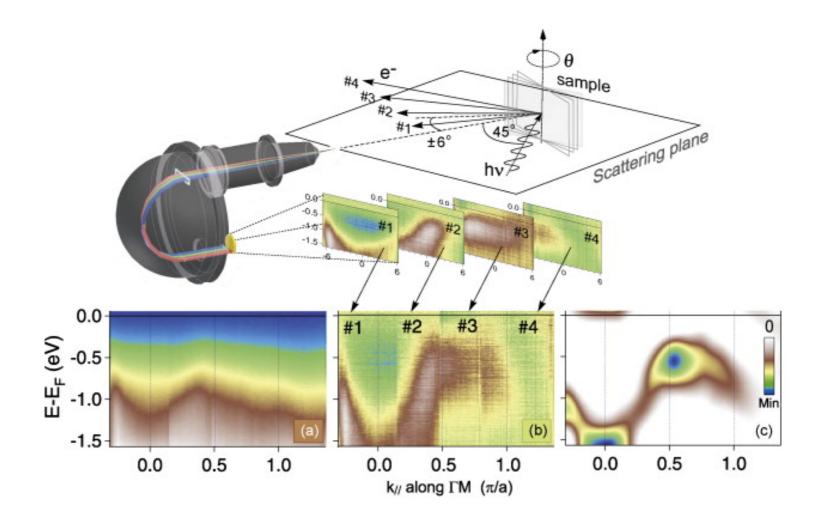
- Low photon energy provides better momentum resolution.
- We expect to study the electronic structure of solids at low photon energies (10 eV~ 100 eV).

SCIENTA R4000 Side View





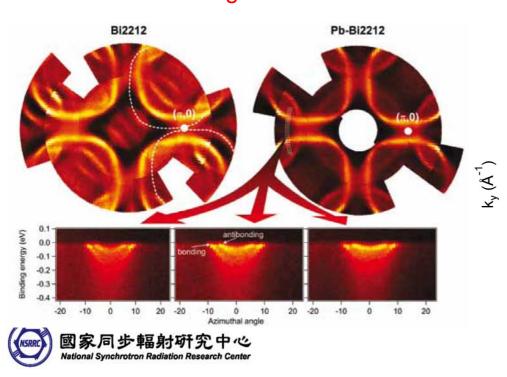


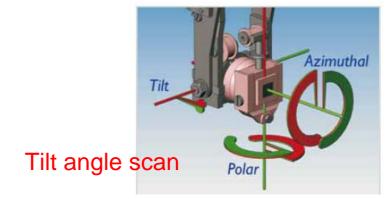


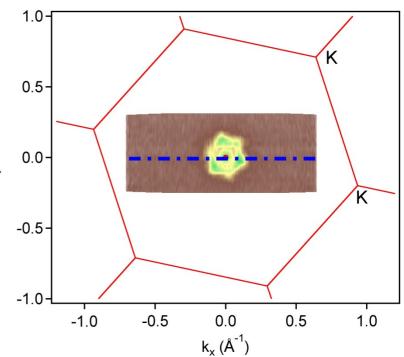


Angle is the soul of ARPES: Band mapping

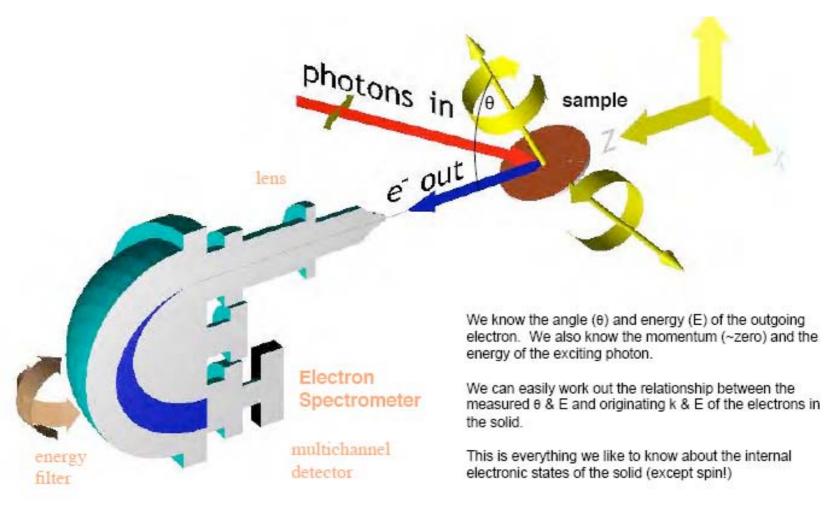
Azmuthal angle scan





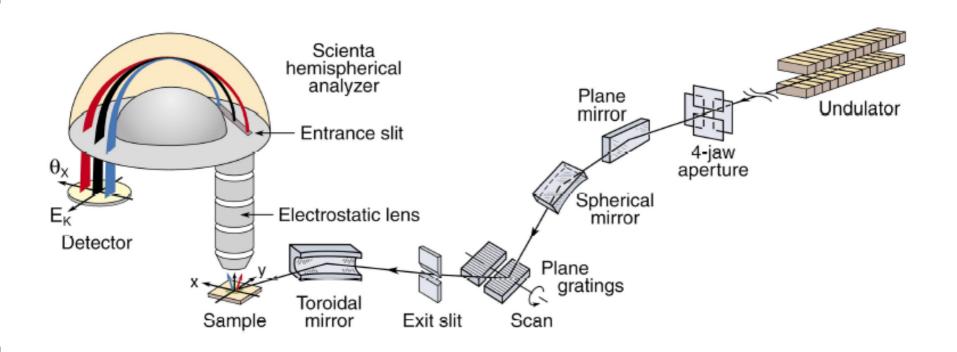


Experimental geometry





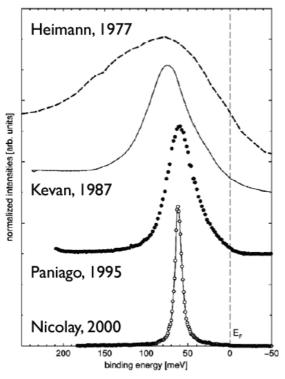
Beamline design for modern high resolution photoemission spectroscopy





The state-of-the-art in electron spectroscopy

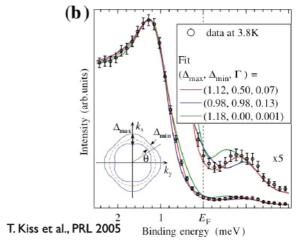
Evolution of instrumental resolution over time



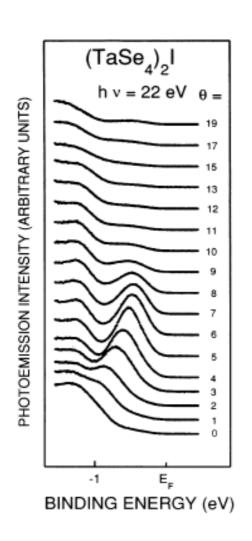
F. Reinert et al., PRB (2001)







Early ARPES experimental result



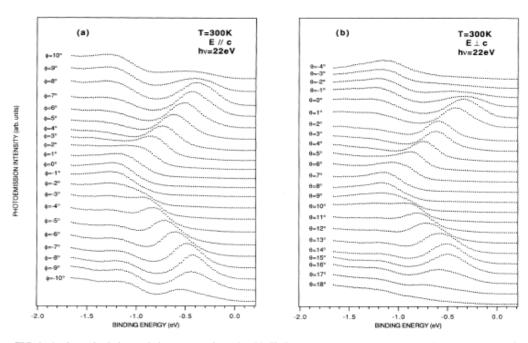


FIG. 1. Angle-resolved photoemission spectra taken using 22-eV photon energy, at room temperature, for photon electric field (a) parallel and (b) perpendicular to the conducting axis. The emission angle is along the conducting axis, with the surface normal defined as 0°.

Now a 2-D detector with ± 30° and 0.1° angular resolution can be obtained.

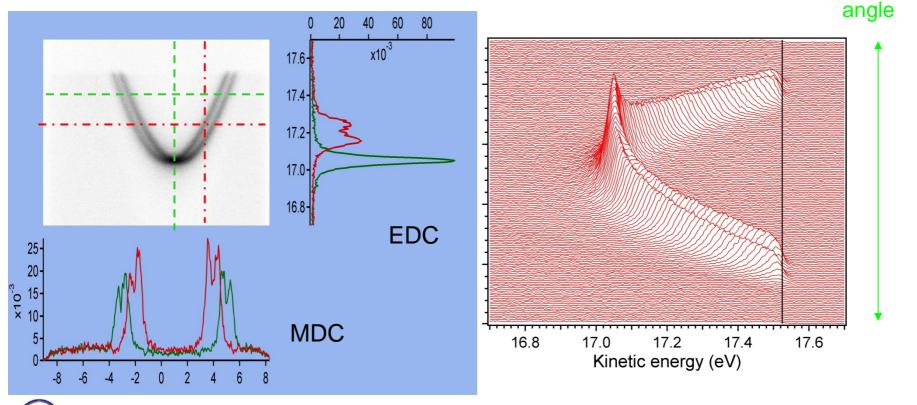


FIG. 1. A series of high-energy-resolution angle-resolved photoemission spectra, taken along the direction of the sample and for different values of the azimuthal angle.

Typical Experimental Result

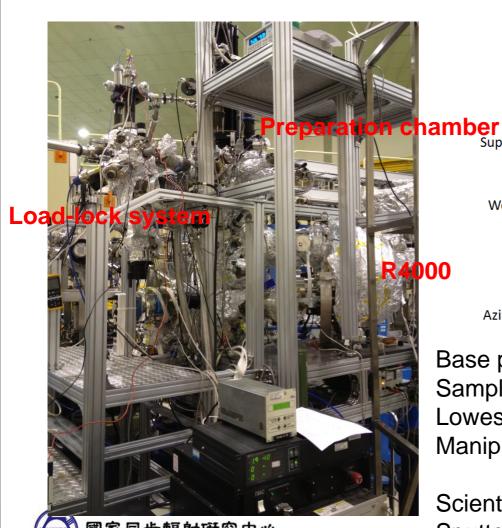
Accumulate spectra of Rashba effect on Au(111) as the angle is scanned

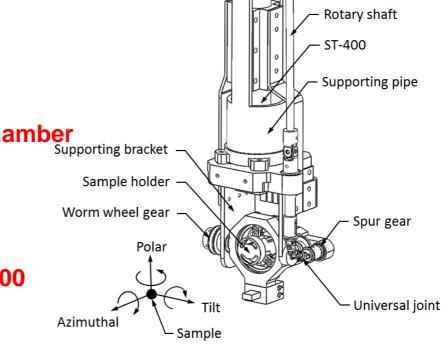
Emission





Current status of ARPES end station





Base pressure: 4.5x10⁻¹¹ torr

Sample Preparation: *in-situ* cleave, MBE growth

Lowest temperature range : 10 K

Manipulator: 6-axis motorized manipulator

Scienta R4000 analyzer, LEED, RHEED, Sputtering, Load-lock system

Probe the electronic structure of materials

- Angle-resolved photoemission spectroscopy (ARPES) is the most general tool to probe band structure, low-lying excitations or spectral function mapping.
- Scientific topics for current users :
 - Molecular thin film/metal systems
 - Metal/semiconductor systems
 - Cuprates and complex oxides
 - Graphene based materials
 - Topological insulators
 - Iron-based superconductors



Electron Escape Depth : Surface Sensitivity

Why are electrons so useful as probes of surfaces?

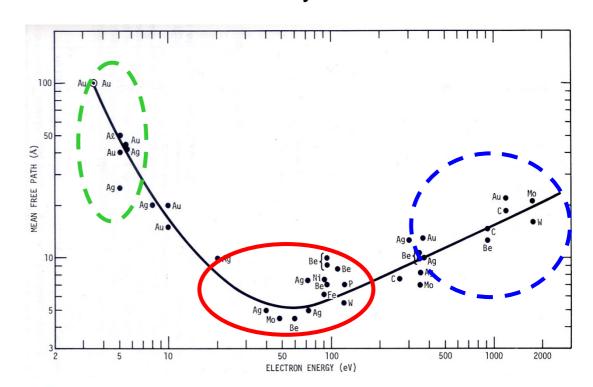
Or

Not so useful for studying bulk properties!!

