



**PHYS543000**

# **Principle and Application of Quantum Technology**

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# Course Information

**Lecture room: Phys Dept 019**

**Time: 2:20PM – 5:10PM**

**Homework and course outline:**

<http://w3.phys.nthu.edu.tw/~mou/teach.html>

**Feb. 27, March 20 no class (due to conference)**

**March 13, April 24 speaker lecture**

**•TA:**

**Shih-Si Hsiao (蕭世熙)**

**email: tousiotousio@gmail.com**



## •Grading scheme:

- Homework (4, 60%) and final report (40%)

### Textbooks

1. Introduction to Quantum Technologies, Alto Osada, Rekishu Yamazaki, and Atsushi Noguchi, Springer 2022.
2. eBook: Understanding Quantum Technologies 2021, 4th edition, Oliviar Ezratty

<https://www.oezratty.net/wordpress/2021/understanding-quantum-technologies-2021/>

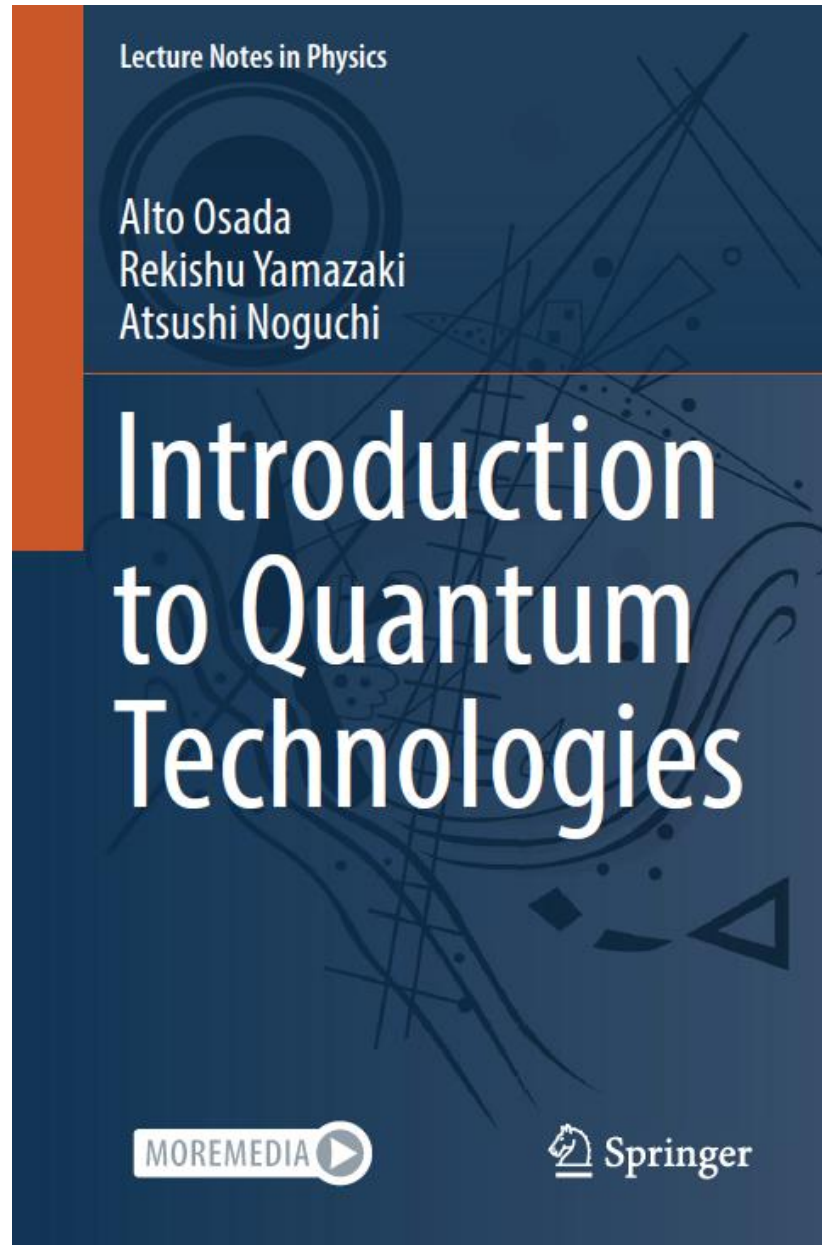
### References:

Quantum Computation and Quantum Information, Michael Nielsen and Isaac Chuang, Cambridge University press, 2000.

## Topics for final report:

1. Status report of quantum computation to break RSA (including methods using method of quantum simulation such as the preprint arXiv 2212.12372)
2. Quantum radar and quantum illumination
3. Status report of most recent quantum error corrections code
4. Status report on photonic quantum computer
5. Status report on Si-based quantum computer
6. Status report on trap-ion based quantum computer
7. Status report on Satellite-based quantum communication and quantum network

More accurate syllabus: following



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# Overview of Quantum Technology

Two important technologies  
that are being developed  
started from the beginning of  
the 21th century



## 100 years of quantum is just the beginning...

On June 7, 2024, the United Nations proclaimed 2025 as the International Year of Quantum Science and Technology (IYQ). According to the proclamation, this year-long, worldwide initiative will "be observed through activities at all levels aimed at increasing public awareness of the importance of quantum science and applications."

The year 2025 was chosen for this International Year as it recognizes 100 years since the initial development of quantum mechanics. [Join us](#) in engaging with quantum science and technology education and celebration throughout 2025!

# It takes times for a technology to be fully developed...

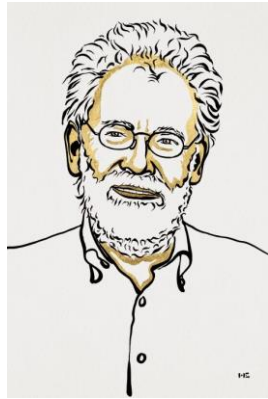
## The Nobel Prize in Physics 2022



III. Niklas Elmehed ©  
Nobel Prize  
Outreach  
**Alain Aspect**  
Prize share: 1/3



III. Niklas Elmehed ©  
Nobel Prize  
Outreach  
**John F. Clauser**  
Prize share: 1/3



III. Niklas Elmehed ©  
Nobel Prize  
Outreach  
**Anton Zeilinger**  
Prize share: 1/3

The Nobel Prize in Physics 2022 was awarded jointly to Alain Aspect, John F. Clauser and Anton Zeilinger "for experiments with entangled photons, establishing the violation of Bell inequalities and pioneering quantum information science"

量子糾纏發展年表：

\*1935年

愛因斯坦(Einstein)、波多爾斯基(Podolsky)、羅森(Rosen)共同發表一篇論文，提出了量子糾纏之思想實驗，來反駁哥本哈根學派所詮釋的“偶然論”。這著名的EPR思想實驗(EPR Paradox)主張量子力學裡面應仍有“隱藏變數”，來維護古典的“必然論”，並聲稱量子力學尚未完備。

\*1964年

貝爾(John Bell, 1928~1990)為了證實EPR所主張的“必然論”，設計了一個思想實驗，表明糾纏粒子的狀態如果有隱藏變數，則應遵守所謂的“貝爾不等式”(Bell Inequality)。然而以當時的技術很難做出此實驗。

貝爾不等式被認為是當代最具深邃的理論物理上的見解。

\*1972年

美國的克勞澤(John Clauser, 1942~)改進了貝爾定理，並提出了產生糾纏光子的方法（紫外線照射鈣原子），然後在1972年首次做出實驗。該實驗結果是貝爾不等式並不成立。當時克勞澤所做的實驗被認為仍有許多漏洞，所以貝爾不等式成立與否尚未能定音於一錘。

\*1982年

之後的十年間法國的阿思佩克特(Alain Aspect, 1947~)不斷改進克勞澤的實驗，例如改用雷射激發鈣原子來產生更有效率的糾纏光子對，也改善了偵測的精準度，並也設計出更為古怪的“量子延遲實驗”。這一連串的實驗結果都大幅偏離貝爾不等式。

然而這些實驗裡還有一個瑕疵是設備中的亂數產生器被認為非真正隨機；這讓糾纏光子對仍有機會暗通款曲。

\*2010s

奧地利的蔡林格(Anton Zeilinger, 1945~)利用遙遠星系所發出了訊號作為控制訊號，讓糾纏實驗的進行真正處於隨機狀態。蔡林格早在1997做出了單光子量子態傳送(Quantum Teleport)，也奠定了量子計算、量子通訊的基礎。

\*2022

瑞典皇家科學院稱，2022年諾貝爾物理獎表彰了法國的阿思佩克特、美國的克勞澤和奧地利的蔡林格等三人「展示了對『糾纏狀態』的粒子進行考察和控制的潛力」。

<https://doi.org/10.1038/s41746-024-01345-9>

# Artificial Intelligence awarded two Nobel Prizes for innovations that will shape the future of medicine

Ben Li & Stephen Gilbert



Check for updates

John J. Hopfield and Geoffrey E. Hinton were awarded the 2024 Nobel Prize in Physics for developing machine learning technology using artificial neural networks. In Chemistry it was awarded to Demis Hassabis and John M. Jumper for developing an AI algorithm that solved the 50-year protein structure prediction challenge. This highlights AI's impact on science, medicine and society; however, the winners acknowledge ethical aspects of AI that must be considered.

In October 2024, the Nobel Committees in Stockholm announced that the prizes in Physics and Chemistry were awarded to work related to artificial intelligence (AI)<sup>1,2</sup>. The prize in Physics was awarded to John J. Hopfield and Geoffrey E. Hinton (formerly of Google) for “foundational discoveries and inventions that enable machine learning with artificial neural networks<sup>1</sup>.” The prize in Chemistry was awarded one-half to David Baker for “computational protein design” and one-half to Demis Hassabis and John M. Jumper (of DeepMind) for “protein structure prediction<sup>2</sup>.” The historic announcement of these Nobel Prizes for AI-related work has been widely

aggregation with other ML methods and architectures brought us to the ML technologies of today, including the overlapping concepts and implementations of deep learning, convolution neural networks, transformer and attention-based architectures (advanced neural networks that excel at, for example, natural language processing), large language models and large multimodal models<sup>11</sup>. This is an evolving landscape of multipurpose foundation technologies, that some have compared to the printing press or the Internet in terms of reach and impact<sup>12</sup>. As an example of this, and maybe as a portent of what is to come, the ML of the 2024 Nobel Prize in Physics even enabled the groundbreaking discovery associated with the 2024 Nobel Prize in Chemistry<sup>2</sup>.