Minimum due to electron-electron scattering, mainly plasmons

PES is a surface sensitive technique! (requires UHV)

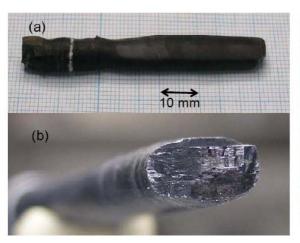
High energy photoemission: several keV to increase bulk sensitivity

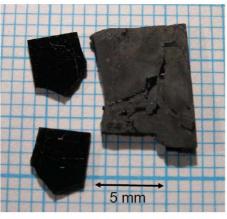




The requirement of ARPES

- UHV environment : better than 1x10⁻¹⁰ Torr
- Single crystals or in-situ growth thin films
- Conductors or semiconductors
- Tunable photon energies





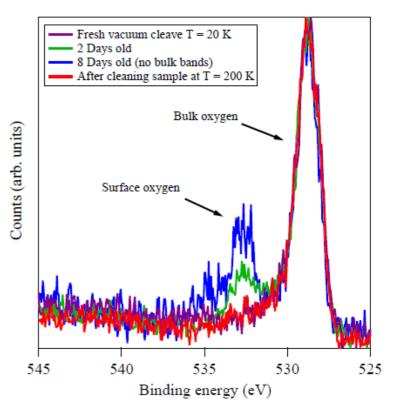


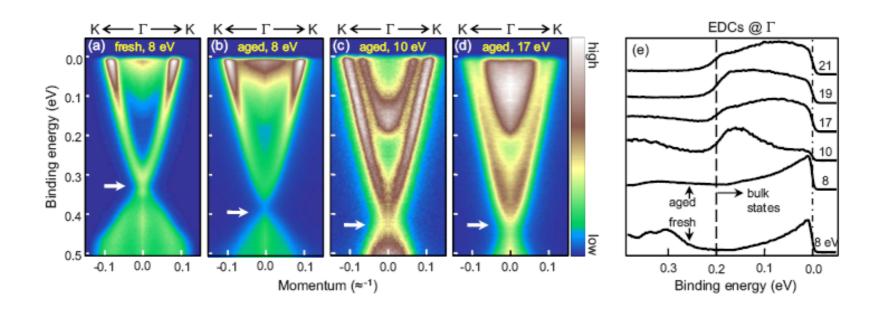
Figure 5.2: (color) The oxygen 1s peaks from Bi2212 at different times after the cleave. A constant background was subtracted from each spectrum to allow direct comparison. The peak derived from bulk oxygen is stable over time, while the surface oxygen peak grows as more oxygen sticks to the cold surface.



HC Hsu, Ph.D. Thesis NTNU(2010) Koralek, U. Colorado Ph.D. Thesis (2007)

Impurity doping on topological insulators

Base pressure : 1x10⁻¹⁰ Torr Bi₂Se₃ single crystal

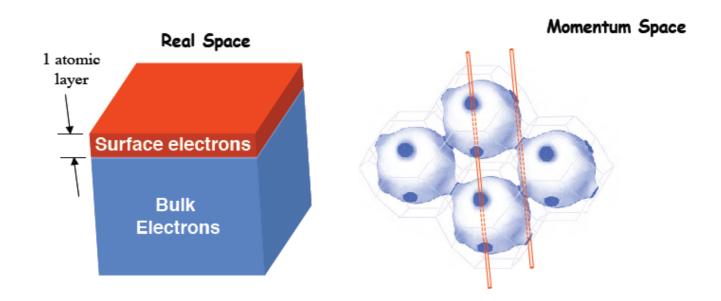




Single crystals or *in-situ* growth wellordered thin films are good candidates for ARPES measurement



Surface state

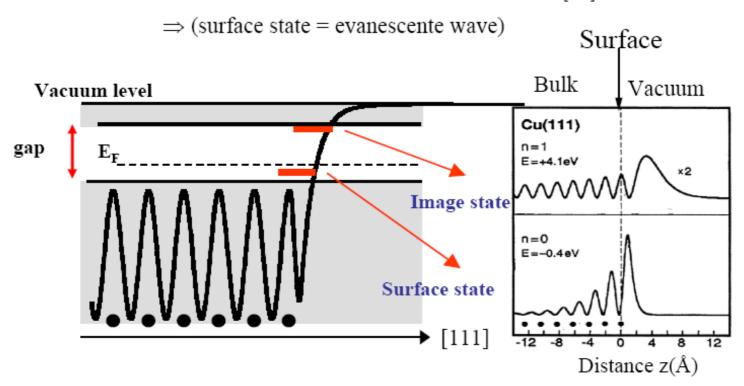


Surface states are highly localized in real space, therefore completely delocalized in k-space along kz.

- NO DISPERSION OF SURFACE STATES in kz direction



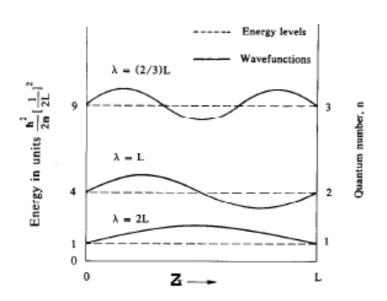
- Surface = Breakdown of the translational symmetry
- \Rightarrow Peculiar solution in the gap with a complexe wave vector $\mathbf{k}_{[111]}$



→localisation of the electronic density at the surface Surf. State is very sensitive to any structural modification



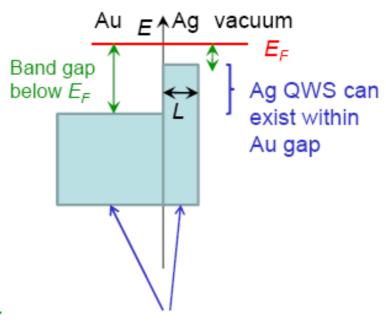
Quantum well states



Quantized discretely along z-direction Energy levels depend on film thickness L

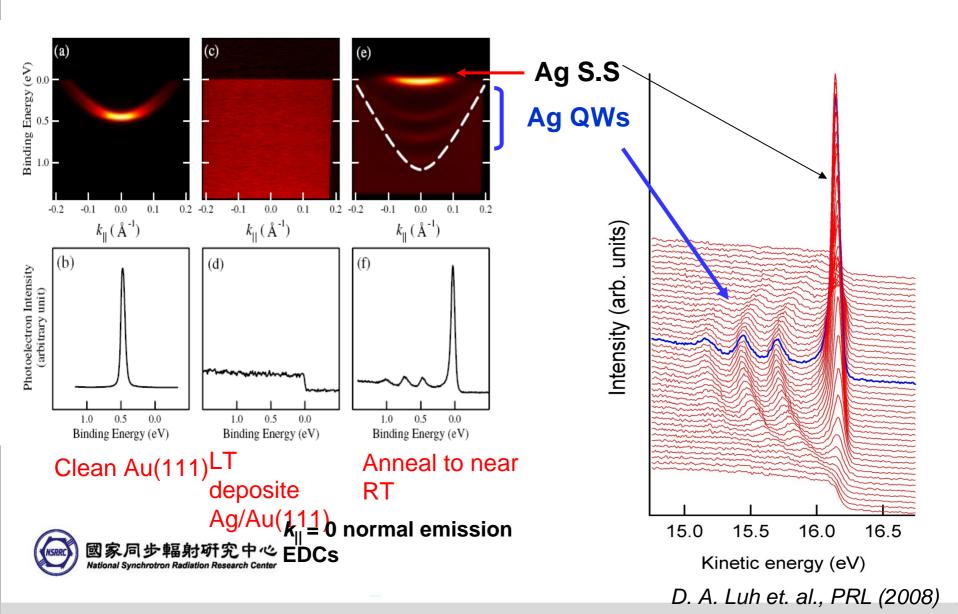
Nearly free electron like in xy-plane

Ag(111) thin films expitaxially grown on Au(111) substrate



Bulk projected bands along Γ L of Au and Ag, respectively

Absolute coverage of thin films: Ag/Au(111) system



Dynamically monitor the thin film growth mechanism

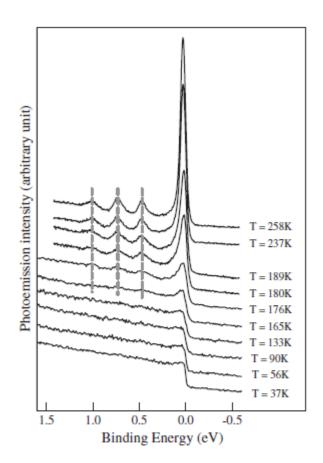
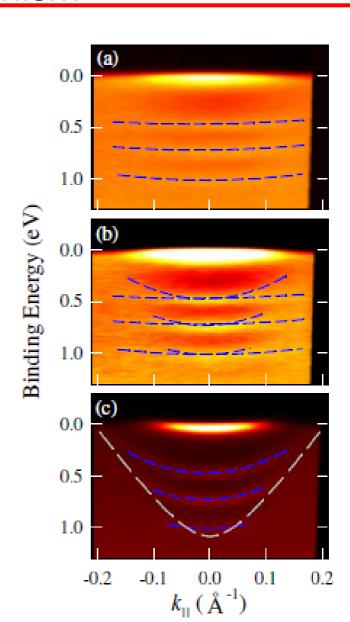
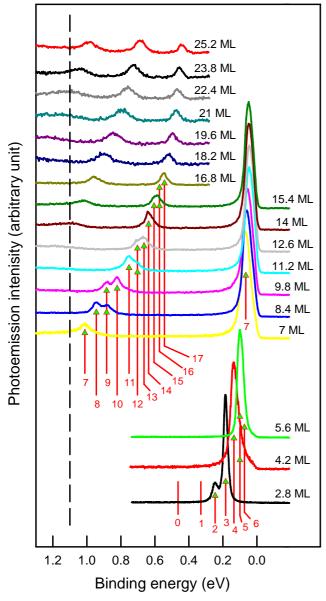


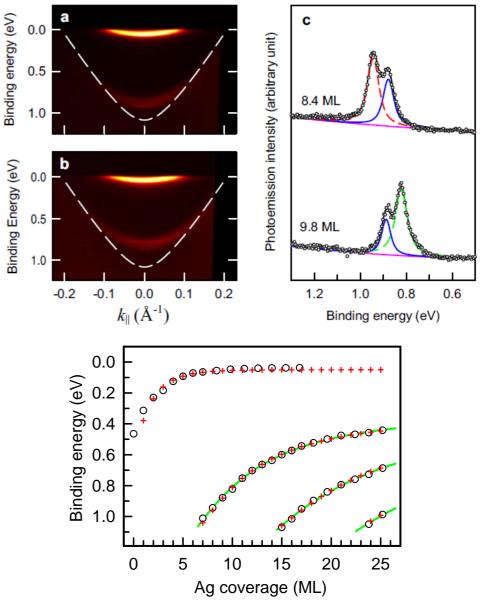
FIG. 2. Energy distribution curves of normal emission from Ag (22 ML) on Au(111) annealed at the indicated temperatures; intensities have been scaled variously for stacking presentation.