## 2024 Nobel Prize in Chemistry

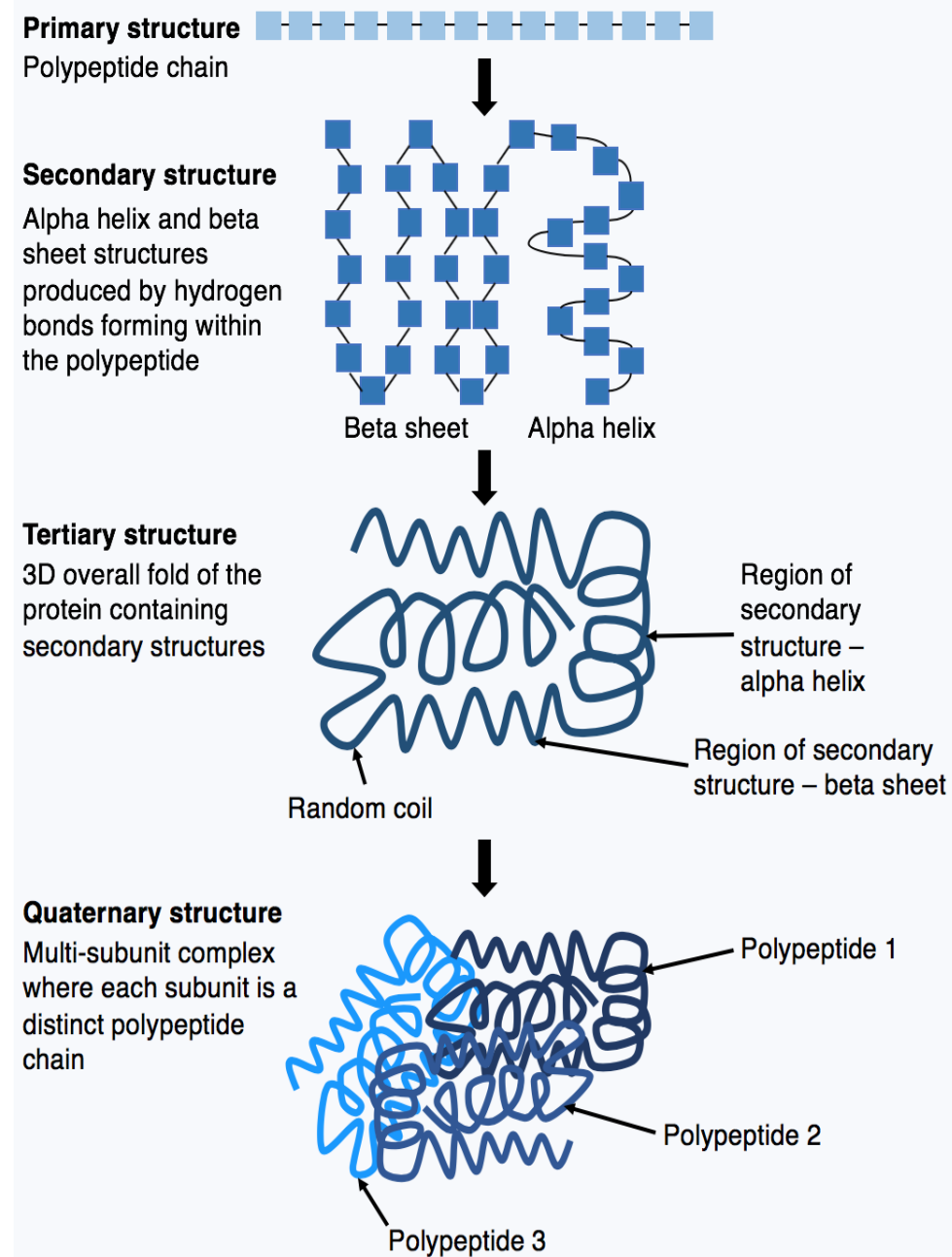
Hassabis and Jumper developed an AI model that accurately predicts protein structures from their amino acid sequences, which is one of the most intriguing and famous scientific challenges of the last 50 years<sup>2</sup>. As every biology student learns in school, a gene codes simply for the amino acid sequence, (with a few exceptions), and based on the environment of the cell, this sequence folds and assembles into a definitive and complex three-dimensional structure that dictates its function<sup>13</sup>. The 3D protein (again, with a few exceptions) is always the same, and thus, it should be possible to predict its structure just from the gene sequence, and perhaps knowledge of the cell environment<sup>13</sup>. Over 200 million amino acid sequences have been identified, yet less than 1% of their corresponding three-dimensional pro-



AlphaFold is an artificial intelligence (AI) program developed by DeepMind, a subsidiary of Alphabet, which performs predictions of protein structure. It is designed using deep learning techniques.

AlphaFold has two versions: AlphaFold 1 (2018) and AlphaFold 2 (2020).

AlphaFold 1 (2018) was placed first in the overall rankings of the 13th Critical Assessment of Structure Prediction (CASP) in December 2018. It was particularly successful at predicting the most accurate structures for targets rated as most difficult by the competition organizers.



It is foreseeable that  
successful combination of  
quantum technology and  
artificial intelligence will be  
the next milestone!

# Recent Breakthrough of Quantum Technology

量子電腦 [qubit, 量子位元]

HARDWARE > NEWS 之前: 幾個量子位元

## IBM Inches Closer To Quantum Supremacy With 16- And 17-Qubit Quantum Computers

by Lucian Armasu May 17, 2017 at 9:00 AM



## IBM Raises the Bar with a 50-Qubit Quantum Computer

by Will Knight November 10, 2017

## CES 2018: Intel's 49-Qubit Chip Shoots for Quantum Supremacy

By Jeremy Hsu (/author/jeremy-hsu)  
Posted 9 Jan 2018 | 0:00 GMT

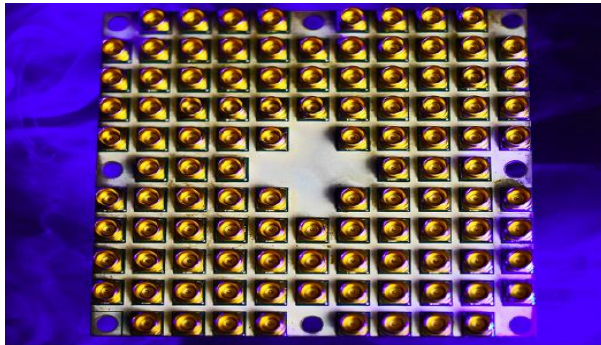


Photo: Intel  
Intel's new 49-qubit superconducting quantum test chip is named Tangle Lake.

Intel Roadmap: 1000 qubits 5-7 years

## ScienceNews

MAGAZINE OF THE SOCIETY FOR SCIENCE & THE PUBLIC

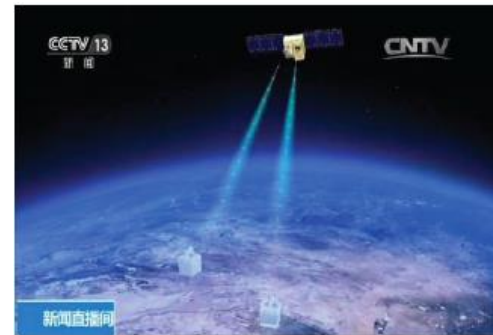
Google moves toward quantum supremacy with 72-qubit computer

Google contends its Bristlecone chip demoes 1% error rates for readout, 0.1% for single-qubit gates, and 0.6% for two-qubit gates.



(中央社台北18日電) 2017/06/18 13:52

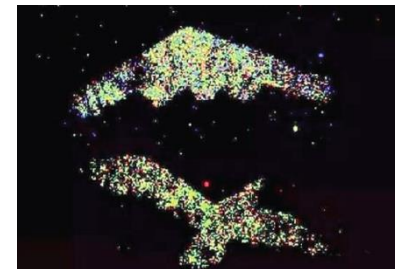
陸首顆量子衛星墨子號 可全球秘密通訊



光子: 飛行量子位元

2017年09月07日 07:51 中時電子報

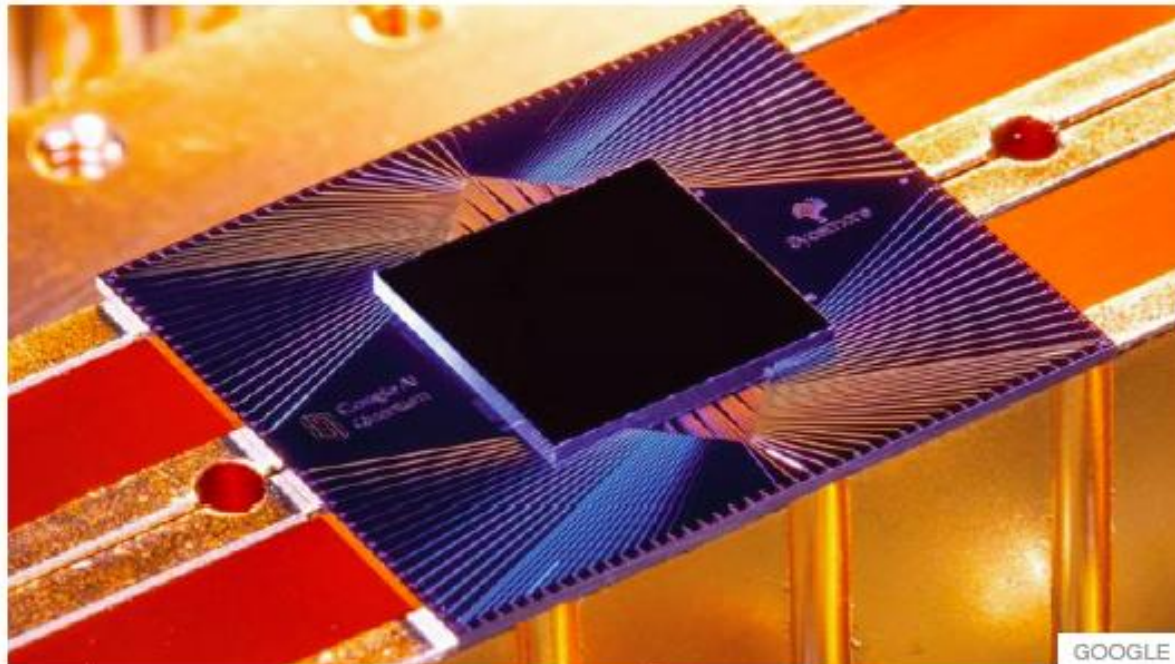
陸量子雷達再突破 F35隱形戰機藏不住



# Google claims 'quantum supremacy' for computer

By Paul Rincon  
Science editor, BBC News website

23 October 2019



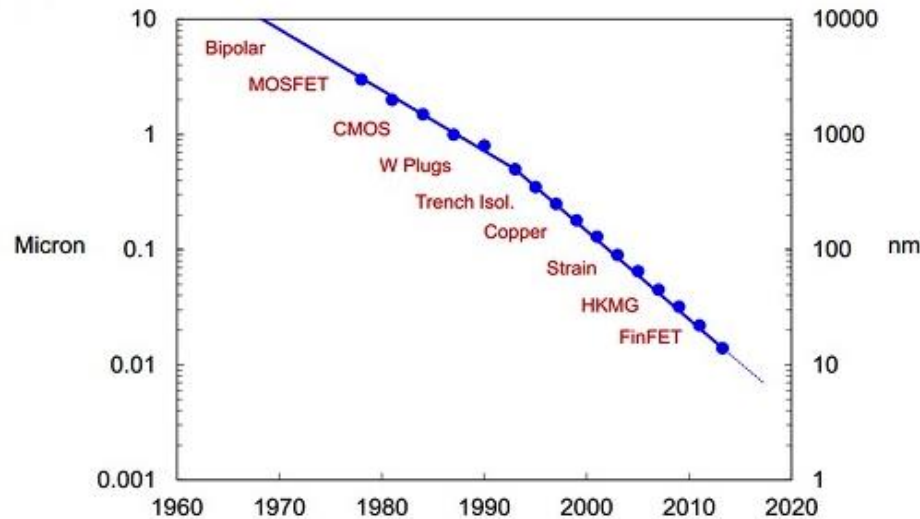
The technology giant's Sycamore quantum processor was able to perform a specific task in 200 seconds that would take the world's best supercomputer 10,000 years to complete.

# Early development

- 1982 R. P. Feynman proposed the idea of a 'quantum computer', a computer that uses the effects of quantum mechanics
- 1984 BB84 Quantum key distribution
- 1994 Shor's algorithm (fast prime factorization)
- 1995 Quantum error correction (Shor and Steane)
- 1996 Grover's searching algorithm
- ...

# Promoted by Nano-technology

Moore's Law Challenges Below 10nm: Technology, Design and Economic



Find post-semiconducting technology platform → 量子資訊 (quantum information science) (~2000)

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[Quantum Information Science](#) - [ [翻譯此頁](#) ]

Quantum Information Science (QIS) is an emerging field with the potential to cause revolutionary advances in fields of science and engineering involving ...

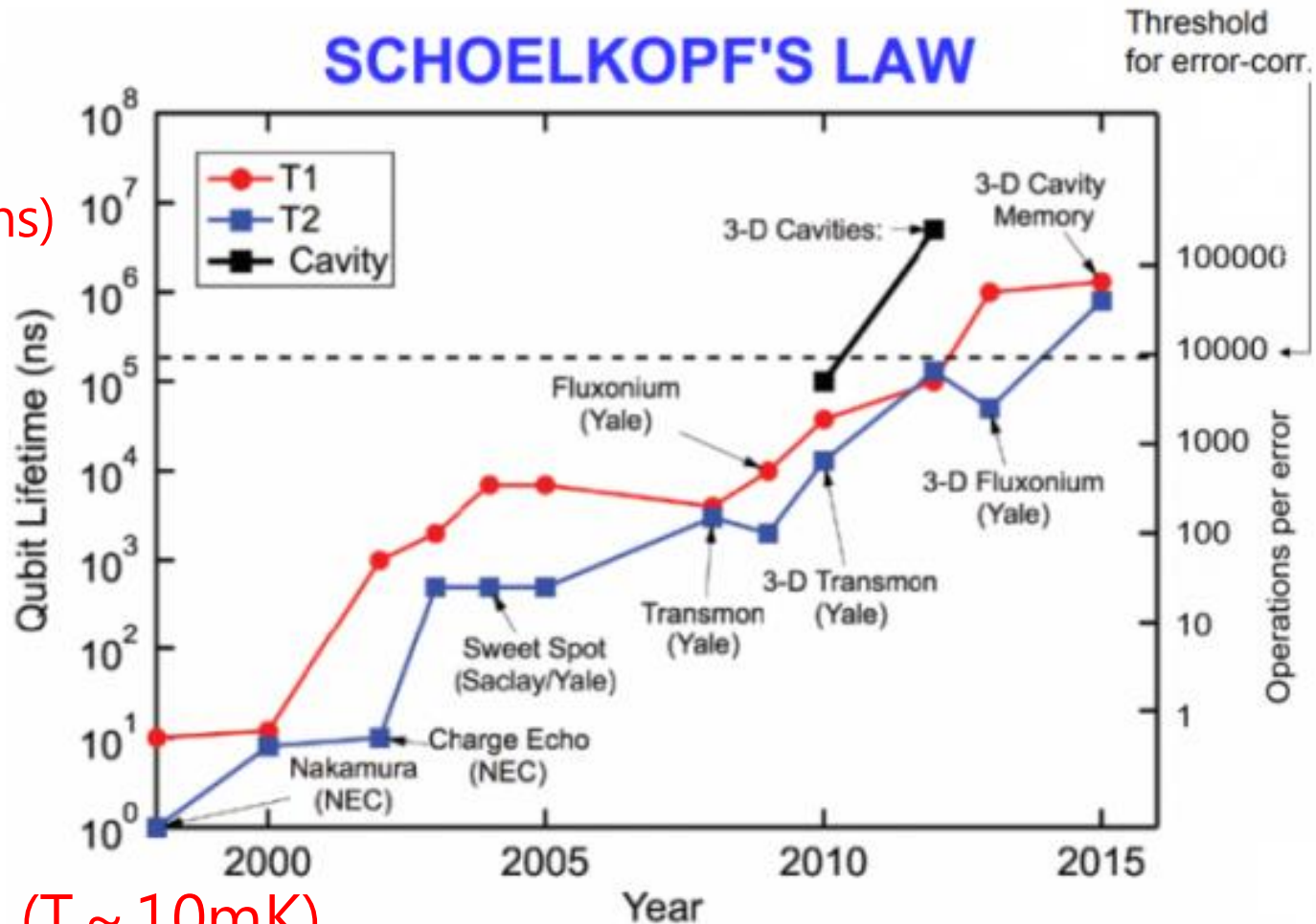
[www.nsf.gov/pubs/2000/nsf00101/nsf00101.htm](http://www.nsf.gov/pubs/2000/nsf00101/nsf00101.htm) - 120k - 頁庫存檔 - 類似網頁



# Breakthrough in Superconducting Qubit (2015)

## SCHOELKOPF'S LAW

存活時間(ns)



30-140  $\mu\text{s}$  ( $T \sim 10\text{mK}$ )

Devoret & Schoelkopf, Science 339, 1169 (2013)

$10^5$  improvement:

Ignite the technology community's hope for quantum technology!



# Developing Critical Point of Quantum Technology

Quantum Technology: Technology that directly utilizes the properties of quantum wave functions for information processing and calculation. The realization of quantum computers can be used to solve problems that are difficult for traditional computers. Absolutely secure communication networks, research and development of new drugs, design of new materials, and new forms of artificial intelligence may bring about revolutionary changes.

Berkeley Lab Supercomputer Breaks New Ground in  
Quantum Computing Simulation

[Michael Feldman](#) | April 12, 2017 11:26 CEST

Cori, the fifth fastest supercomputer in the world, has been used to model a 45-qubit circuit

Classical computers

50 qubit

Quantum supremacy



Qubit number

50 qubit

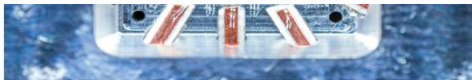


Second quantum revolution

# Facing the arrival of possible second quantum revolution

A number of projects are initiated such as Europe Quantum Manifesto, UK National Quantum Technologies Programme, Centre for Quantum Technologies in Singapore, USA DARPA call program ,...)

426 | NATURE | VOL 532 | 28 APRIL 2016



A €1-billion (US\$1.1-billion) European flagship project could advance the state of quantum computing.

## Billion-euro boost for quantum tech

### Microsoft just upped its multi-million bet on quantum computing

Microsoft pours millions into a new Station Q outpost in Copenhagen.

By [Liam Tung](#) | September 7, 2017 -- 13:38 GMT (21:38 GMT+08:00) | Topic: [Innovation](#)

### The DOE Is Giving Berkeley Lab \$3 Million Annually for Quantum Computing Research

PH Images/Getty Images (<http://www.gettyimages.ca/licenses/08492041>)

繼施堯耘之後，又一重量級量子計算學者入職阿里巴巴達摩院

作者 [雷鋒網](#) | 發布日期 2018 年 01 月 18 日 17:35 | 分類 [AI 人工智慧](#), [人力資源](#), [科技教育](#) [Follow](#) [G+](#) [讚 5](#) [分享](#)

2018年03月08日 10:17 [時報資訊](#) 綜合外電報導

新浪財經消息，百度今日宣布成立量子計算研究所，開展量子計算軟件和信息技術應用業務研究，百度計畫在五年內組建世界一流的量子計算研究所，並逐步將量子計算融入到業務中。

量子計算機在金融、醫藥、化學、材料、人工智能等領域具有廣闊的應用空間，有望應用於人工智能（如自動駕駛軟件）等領域。



The Quantum Manifesto calls upon Member States and the European Commission to launch a €1 billion Flagship-scale Initiative in Quantum Technology, preparing for a start in 2018 within the European H2020 research and innovation framework programme.

This initiative aims to place Europe at the forefront of the second quantum revolution now



UNSW  
SYDNEY

Newsroom

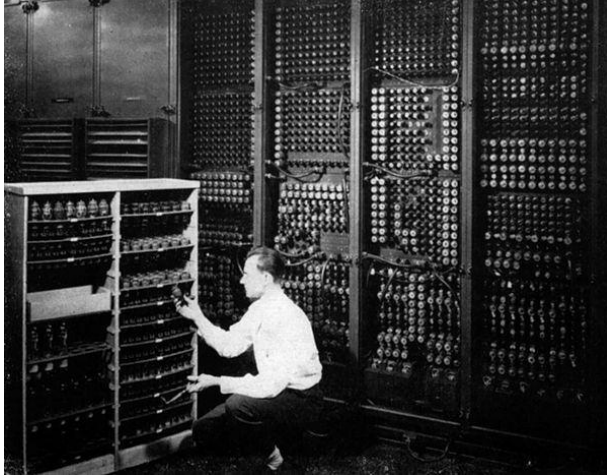
### Australia's first quantum computing company launches at UNSW

23 AUG 2017 | UNSW MEDIA

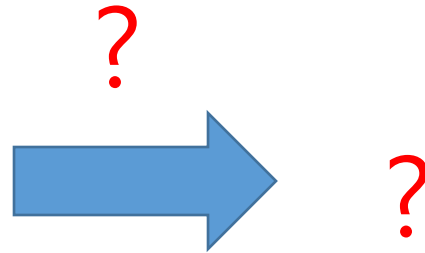
Australia's first quantum computing company, Silicon Quantum Computing Pty Ltd, has been launched to advance the development and commercialisation of UNSW Sydney's world-leading quantum computing technology.