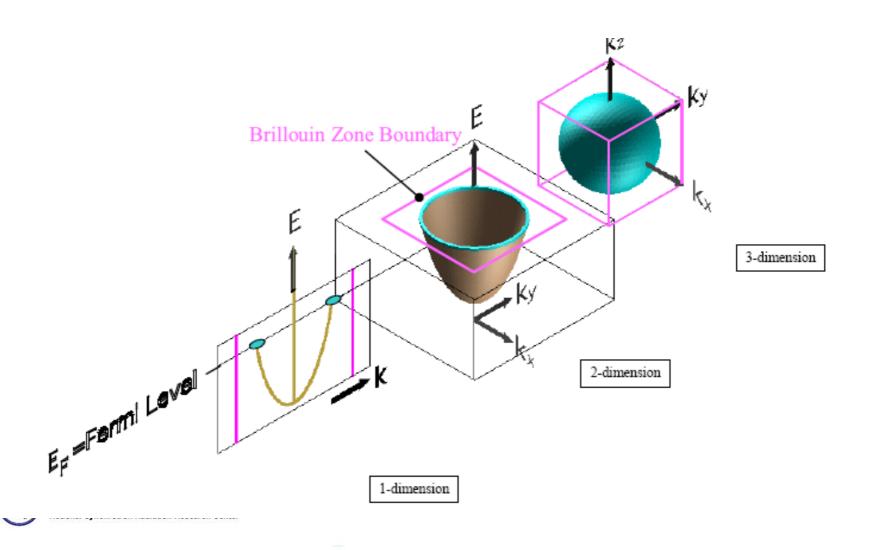


C.-M. Cheng et al., APL (2008)

C.-M. Cheng et al., J. Phys. D: Appl. Phys. (2008)

D.-A. Luh et al., PRB (2008)

Fermi Surface

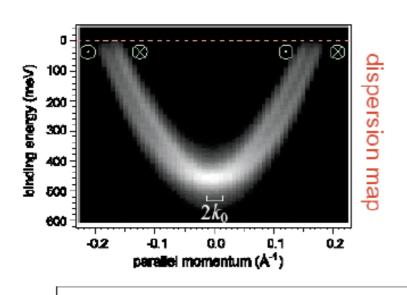


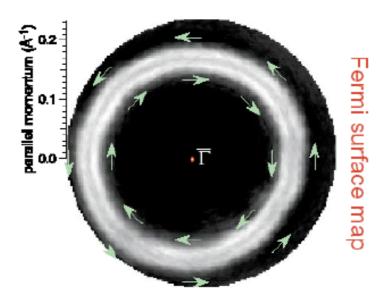
Surface state

The Shockley surface state on Au(111)

spin-integrated photoemission at hv = 21.1 eV, T = 160 K

instrumental resolution $\Delta E = 25 \text{ meV}, \Delta \vartheta = 0.5^{\circ} \text{ (FWHM)}$





 $2k_0 = 0.026 \text{ Å}^{-1}$

 $E_{\rm B}$ = 470 meV

 $k_{\rm F} = 0.173 \, {\rm \AA}^{-1} \pm k_{\rm O}$

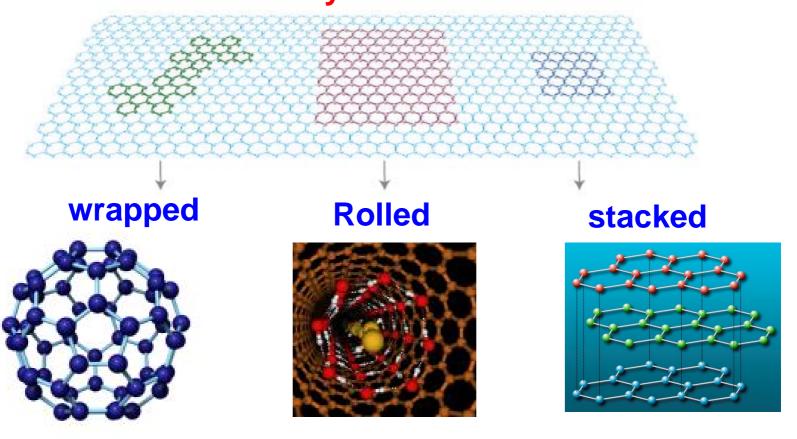
 $m^* = 0.24 m_e$



The electronic structure of graphene

Graphene is the mother of them all!

Very good conductors Extremely thin and resistant



Zero dimensional: 國家同步輻射研究中心 Nation in the Property Center

One dimensional: carbon nanotubes

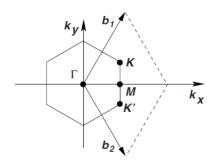
Three dimensional: graphite

Why graphene

- The strictly two-dimensional material
 - Exceptionally high crystal and electronic quality
- Unusual electronic spectrum
 - New paradigm of 'relativisity' condensed-matter physics
- Graphene-based electronics : new cadidate material to take over from Si
 - High mobility, high carrier density, high v_F
 - Tunable gap by electrical field : Field-effect transistor (FET), Single-electron-transistor (SET)
 - Superconducting field effect transistor and Spin valve, Composite material for electric battery, hydrogen storage material

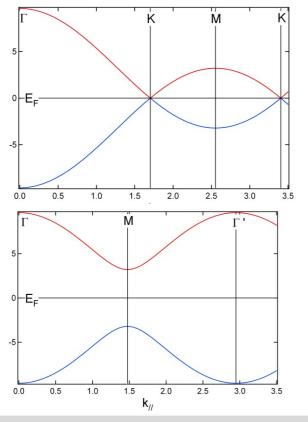


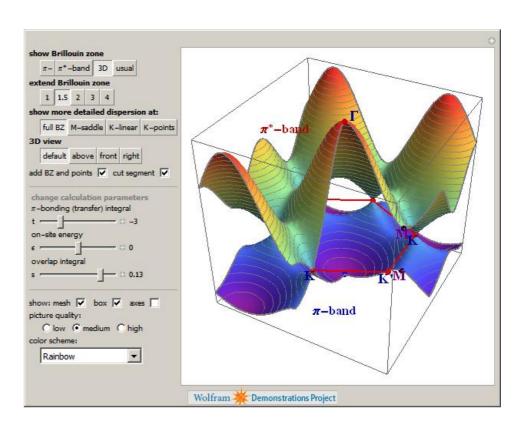
Pure 2D material: graphene



$$\boldsymbol{b}_1 = \frac{2\pi}{3a}(1,\sqrt{3}), \quad \boldsymbol{b}_2 = \frac{2\pi}{3a}(1,-\sqrt{3})$$

$$\mathbf{K} = \left(\frac{2\pi}{3a}, \frac{2\pi}{3\sqrt{3}a}\right), \quad \mathbf{K}' = \left(\frac{2\pi}{3a}, -\frac{2\pi}{3\sqrt{3}a}\right)$$



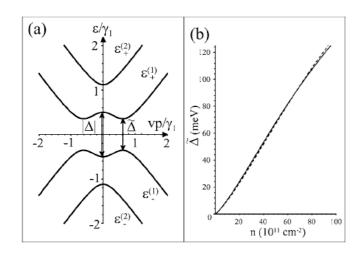


Bilayer graphene : tunable energy gap

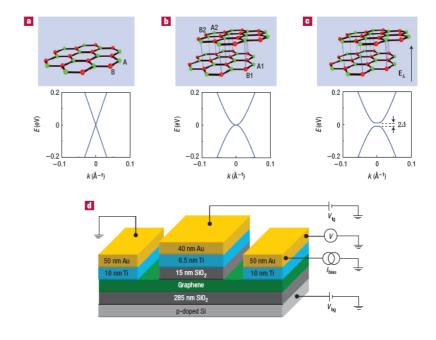
Bilayer graphene

Max. 250 meV by IR detection

Zhang et al., Nature (2009)

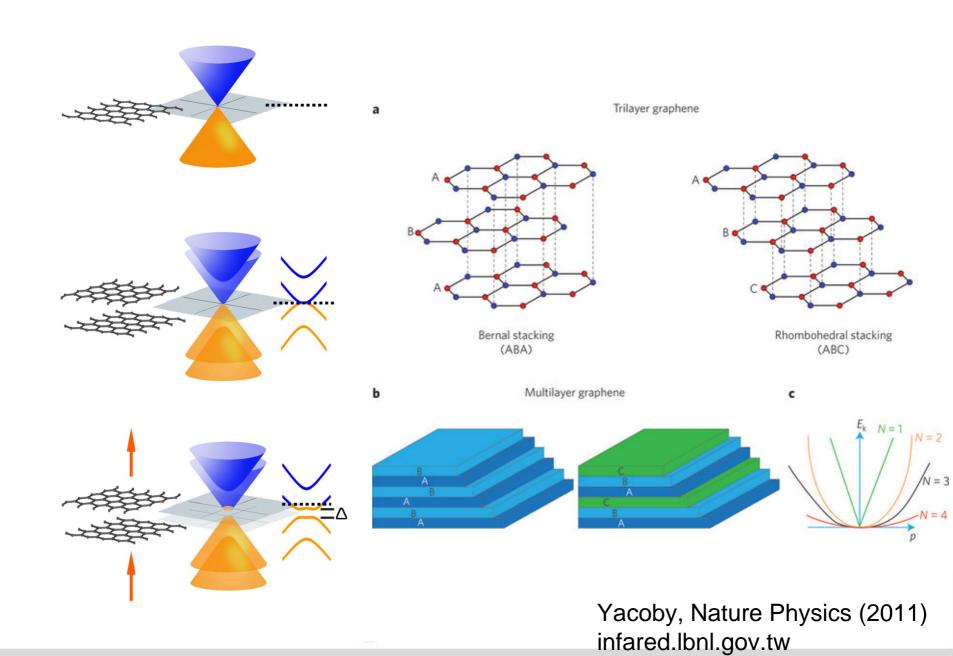


McCann, PRB (2006)



J.B. Ostinga et al., Nature Mat. (2007)





How to prepare graphene



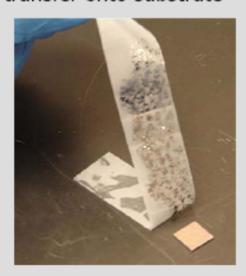
mechanical cleavage

peeling off layers of graphite with a sticky tape





transfer onto substrate



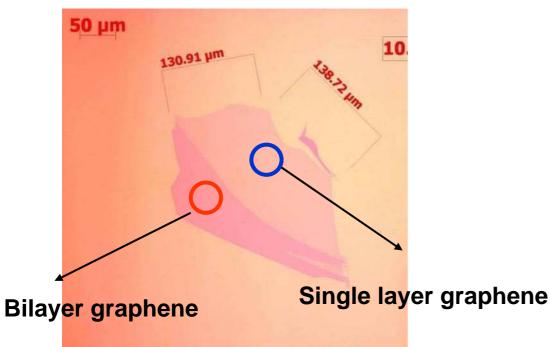


optical microscope image of resulting flakes

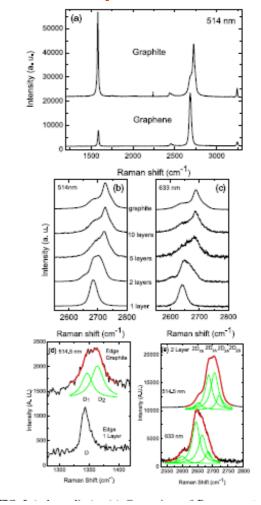


How to distinguish the thickness of graphene

SiO₂(200 nm)/Si Optical microscopy

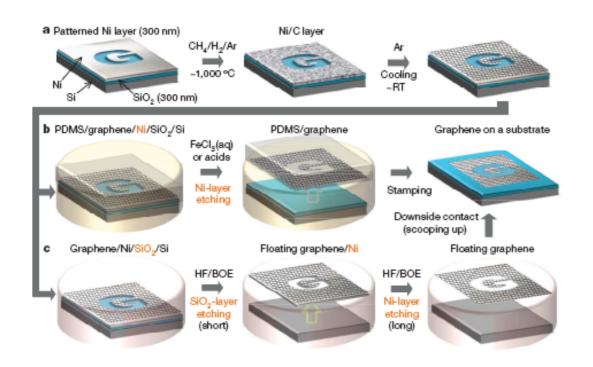


Raman spectroscopy





CVD for large scale graphene film



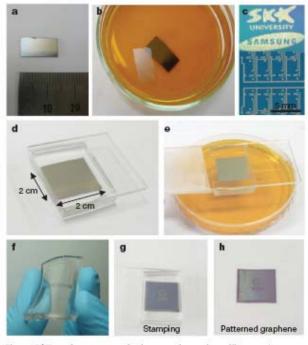
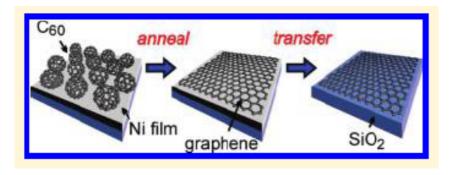
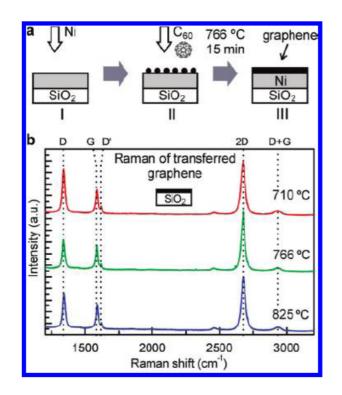


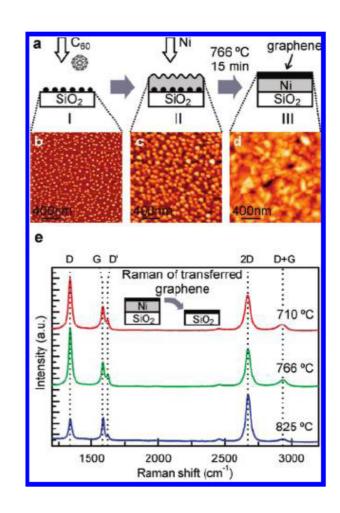
Figure 3 | Transfer processes for large-scale graphene films. a, A



Graphene formation by decomposition of C₆₀

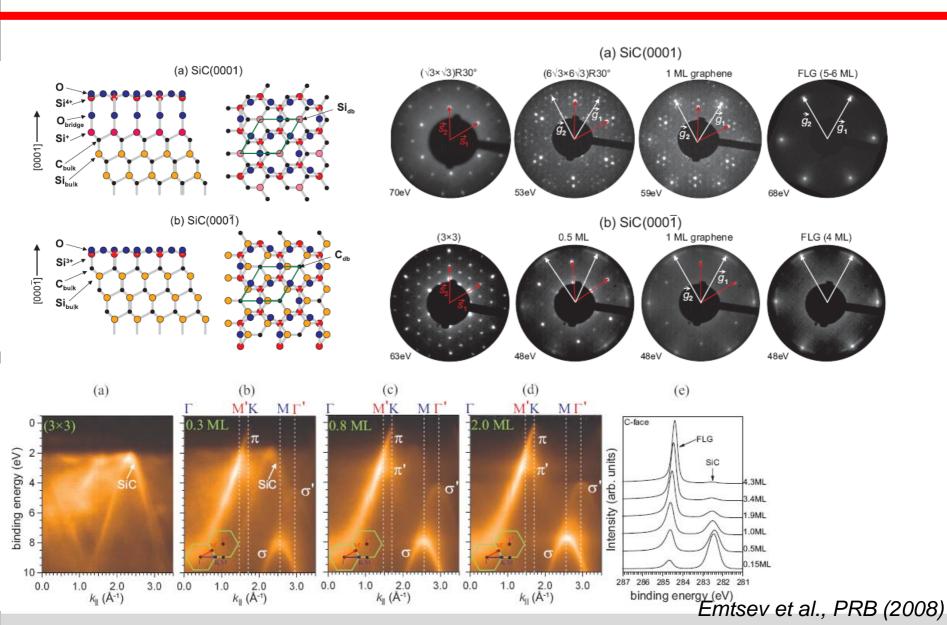




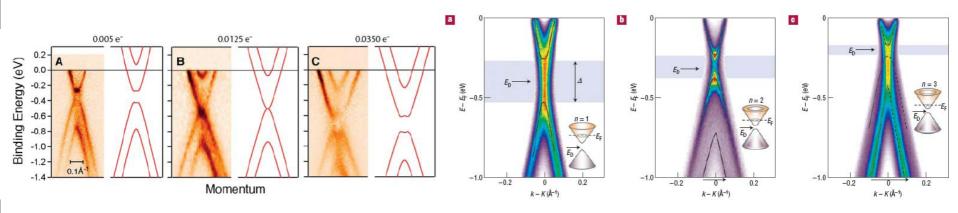




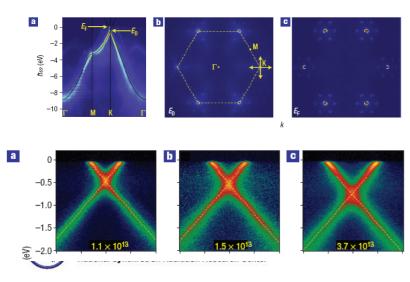
Epitaxial growth graphene on SiC



Epitaxial growth graphene on SiC

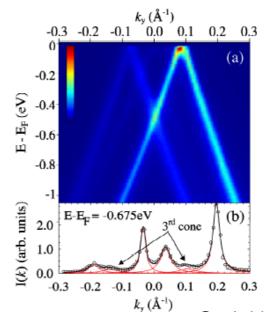


Ohta et al., Science (2007)



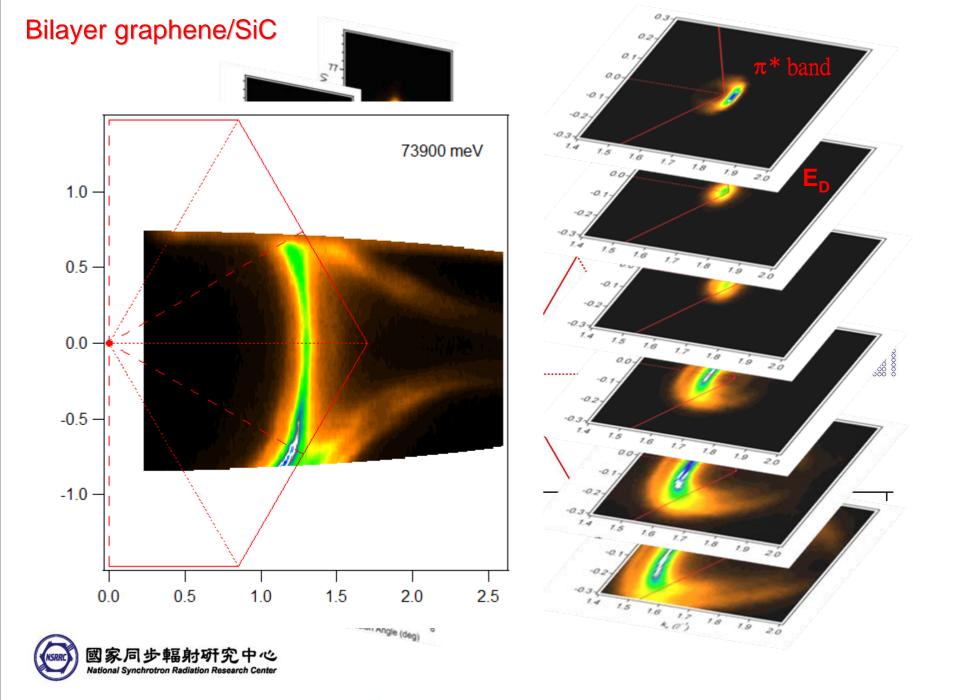
Bostwick et al., Nat. Phys. 3,36 (2007)

Zhou et al., Nat. Mat. 6,770 (2008)

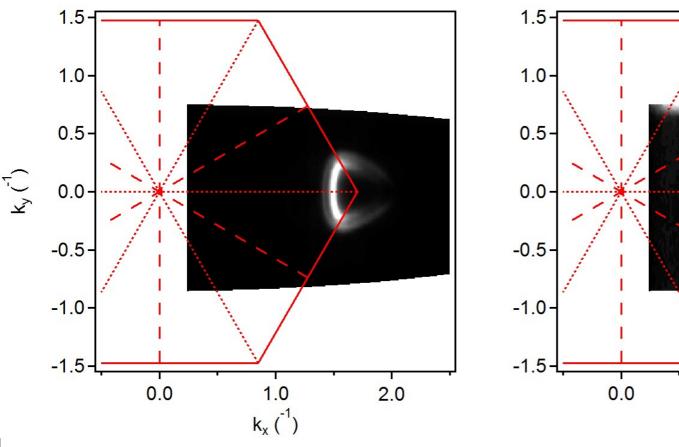


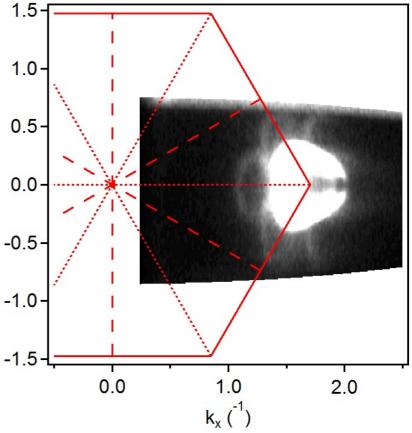
6H-SiC(000 -1)

Sprinkle et al., PRL (2009)



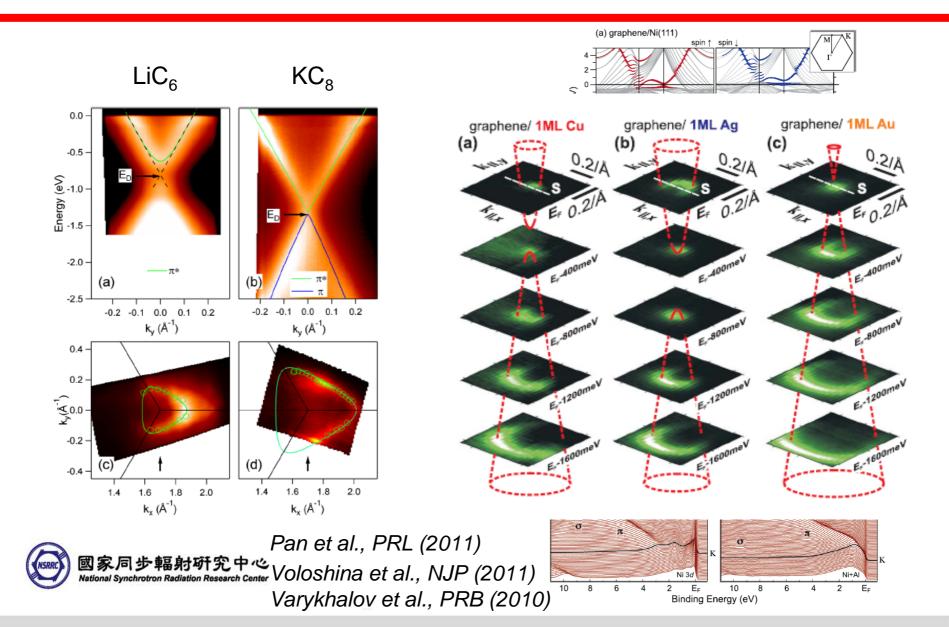
High quality graphene/SiC



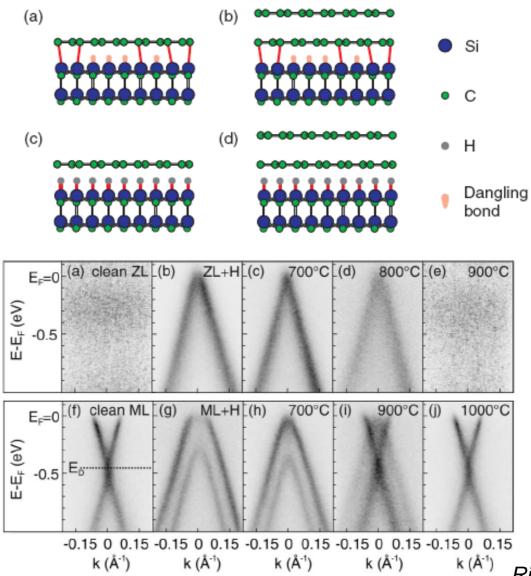




Graphene intercalated compounds (GICs)



Hydrogen intercalated graphene/SiC





Riedl et al., PRL (2009)

A intrinsic gap exists or not?

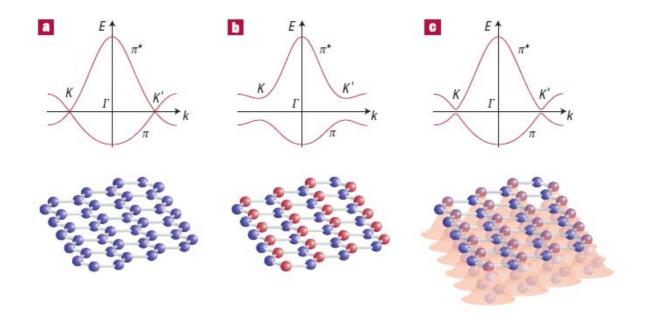


Figure 1 Schematic representation of crystal and electronic band structures (only π -bands are shown). **a**, Free-standing graphene. **b**, Boron-nitride. **c**, Epitaxial graphene. Symmetry between the sublattices in graphene guarantees gapless spectra around K points. This symmetry is broken in boron-nitride (one sublattice consists of boron atoms, another of nitrogen), which immediately opens a gap. In epitaxial graphene, the commensurate underlying potential gives rise to different on-site energies for the two sublattices, which opens a small gap around K points.