# Promise of quantum technology ?

Eniac 1943



## Quantum Technology



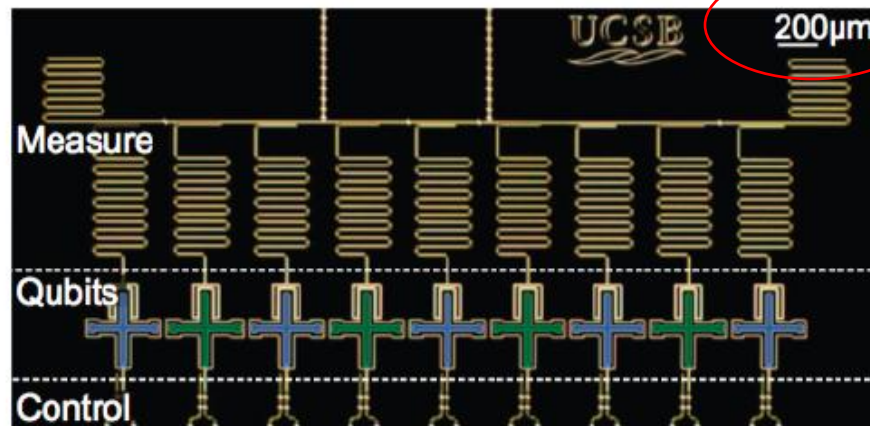
# Typical Misunderstanding

## 台積電3奈米赴美？關鍵在量子電腦

發稿時間：2017/03/20 14:40 最新更新：2017/03/20 15:18

（中央社記者鍾榮峰台北20日電）台積電傳出考量3奈米赴美設廠。工研院IEK主任室計畫副組長楊瑞臨指出，台積電3奈米選址非常關鍵，牽涉布局量子電腦1奈米以下的次奈米新技術和材料。

## UCSB/Google nine X-mon qubit processor



Need to understand What Quantum Mechanics can do?

# Quantum Technology

Quantum information Science

Applications and Programming:  
Quantum Algorithms, Programming, Protocols

量子裝置  
Quantum Device

量子電腦

Universal quantum  
computer

量子模擬器

Quantum simulator

量子退火機

Quantum annealer

量子感測器

Quantum sensor

量子通訊/網路

Quantum network

量子裝置  
Quantum Device

量子材料

Quantum Material

# Status and Challenge

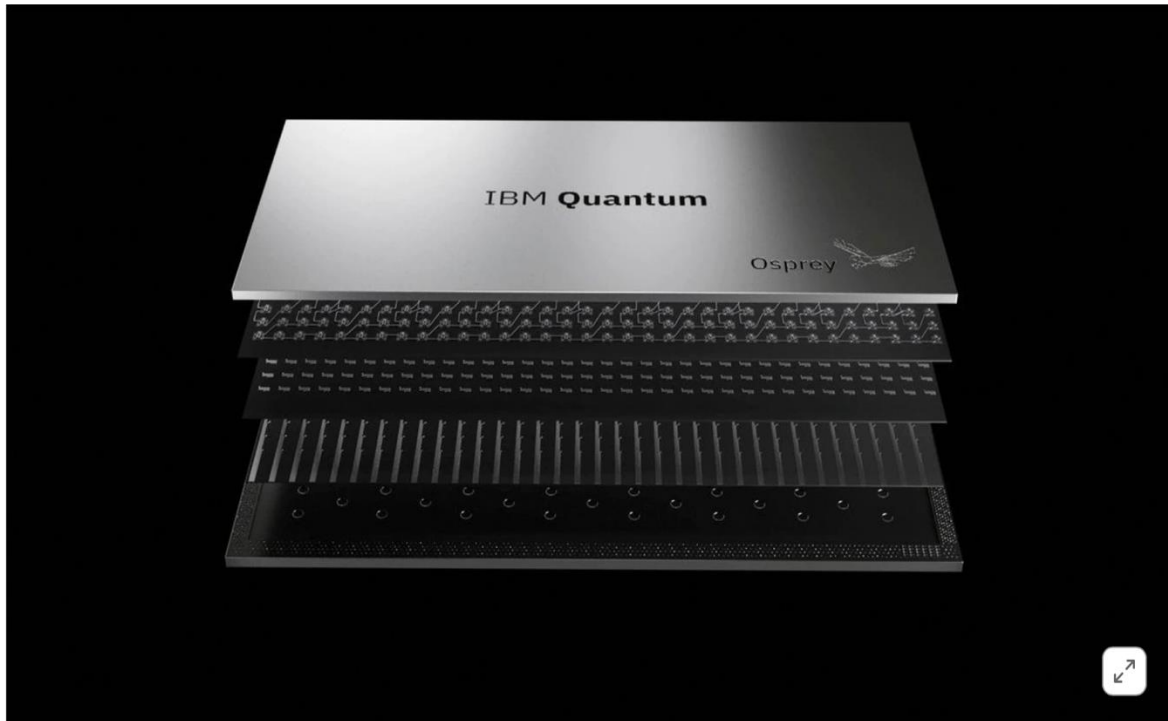
2 minute read · November 9, 2022 10:07 PM GMT+8 · Last Updated a day ago



# IBM launches its most powerful quantum computer with 433 qubits

2022

By Jane Lanhee Lee





## News in focus

algorithms that harness these indicators to estimate a person's 'biological age', which can be higher or lower than their chronological age<sup>3</sup>.

Another hallmark of ageing is a shift in the proteins that the body produces. To explore how organs age, Oh and his colleagues first analysed nearly 5,000 proteins in blood samples from 1,398 healthy adults. They identified about 850 proteins that originated mainly from a single organ and trained a machine-learning algorithm to predict a person's age on the basis of the levels of these proteins. They validated their model using blood samples from more than 4,000 other people.

The results showed that an organ's biological age is linked to disease risk. For example, roughly 2% of participants had accelerated heart ageing – that is, their levels of blood proteins relating to heart ageing differed substantially from those of other people of the same age. Having a prematurely old heart was linked to a 250% increased risk of heart failure, the authors found.

### Marking time

Researchers have used epigenetic markers to show that the pace of organ ageing varies between individuals<sup>4</sup>. But the link between epigenetic changes and ageing is unclear, says Matt Kaeberlein, a specialist in the biology of ageing and chief executive of Optispan, a biotechnology company in Seattle, Washington. Proteins are "much closer to the downstream mechanisms that might be driving ageing", he says.

Combining various hallmarks of ageing could lead to more-robust tests of organ age

# IBM RELEASES FIRST-EVER 1,000-QUBIT QUANTUM CHIP

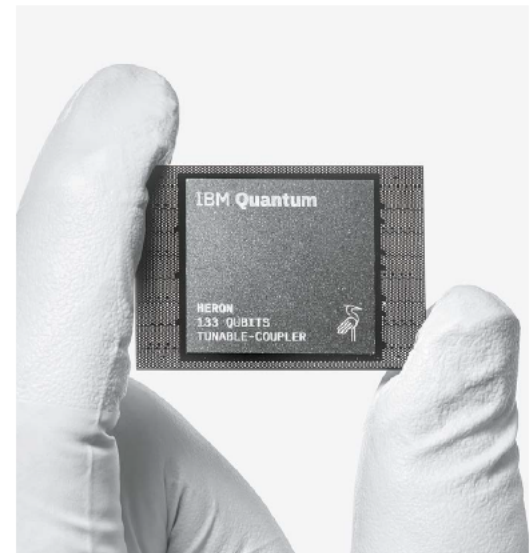
The company will now focus on developing smaller, more reliable processors.

By Davide Castelvecchi

**I**BM has unveiled the first quantum computer with more than 1,000 qubits – the equivalent of the digital bits in an ordinary computer. But the company says that it will now shift gears and focus on making its machines more error-resistant rather than larger.

For years, IBM has been following a quantum-computing road map that roughly doubled the number of qubits every year. The chip unveiled on 4 December, called Condor, has 1,121 superconducting qubits arranged in a honeycomb pattern. It follows on from IBM's other record-setting, bird-named machines, including a 127-qubit chip called Eagle, released in 2021 and a 433-qubit one called Osprey, announced last year.

Quantum computers promise to perform certain computations that are beyond the reach of classical computers. They will do so by exploiting uniquely quantum phenomena, such as entanglement and superposition, which allow multiple qubits to exist in multiple collective states at once.



RYAN LAVINE FOR IBM

IBM's Heron quantum processor.

2023). The company says that it will now focus on building chips designed to hold a few qLDPC-corrected qubits in just 400 or so physical qubits, and then networking those chips together.

The IBM preprint is "excellent theoretical work", says Mikhail Lukin, a physicist at

# 大陸第三代自主超導量子電腦「本源悟空」上線運行

12:57 2024/01/06 | 中時 | 李文輝



央視  
新聞



大陸第三代自主超導量子電腦「本源悟空」上線運行。（翻攝自大陸央視）



# Development assessment



?

## Status

Near-term applications that are beyond the capability of classical computers

50 -100 qubits

1000

1000-10,000

1000,000...

Noisy Intermediate quantum computing regime 、 quantum simulation 、 optimization

Intermediate scale & rate quantum communication

Probably 5-10 years

Universal Quantum computing

?