The difficulties for studying the electronic structure of exfoliated graphene

- Insulating substrates induce the strong charging effect
- Sample size: only several tens microns sample is obtained, the size is small for current ARPES beam spot in VUV region
- ex-situ sample preparation is not good for ARPES experiments

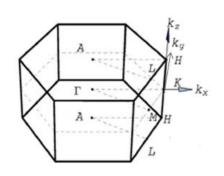


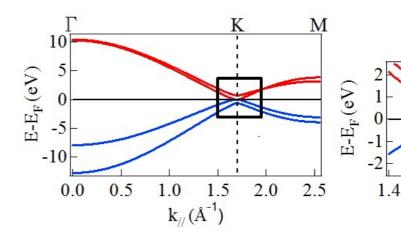
Sample preparation

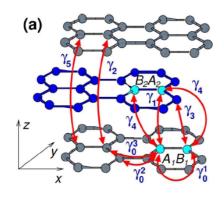
- Use highly-doped Si-substrate to replace Si capped with 200nm SiO₂ substrate.
- Anneal sample above 400 °C to flash gas condensations in UHV environment.
- Choose suitable photon energy to enhance the cross section of carbon.

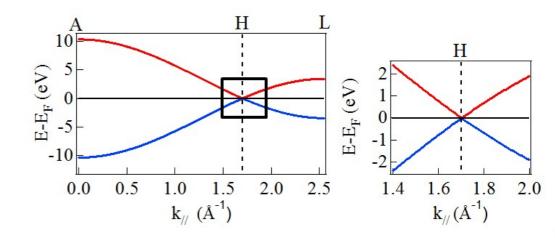


The electronic structure of graphite







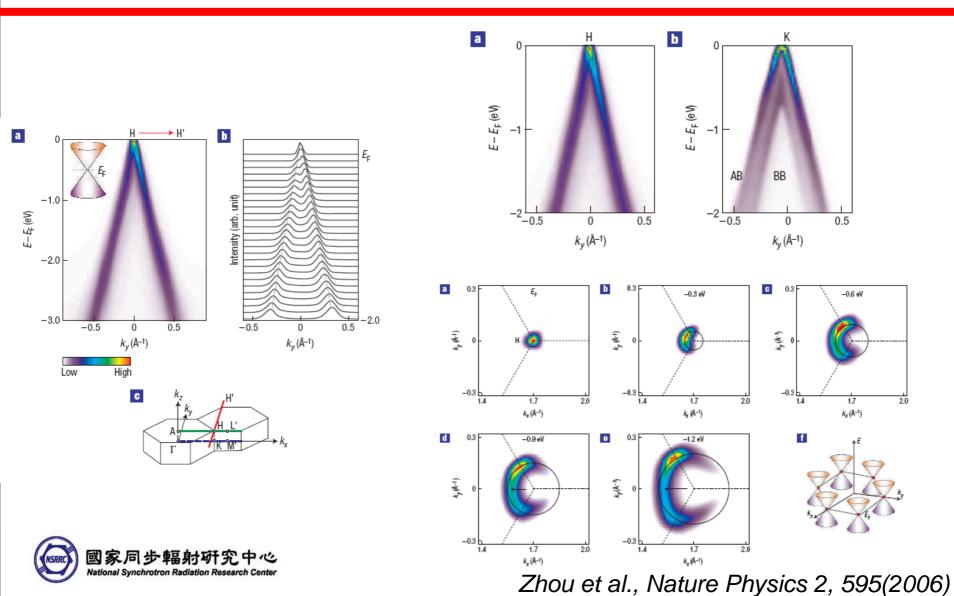


1.6 1.8

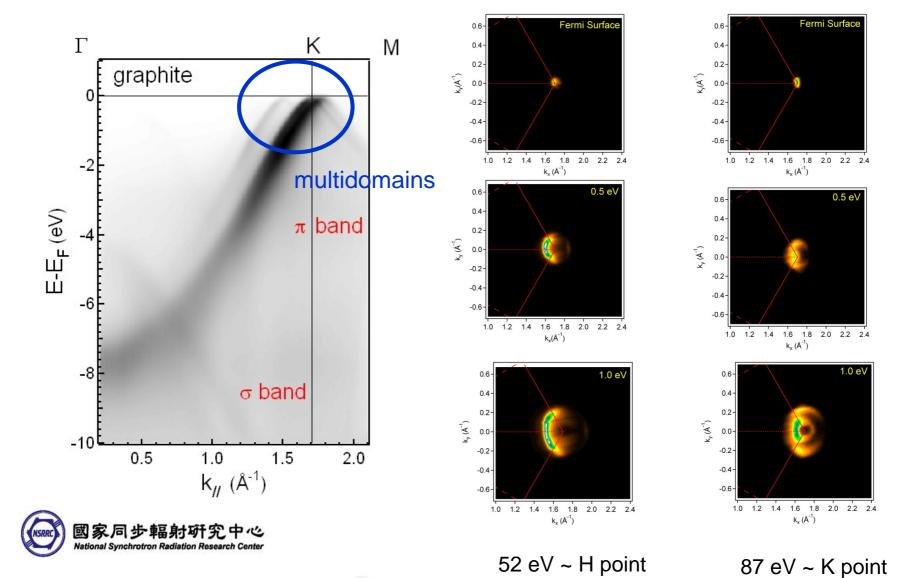
 $k_{//}(\text{Å}^{-1})$



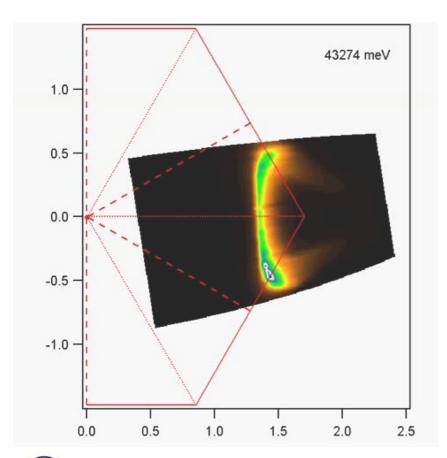
Early ARPES work on graphite

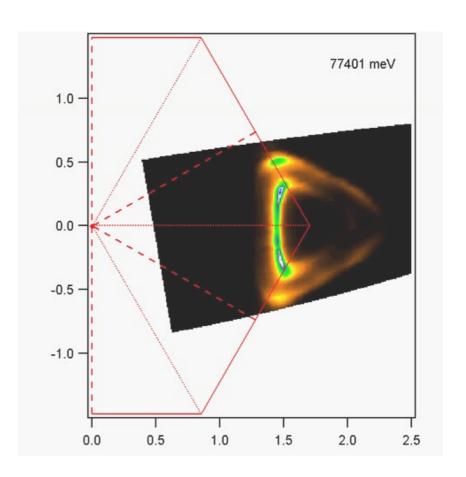


The band mapping result of Kish graphite



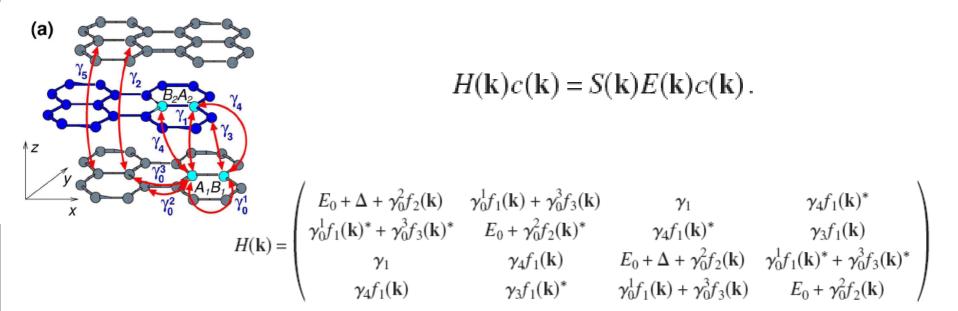
Constant energy mapping of graphite







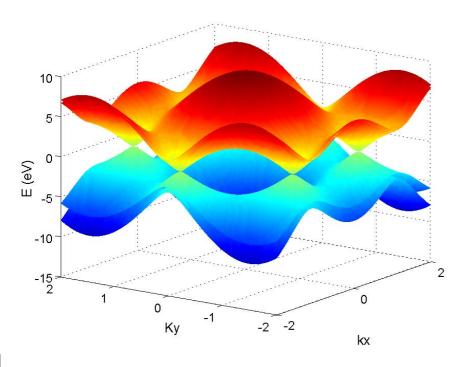
3NNN SWMc Hamiltonian of bilayer graphene

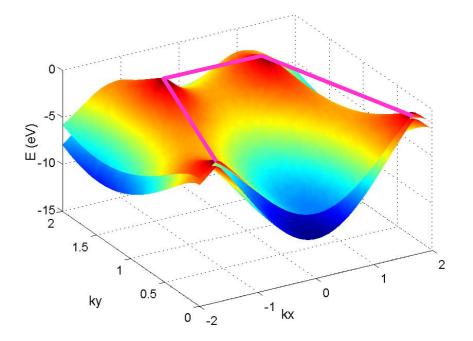


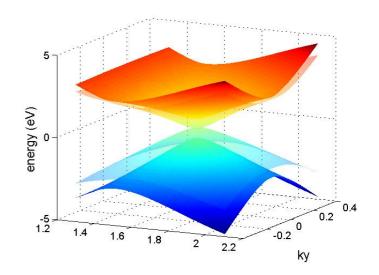
$$S(\mathbf{k}) = \begin{pmatrix} 1 + s_0^2 f_2(\mathbf{k}) & s_0^1 f_1(\mathbf{k}) + s_0^3 f_3(\mathbf{k}) & 0 & 0 \\ s_0^1 f_1(\mathbf{k})^* + s_0^3 f_3(\mathbf{k})^* & 1 + s_0^2 f_2(\mathbf{k})^* & 0 & 0 \\ 0 & 0 & 1 + s_0^2 f_2(\mathbf{k}) & s_0^1 f_1(\mathbf{k})^* + s_0^3 f_3(\mathbf{k})^* \\ 0 & 0 & s_0^1 f_1(\mathbf{k}) + s_0^3 f_3(\mathbf{k}) & 1 + s_0^2 f_2(\mathbf{k}) \end{pmatrix}$$



Simulation result of the $\,\pi\,$ band for bilayer graphene

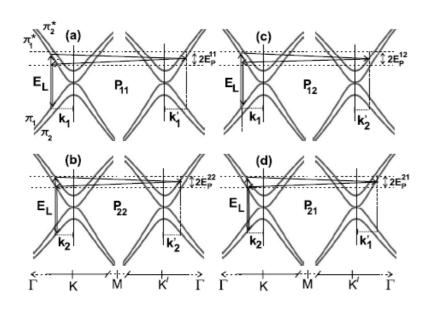


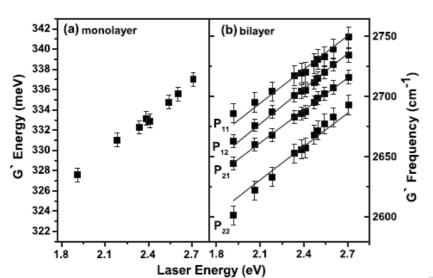






TBM parameters determined by rasonance Raman scattering





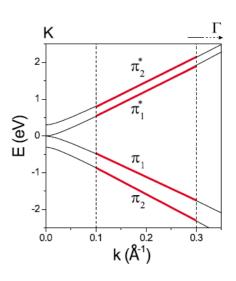
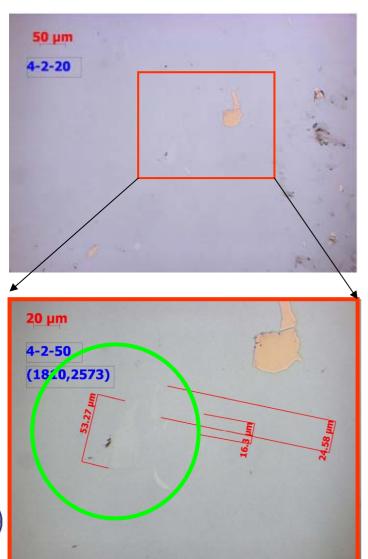


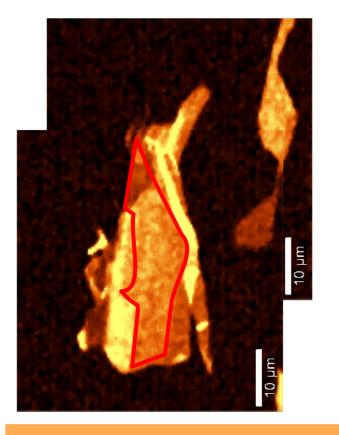
TABLE II. Experimental SWM parameters (in eV) for the band structure of bilayer graphene. The parameters for graphite are taken from Refs. 18 and 19.

		γ_0	γ_1	γ_2	γ_3	γ_4	γ_5	$\gamma_6 = \Delta$
Bilayer graphe	ıe	2.9	0.30	n/a	0.10	0.12	n/a	n/a
Graphite		3.16	0.39	-0.02	0.315	0.044	0.038	0.008

Malard et al.,PRB (2007)

Bilayer graphene / Highly doped Si substrate



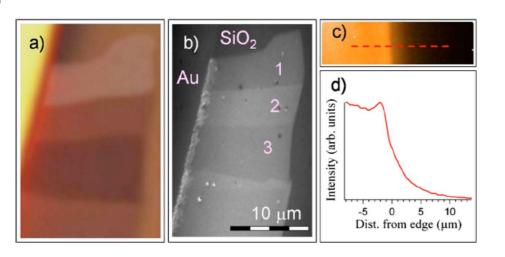


Intensity of G band (overlap of 2 scans showing flake 1 and 3)

Raman result from Germany,, the bilayer graphene should be the area marked in red.



The electronic structure of single layer graphene on SiO₂ (200nm)



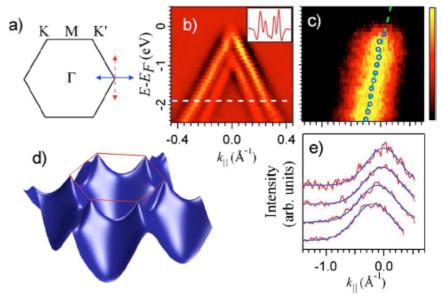
graphite graphene

graphite graphene

graphite graphene

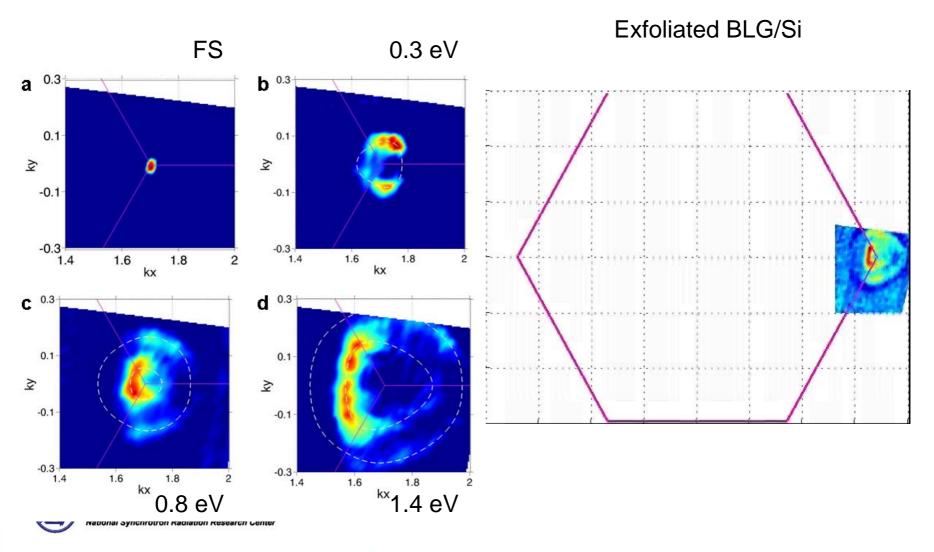
graphite graphene

- Use lithography to pattern graphene flake with gold contact
- 2. Microfocus beam size $< 5 \mu$ m

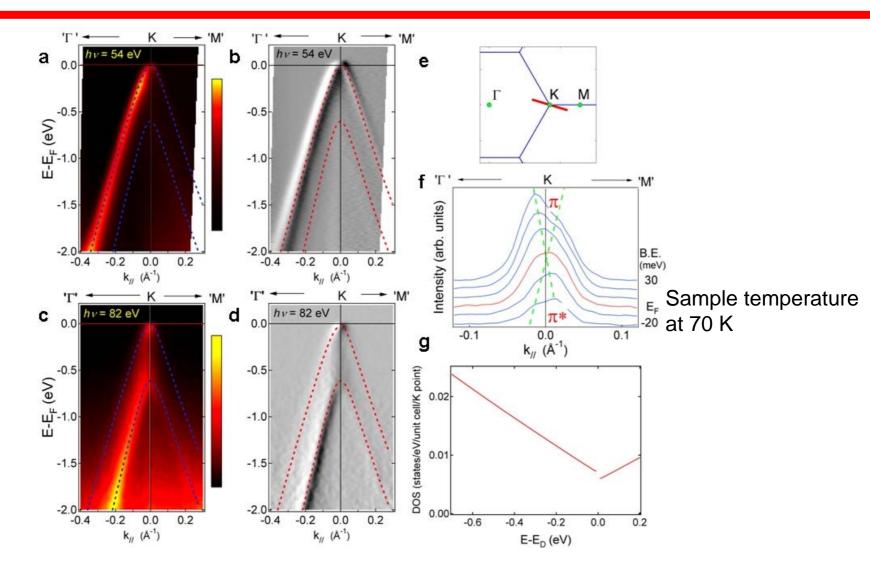


Fit TBM parameters to high binding energy

Data were taken at 82 eV

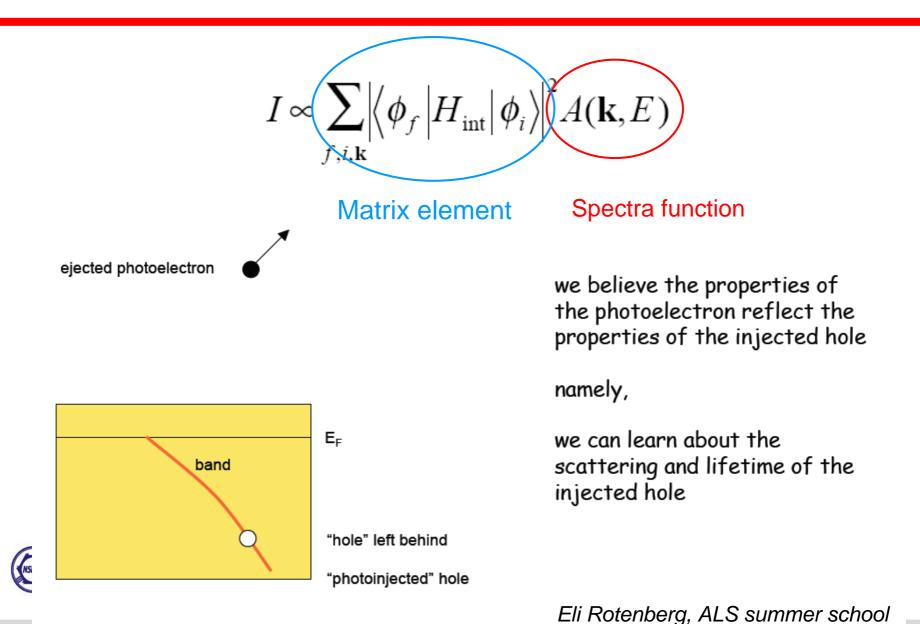


The electronic structure of bilayer graphene

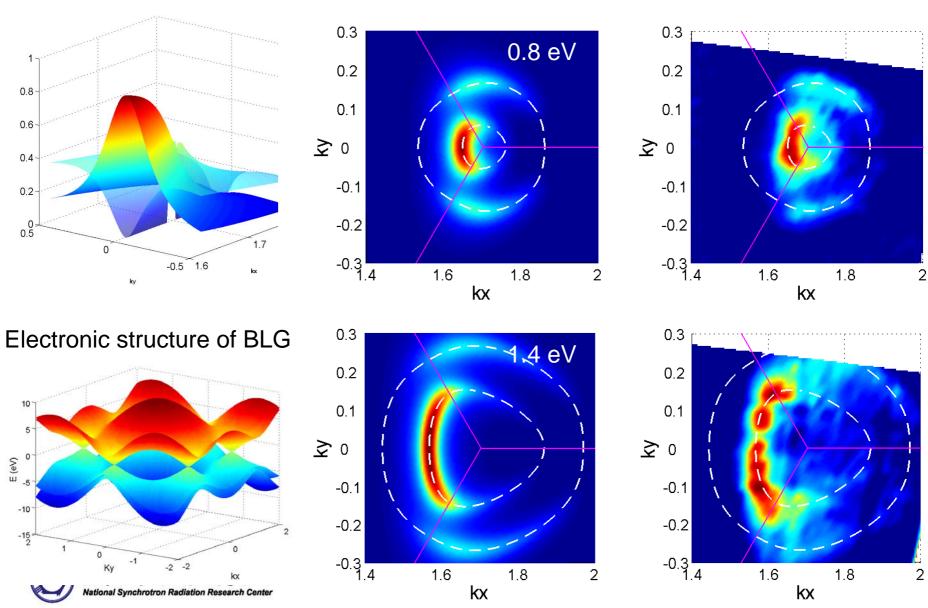




What does ARPES measure



82 eV ME effect



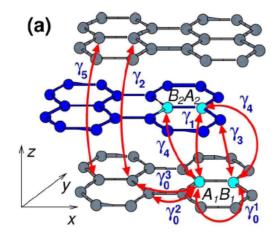
TB parameters for experimental and theoretical results

TABLE I. 3NN tight-binding parameters for few-layer graphene and graphite. All values except the ones for s_0^1 , s_0^2 , and s_0^3 are in eV. The parameters of fits to LDA and GW calculations are shown. The 3NN Hamiltonian is valid in the whole two (three) dimensional BZ of graphite (graphene layers).

Method	γ_0^1	γ_0^2	γ_0^3	s_0^1	s_0^2	s_0^3	γ_1	γ_2	γ ₃	γ_4	γ_5	E_0	Δ
3NN TB-GW a	-3.4416	-0.7544	-0.4246	0.2671	0.0494	0.0345	0.3513	-0.0105	0.2973	0.1954	0.0187	-2.2624	0.0540 ^b
3NN TB-LDA ^a	-3.0121	-0.6346	-0.3628	0.2499	0.0390	0.0322	0.3077	-0.0077	0.2583	0.1735	0.0147	-1.9037	0.0214
EXPc	-5.13	1.70	-0.418	-0.148	-0.0948	0.0743							
3NN TB-LDA ^d	-2.79	-0.68	-0.30	0.30	0.046	0.039						-2.03	

^aThis work.

^dFit to LDA by Reich et al. (Ref. 20).