global quantum network

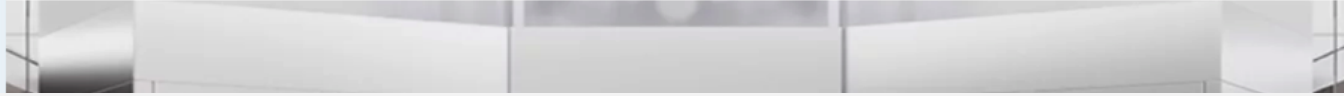
200km

1000km

# IBM Aims For 100,000-Qubit Machine By 2033, Pioneering 'Quantum-Centric Supercomputing'

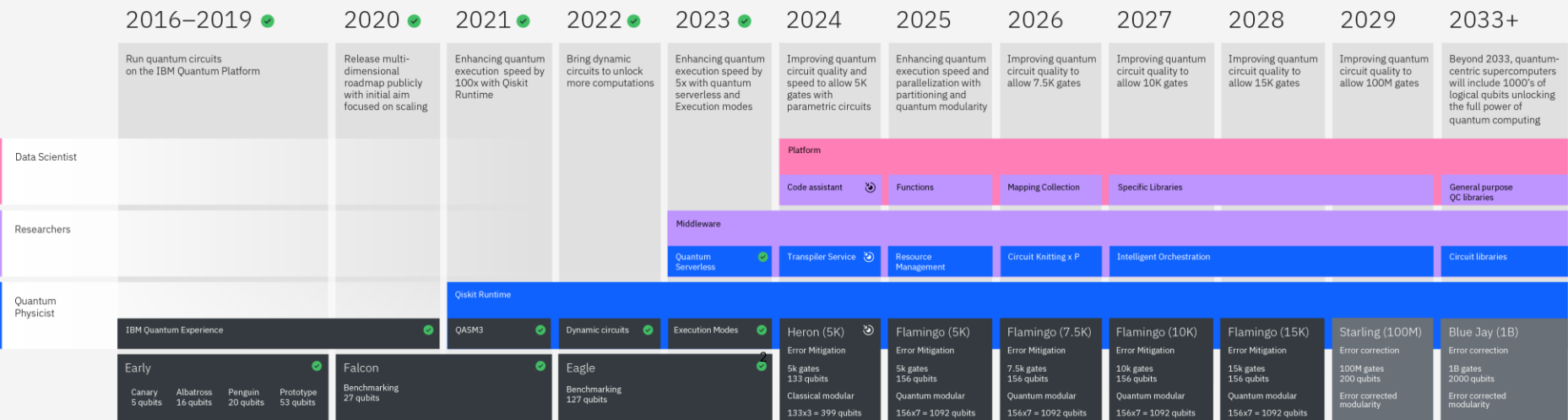
Quantum Computing Business

Matt Swayne • May 23, 2023

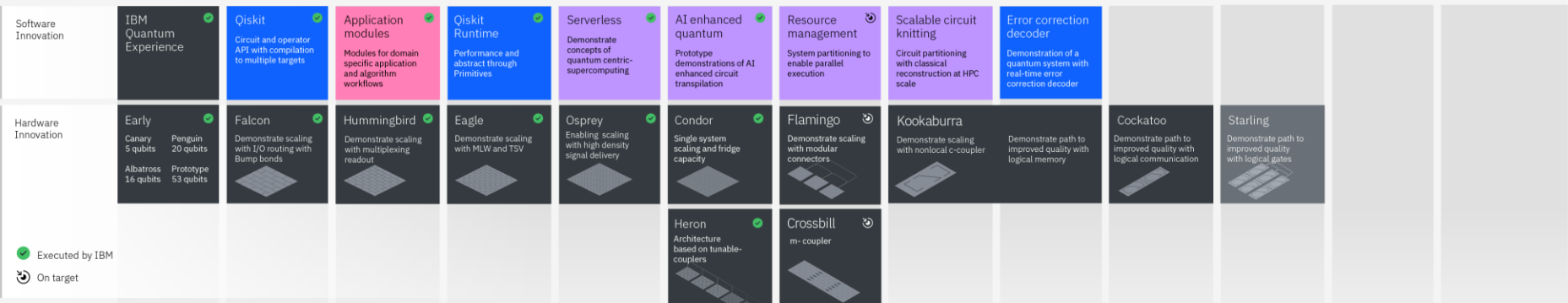


## Development Roadmap

IBM Quantum



## Innovation Roadmap



Executed by IBM

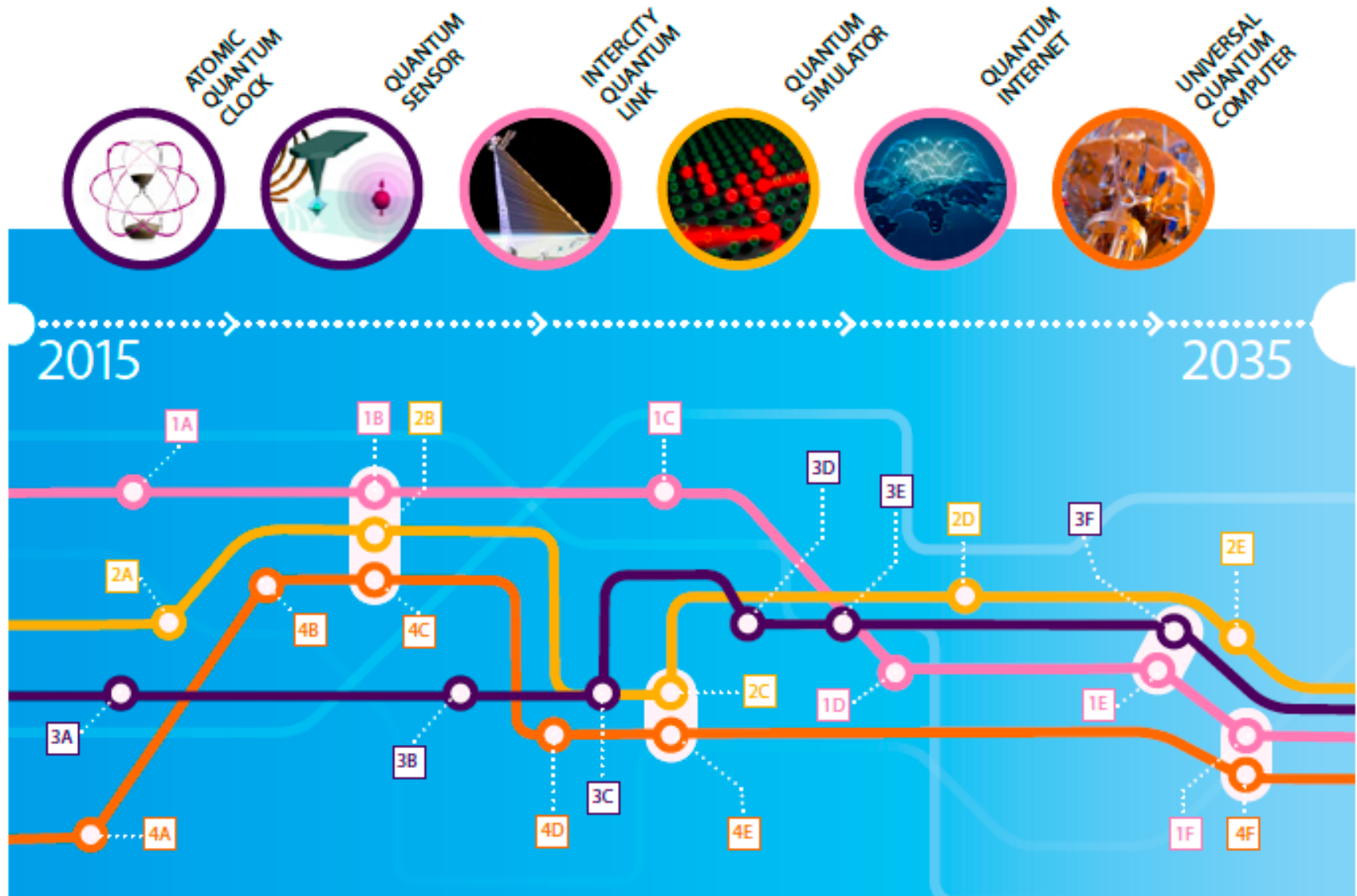


On target



# Quantum Manifesto (European union)

## Quantum Technologies Timeline



# Effort for establishing quantum network



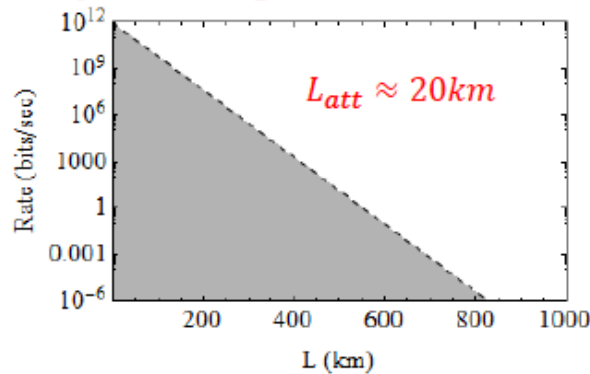
## DiVincenzo criteria

- A **scalable** physical system with well characterized qubits. ?
- The ability to **initialize** the state of the qubits to a simple fiducial state. ✓
- **Long** relevant **decoherence times** ( $>10^4$  operation time) ✓
- A **"universal"** set of quantum gates. ✓
- A **qubit-specific measurement** capability. ✓
- The ability to interconvert stationary and flying qubits.
- The ability to faithfully transmit flying qubits

# Challenge for quantum communication and n

## Decay in optical fibre

Major Challenge – Fiber Attenuation

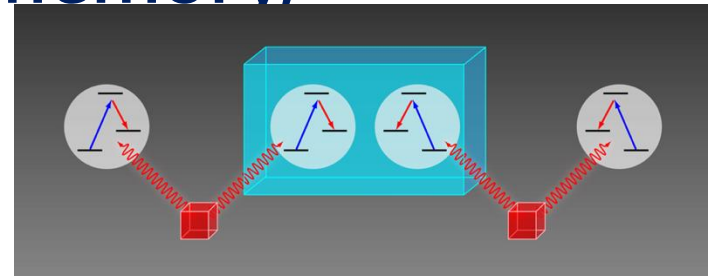


No clone theorem !

( 量子態無法複製 )

Need to develop quantum repeater (quantum repeater) to break through the 200km limit

Key technologies: quantum memory, quantum teleportation, entanglement swapping



Credit: Alan Stonebraker



photon: flying qubit, decay length  
200km

European scientists propose world's largest quantum  
network, between Earth and the ISS

April 9, 2013 at 8:50 am

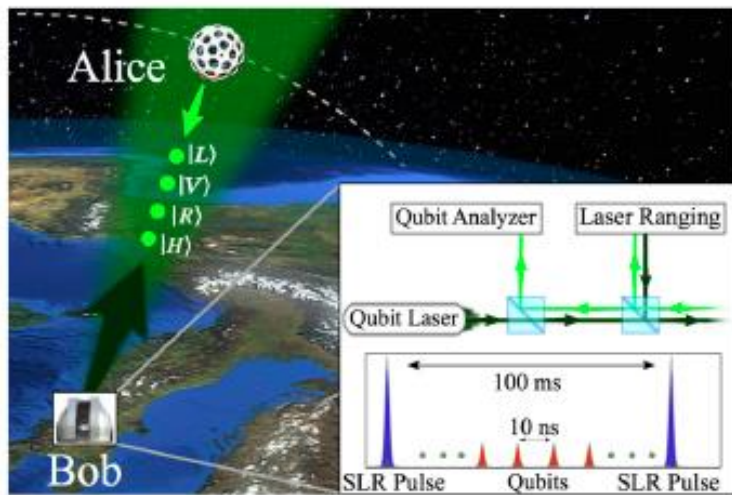


FIG. 1 (color online). Scheme of the satellite QKD demonstration. Qubit pulses are sent at a 100 MHz repetition rate and are reflected back to the single photon level from the satellite, thus mimicking a QKD source in space. Synchronization was performed by using the bright SLR pulses at a repetition rate of 10 Hz.