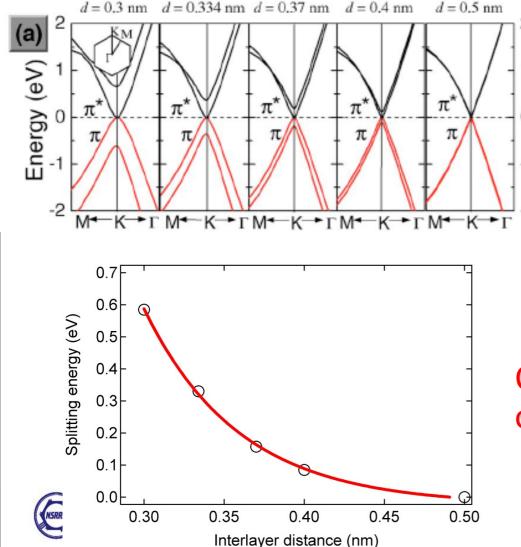
TB parameters	γ_0	γ_1	γ_3	γ ₄
Pres. work	-3.21	0.61	0.39	0.15
Prev. bilayer/SiC	-3.24	0.48		
Prev. graphite	-3.16	0.39	0.315	0.044

^bWe adjusted the impurity doping level in order to reproduce the experimental value of Δ .

^cFit to ARPES by Bostwick et al. (Ref. 22).

Strong interlayer interaction induced smaller interlayer spacing on BLG?

Interlayer spacing of neutral BLG



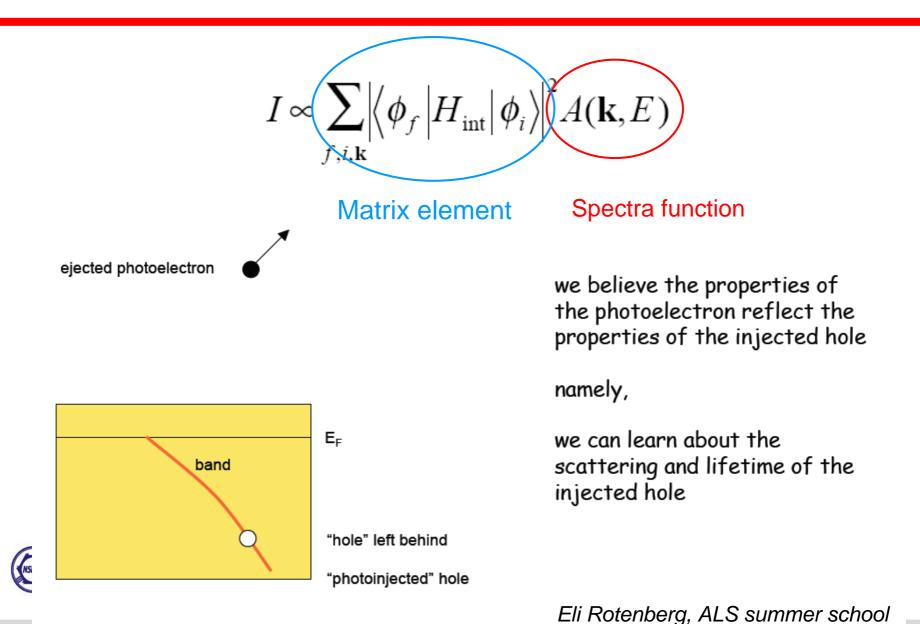
Graphite: 3.35 Å

BLG/SiO₂ with 0.61 splitting energy: 2.99 Å

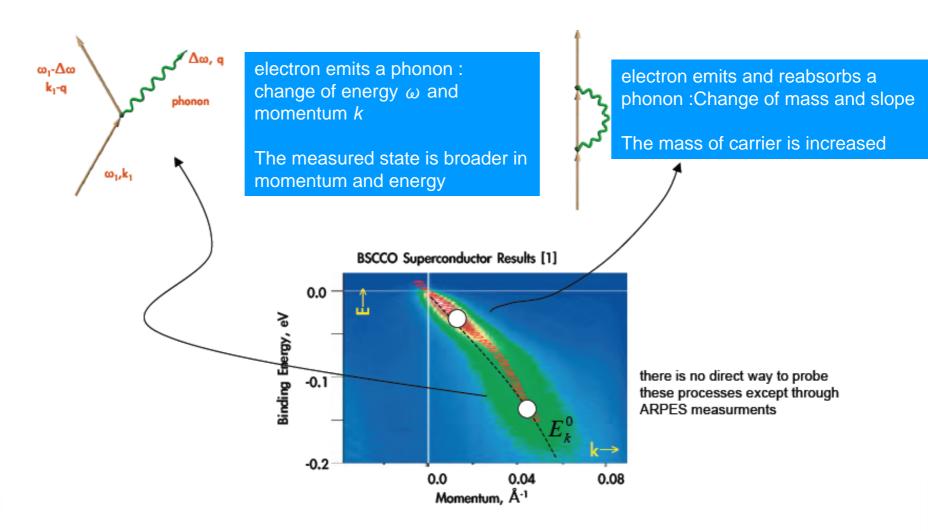
Consistent with larger γ_1 in our case

Y. Guo et. al., APL (2008)

What does ARPES measure



The carriers have a finite lifetime due to absorption and emission of phonons and other excitations



Self energy in photoemission spectra

The quantity determined in ARPES experiments is the single-particle spectral function

$$G(k,\omega) = \frac{1}{\omega - \varepsilon_k - \Sigma(k,\omega)}$$

$$A(k,\omega) = \frac{\operatorname{Im}\Sigma(k,\omega)}{\left[\omega - \varepsilon_k - \operatorname{Re}\Sigma(k,\omega)\right]^2 + \left[\operatorname{Im}\Sigma(k,\omega)\right]^2}$$

$$\Sigma = \text{Re}\,\Sigma + i\,\text{Im}\,\Sigma$$



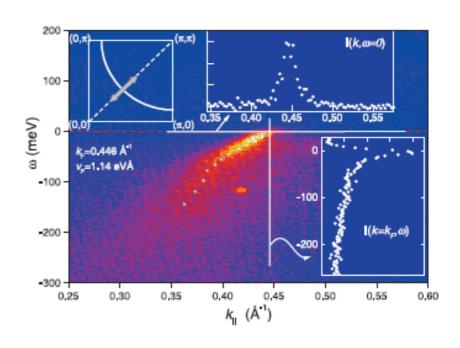
Dispersion:

E-k Relation (Velocity; Effective mass etc.)



Scattering rate (Lifetime)

Optimally doped Bi-2212 cuprate



$$\hbar v_k \Delta k = \frac{\hbar v_k}{l} = \left| 2 \operatorname{Im} \Sigma(k, \omega) \right|$$

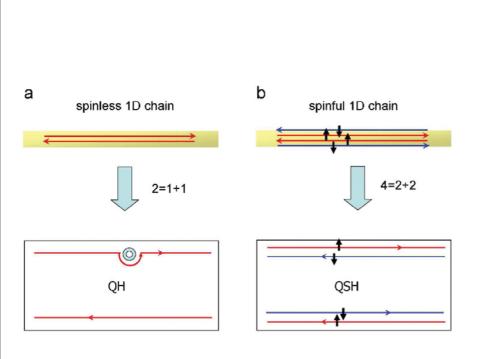
T. Valla et al., Science 285, 2110 (2000)

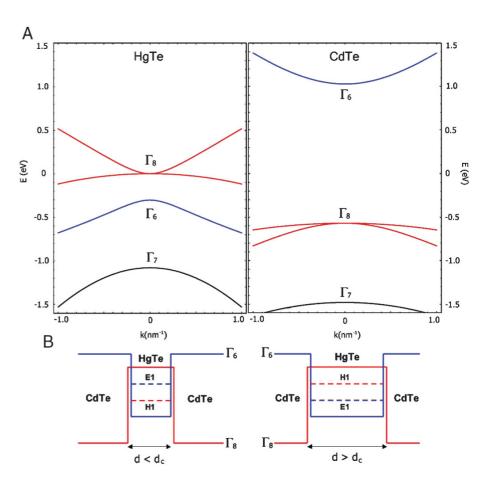
Summary for graphene

- The free standing bilayer graphene is gapless semiconductor.
- The splitting energy is larger than epitaxial graphene and bulk graphite due to the stronger screening effect.
- A reliable TBM parameters be obtained from presented experimental result.



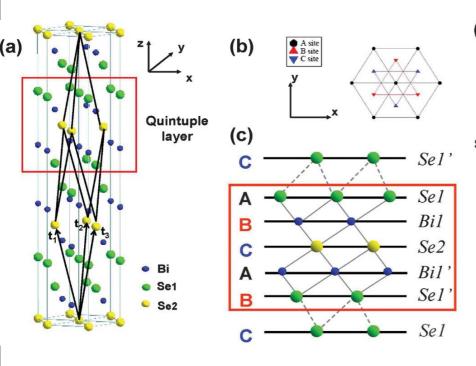
Topological insulators

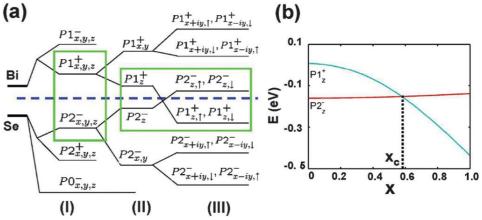






3D topological insulators

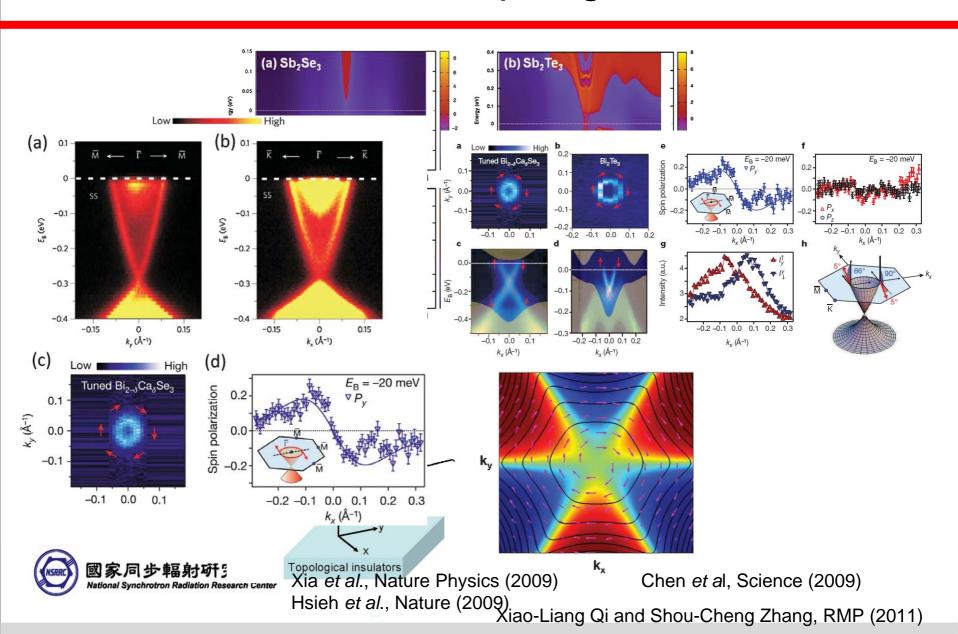




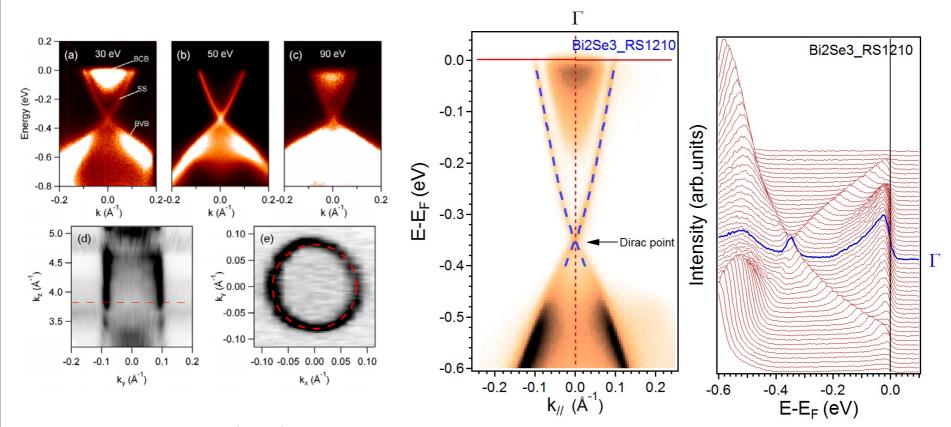
Strong spin-orbit coupling Band inversion



Predictions for 3D topological insulators



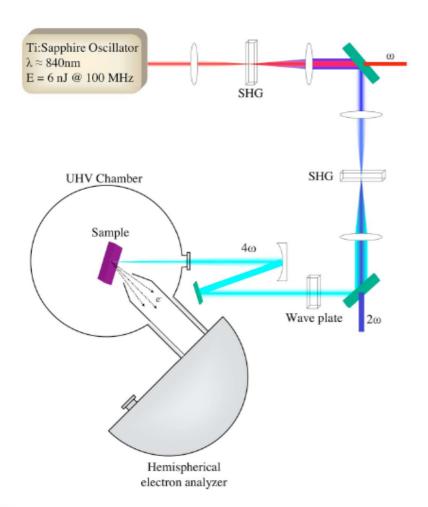
Typical experimental result at NSRRC



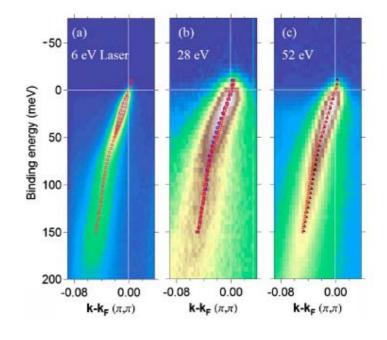
Pan et al., PRL (2011)



Setup for Laser ARPES



Band mapping with various photon energies on Bi-2212





Koralek et al., Rev. Sci. Instrum. (2007)

Time-resolved ARPES

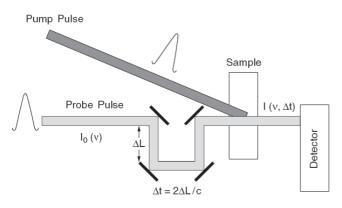


Fig. 8.1. Typical scheme of a "pump-probe" experiment

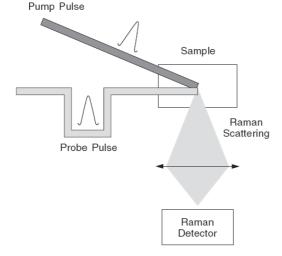
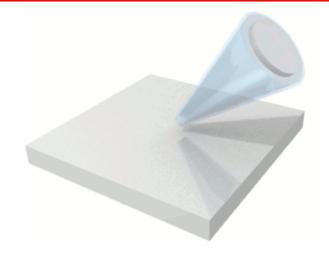
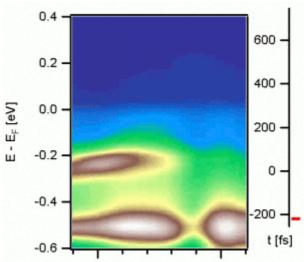


Fig. 8.12. Experimental setup for time-resolved Raman spectroscopy t [18]

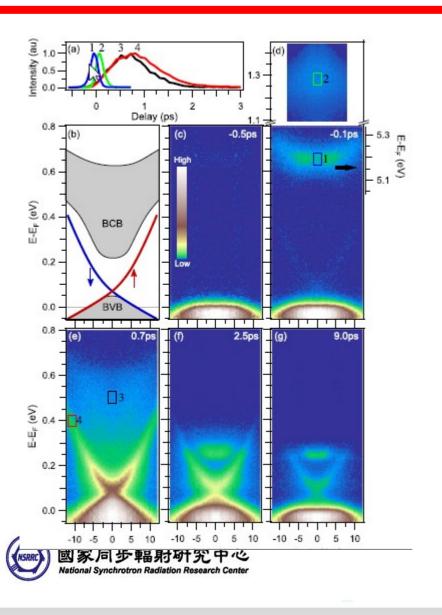


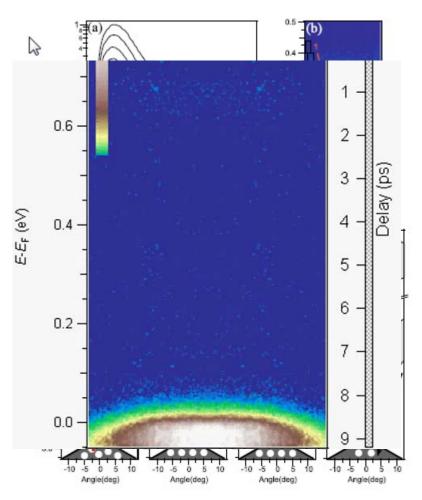




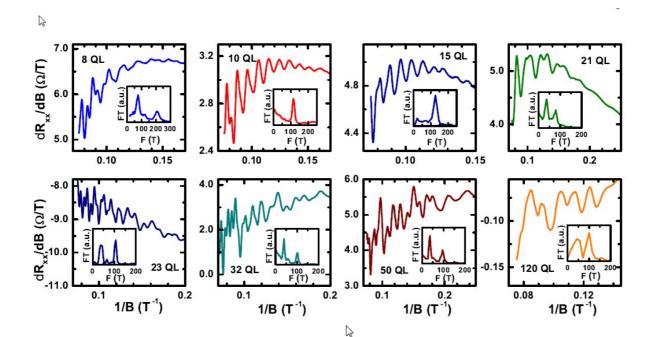
E-E_F [eV]

Ultrafast Dynamics of Dirac Fermion in Topological Insulators

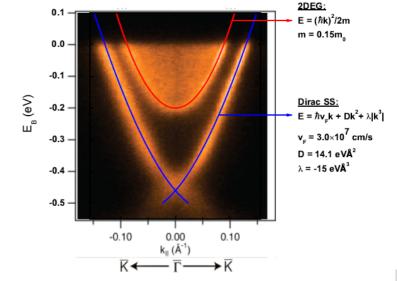




Estimate the surface charge carrier density : SdH oscillations ($n_s = \frac{k_F^2}{4\pi}$)

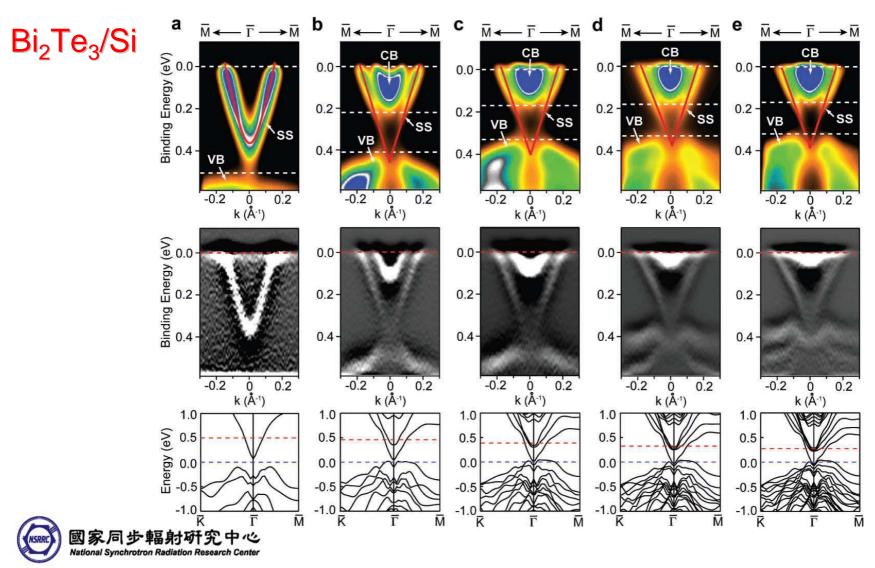


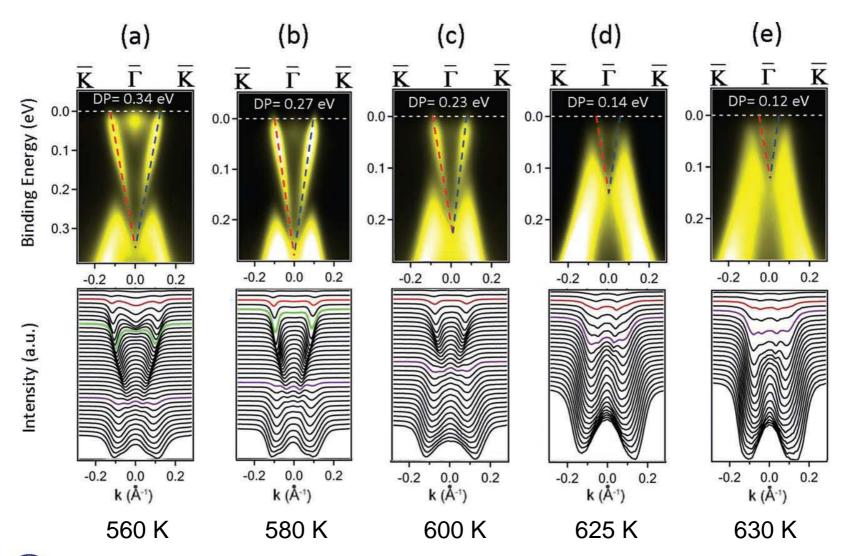
Estimate the surface charge carrier density : ARPES





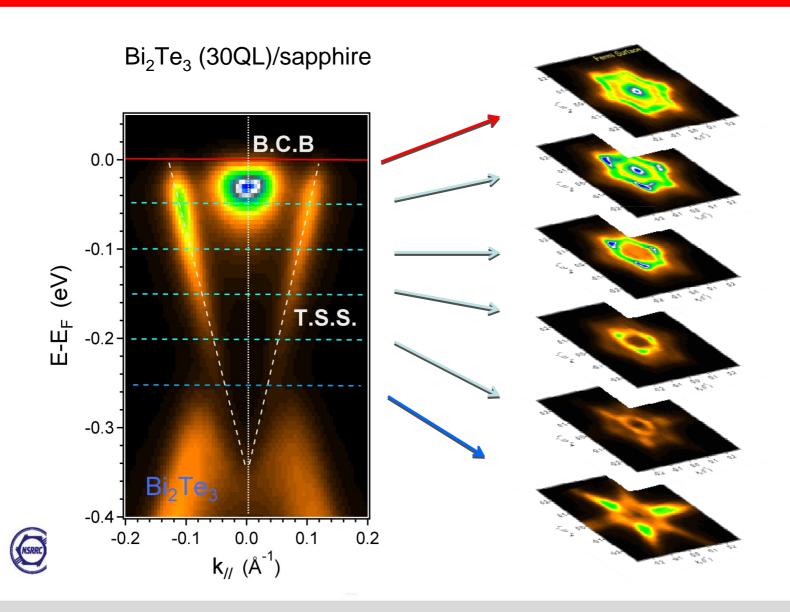
MBE growth topological insulators (Bi₂Te₃)

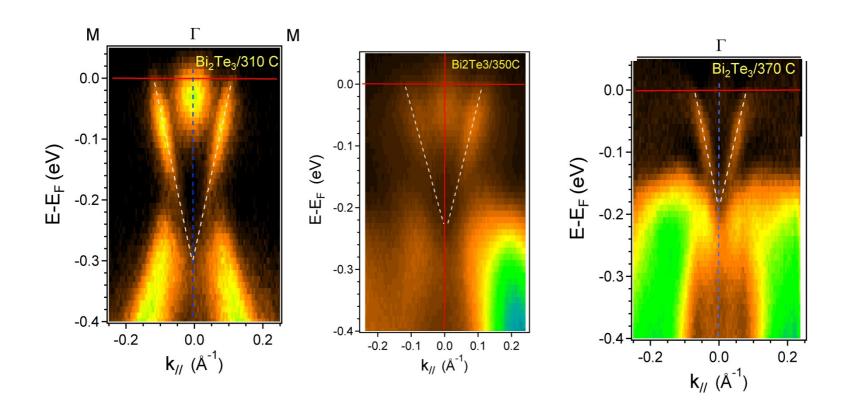






Bi₂Te₃ /Sapphire





Controlling substrate temperature and Bi/Te flux ratio can vary the doping condition arbitrary



Topics for TIs

New ternary Tis: Bi₂Te₂Se, TlBiSe₂, GeBi₂Se₄, SmB₆....

Impurity doping : Cu, Mn, Cr....

 Heterostructure TIs for devices : spintronic devices, thermoelectric devices



Collaborators

Graphene

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TIs

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