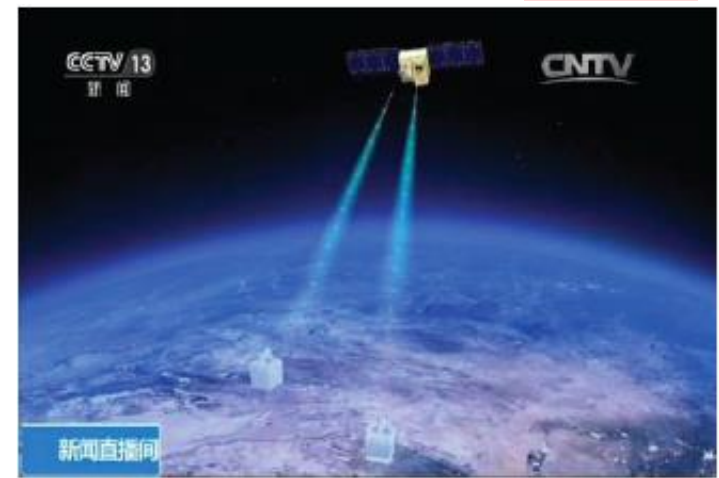
Phys. Rev. Lett. **115**, 040502 (2015)  
Italian group, qubit error ratio 4.6%

➡ satellite quantum  
communication

**The world's first  
quantum communication  
satellite (China), viable  
for 300s**

(中央社台北18日電) 2017/06/18 13:52

陸首顆量子衛星墨子號 可全球秘密通訊



Phys. Rev. Lett. **120**,  
030501( 2018)

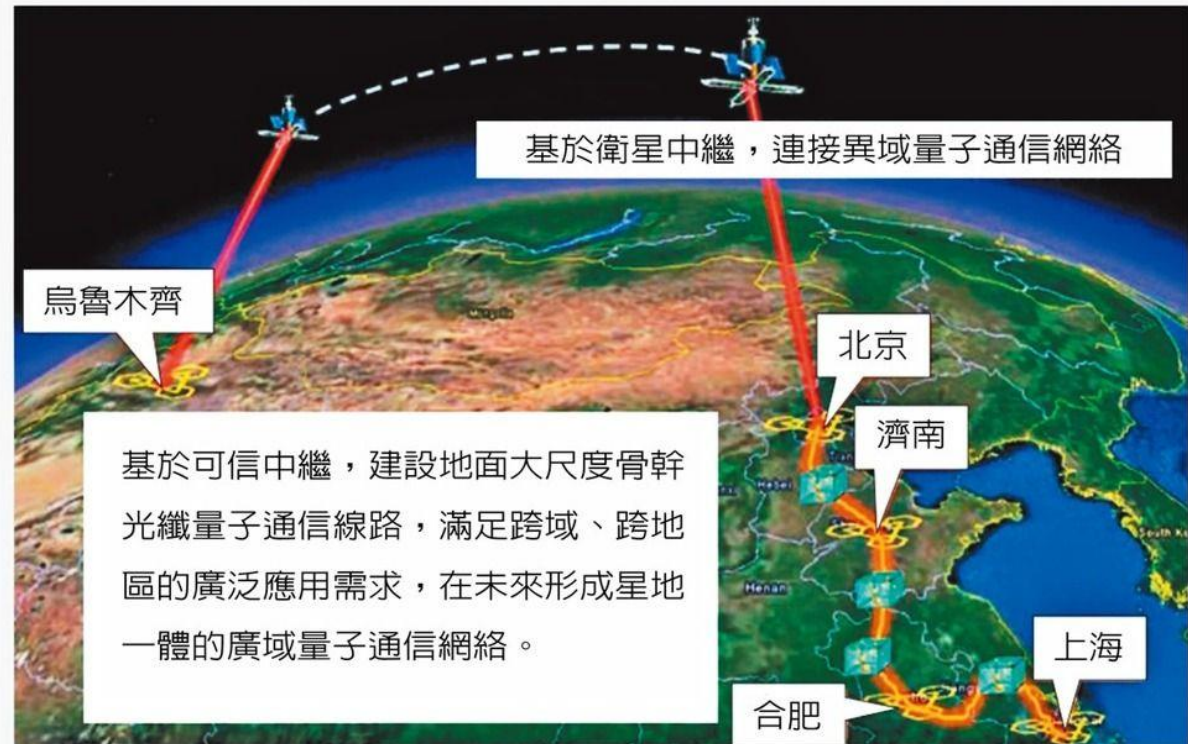
# 量子保密通信 京滬幹線開通

全長逾2000公里的量子保密通信骨幹網絡「京滬幹線」2017/09/29 開通，是世界首條量子保密通信幹線。中科院院長白春禮昨日到「京滬幹線」北京控制中心，用量子加密視頻會議系統與合肥、濟南、上海、新疆南山等地的科研人員對話，並通過「墨子號」量子衛星與奧地利地面站的衛星量子通信，與奧地利科學院院長塞林格(Anton Zeilinger)作了世界首次洲際量子保密視頻通話。交通銀行、工商銀行、阿里徵信已開始使用此幹線加密實時交易和數據傳輸。

量子通信是迄今唯一被嚴格證明無條件的安全通信方式，可以有效解決信息安全問題。「中國量子通信技術已經走在了世界前列，並持續保持著其優勢地位。我們的量子保密通信技術比國外領先了4-5年。」潘建偉說。

## 京滬幹線

示意圖





# The world's first commercial quantum communication network successfully tested in Jinan



世界首個大型商用量子通信專網於2017年7月在濟南完成第一階段黨政機關量子通信專網測試，與周邊數百平方公里的，近200個終端進行保密通信。它是目前世界上規模最大、功能最全的城域量子通信網路，業務可涵蓋政務、金融、政法、科研、教育等五大領域，能為用戶提供基於量子加密的電話、傳真、文件和文本通信業務。

Source: MOST\_量子科技研究與發展規劃案報告(管希聖)

# Recent developments of quantum communication network

UK

QKD network integrated with commercial communication

Austria

QKD network of 8 nodes demonstrated

China

2,000 km QKD network between Shanghai and Beijing is underway



USA

Installing QKD network

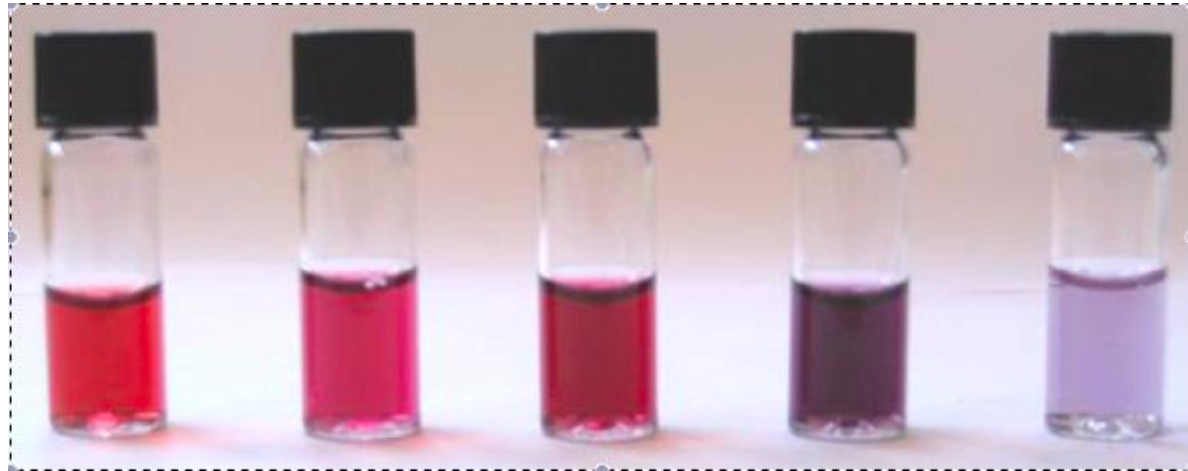
Japan

QKD network to transmit sensitive Genome data

- What is quantum technology? Quantum Computer? Quantum Phenomenon?

# Typical Quantum Phenomenon

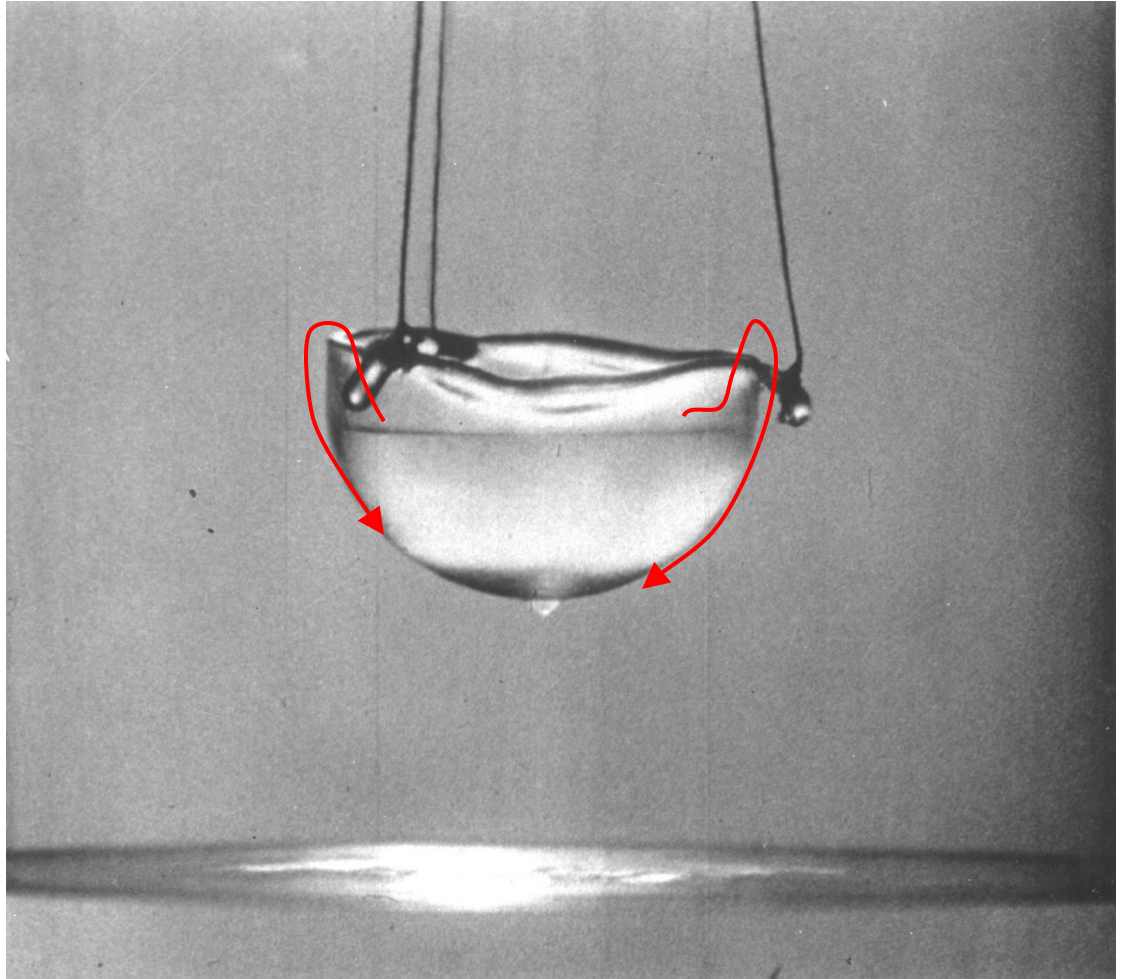
Gold is not  
shining





# Macroscopic quantum phenomena : usually require low T and coherence

## Creeping of liquid helium



<http://www.youtube.com/watch?v=2Z6UJbwx>

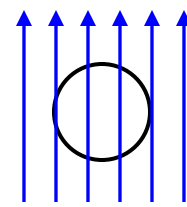
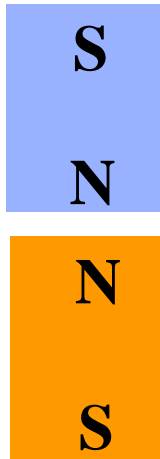
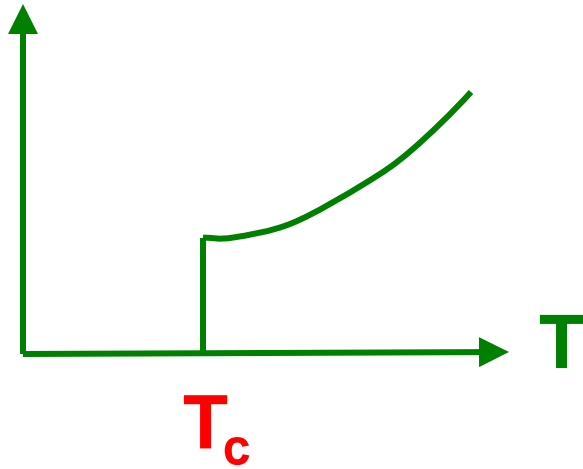


<https://youtu.be/2Z6UJbwxBZI>

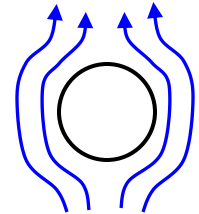


# Macroscopic quantum phenomenon: superconduct

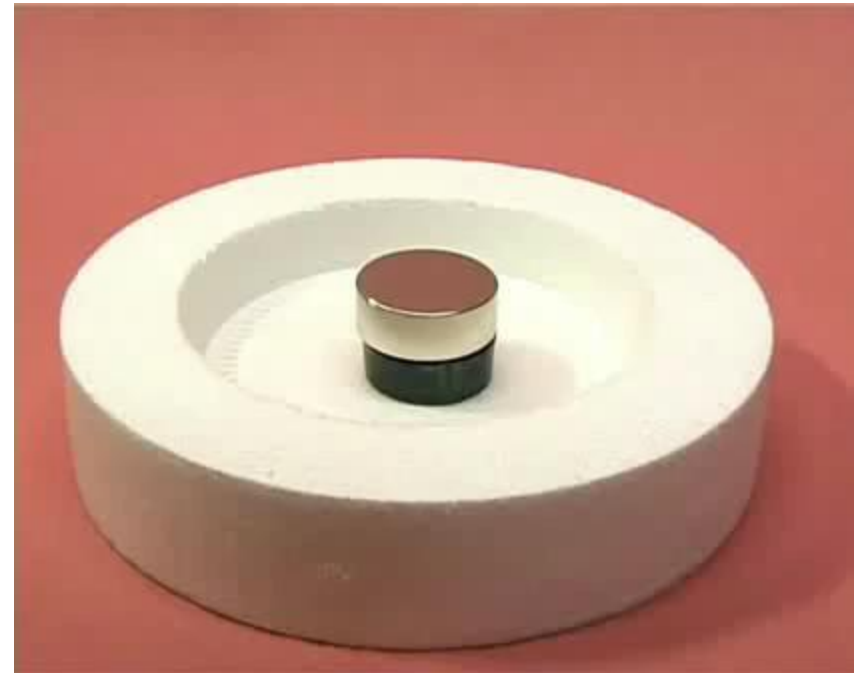
電阻



$T > T_c$

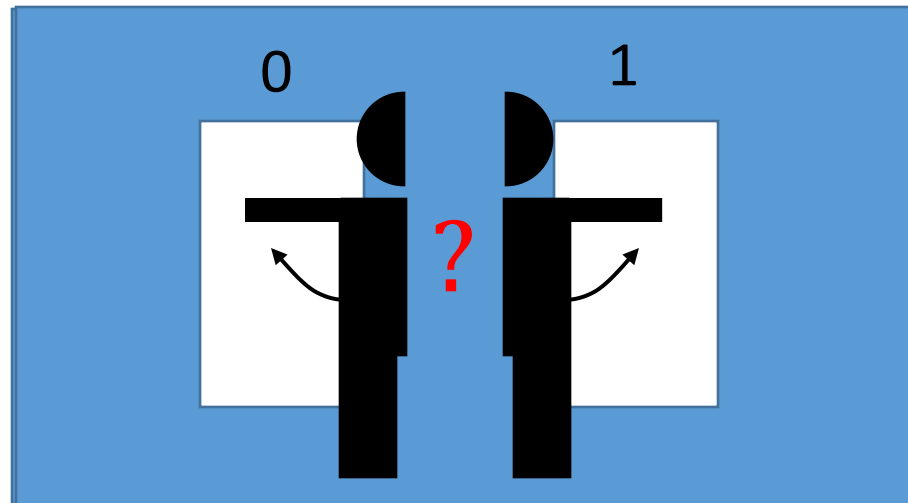


$T < T_c$



# Essential of Quantum Mechanics

A way to describe a particle that pass two doors (**qubit**) at the same time.



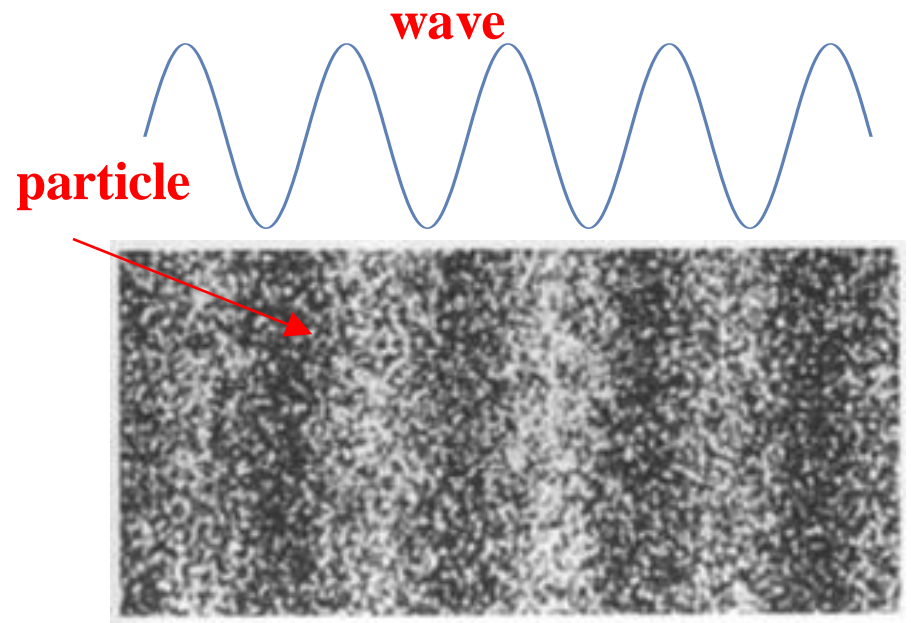
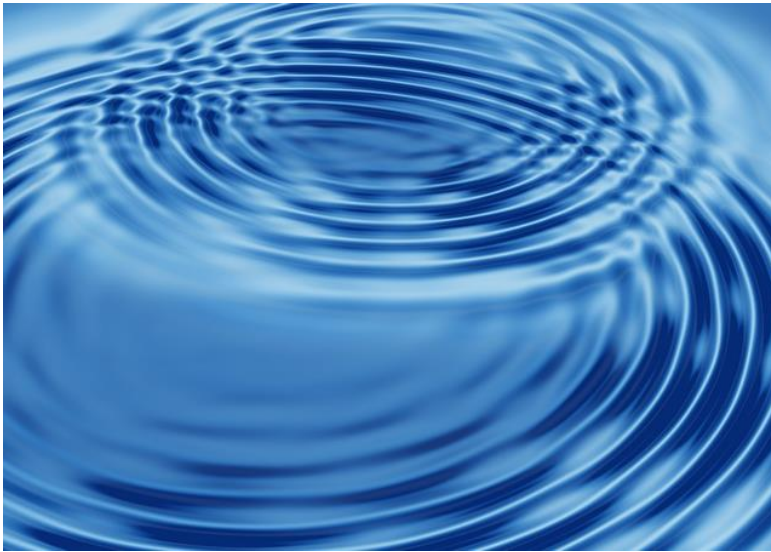


Richard Feynman  
(1965 Nobel Prize)

**I think that it is fair to say that no one understands the quantum theory...**

**Quantum Mechanics: wave and particle duality, matter needs to be described using both concept of particle and wave:**

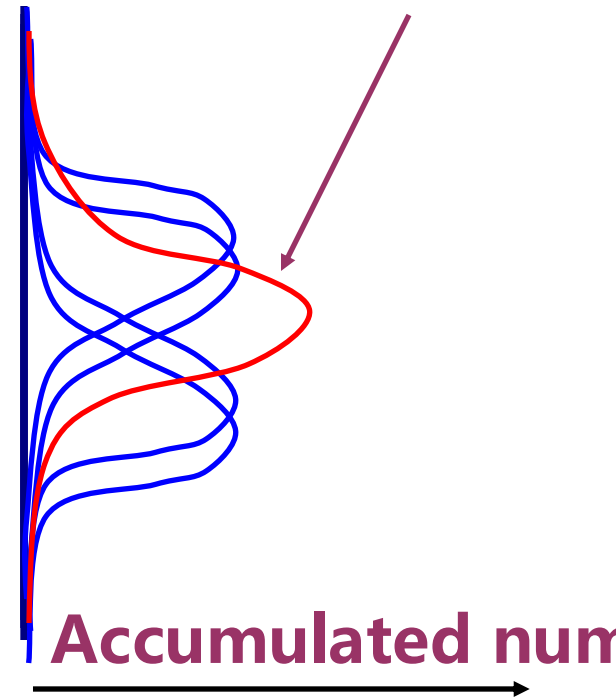
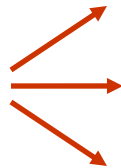
**Matter wave dictates where the particle goes to, but when it is measured, one piece of particle is found.**



# Let us examine the statement “passing two door at the same time”

Pass through one of doors (ad

Electron  
gun

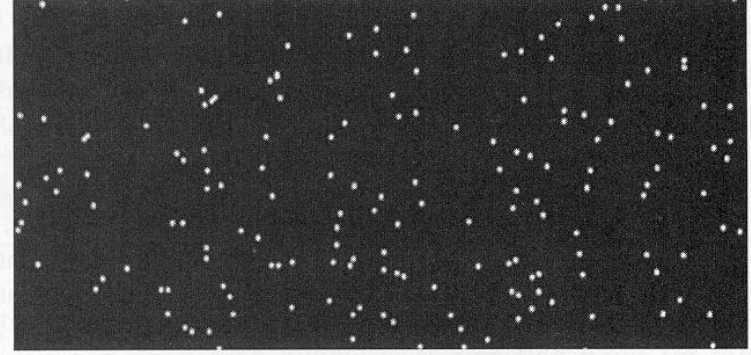
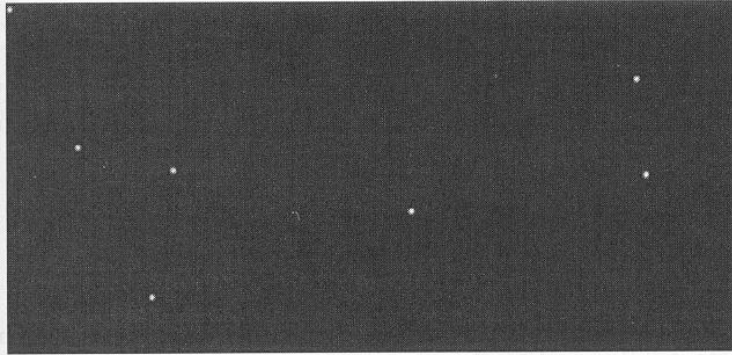


# **Shooting one electron each time** **(Tonomura et al, 1989)**

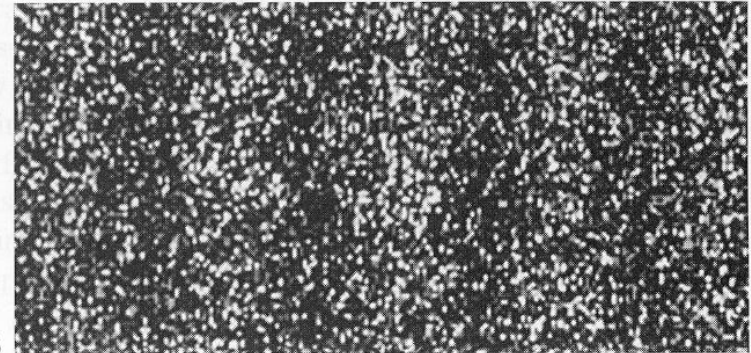
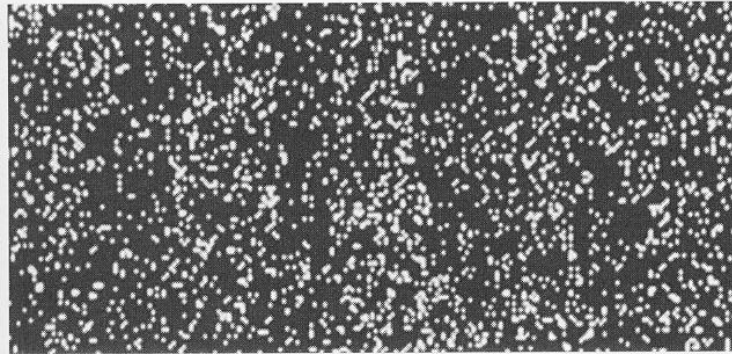




# Number of events $\longleftrightarrow$ probability



(b)



(d)

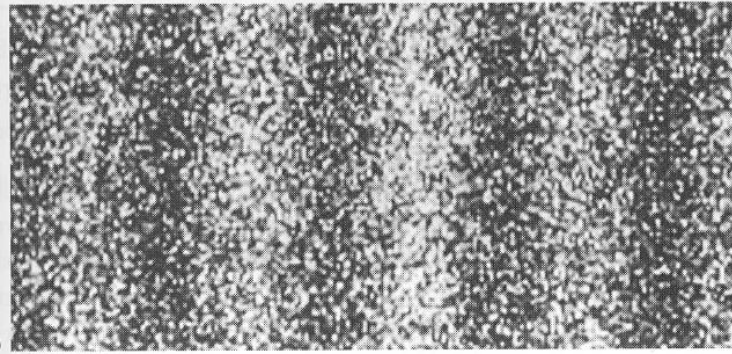
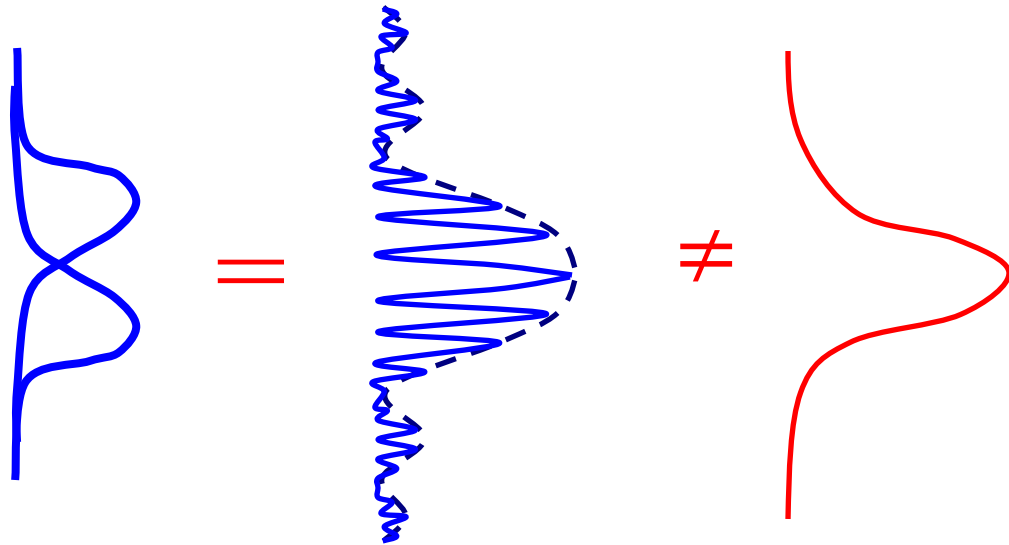
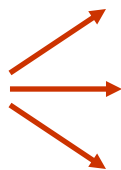


Fig. 39-8 Photographs showing the buildup of an interference pattern by a beam of electrons in a two-slit interference experiment like that of Fig. 39-6. Matter waves, like light waves, are *probability waves*. From top to bottom the approximate numbers of electrons involved are 7, 100, 3000, 20 000, and 70 000.

# A great puzzle



Electron  
gun



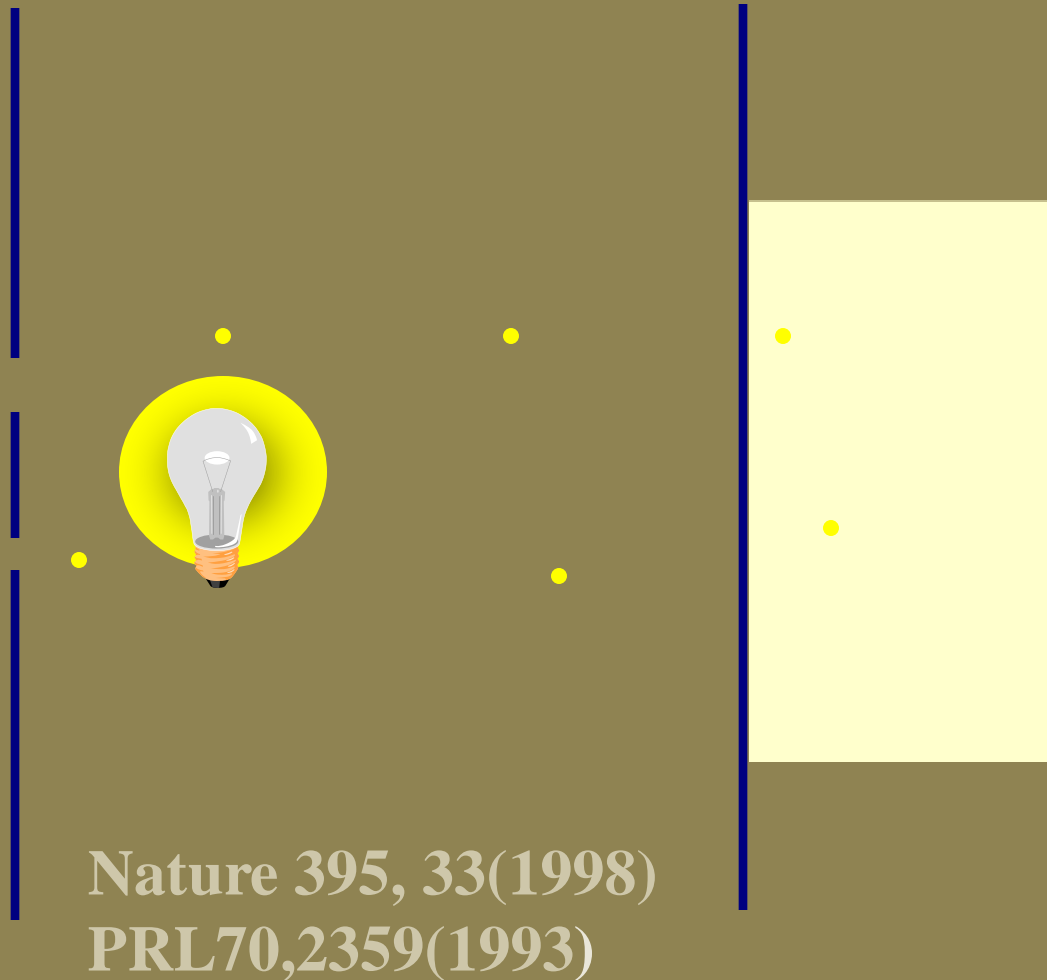
1

2

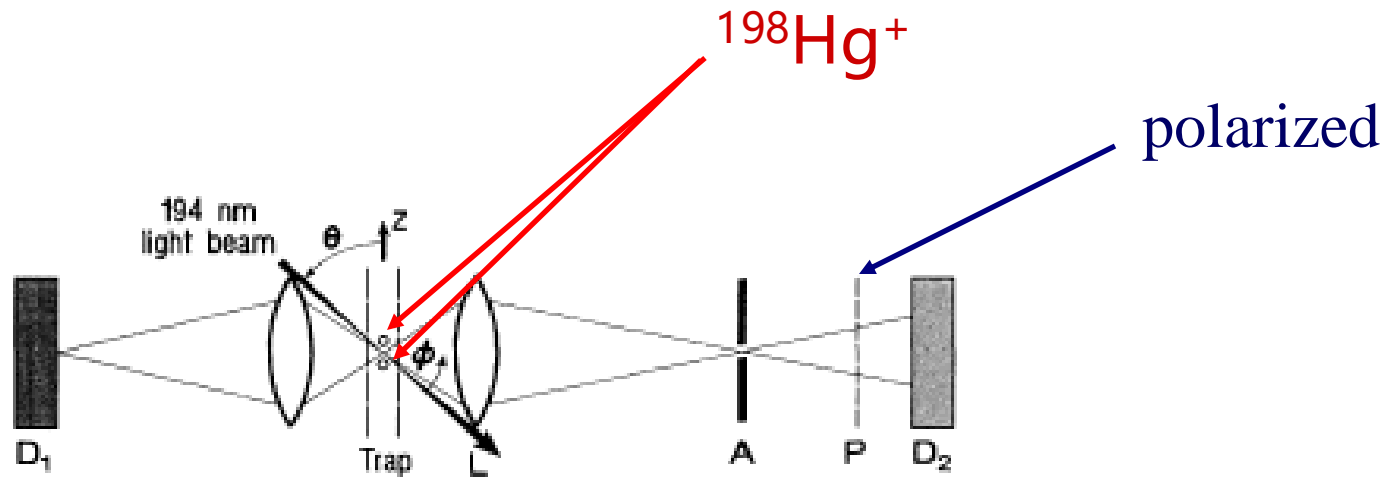
Electron is not passing 1 or 2,  
Instead it passes through 1 and 2  
at the same time.

# Which-way experiment

電  
子  
源



# Which way expt. by using photons



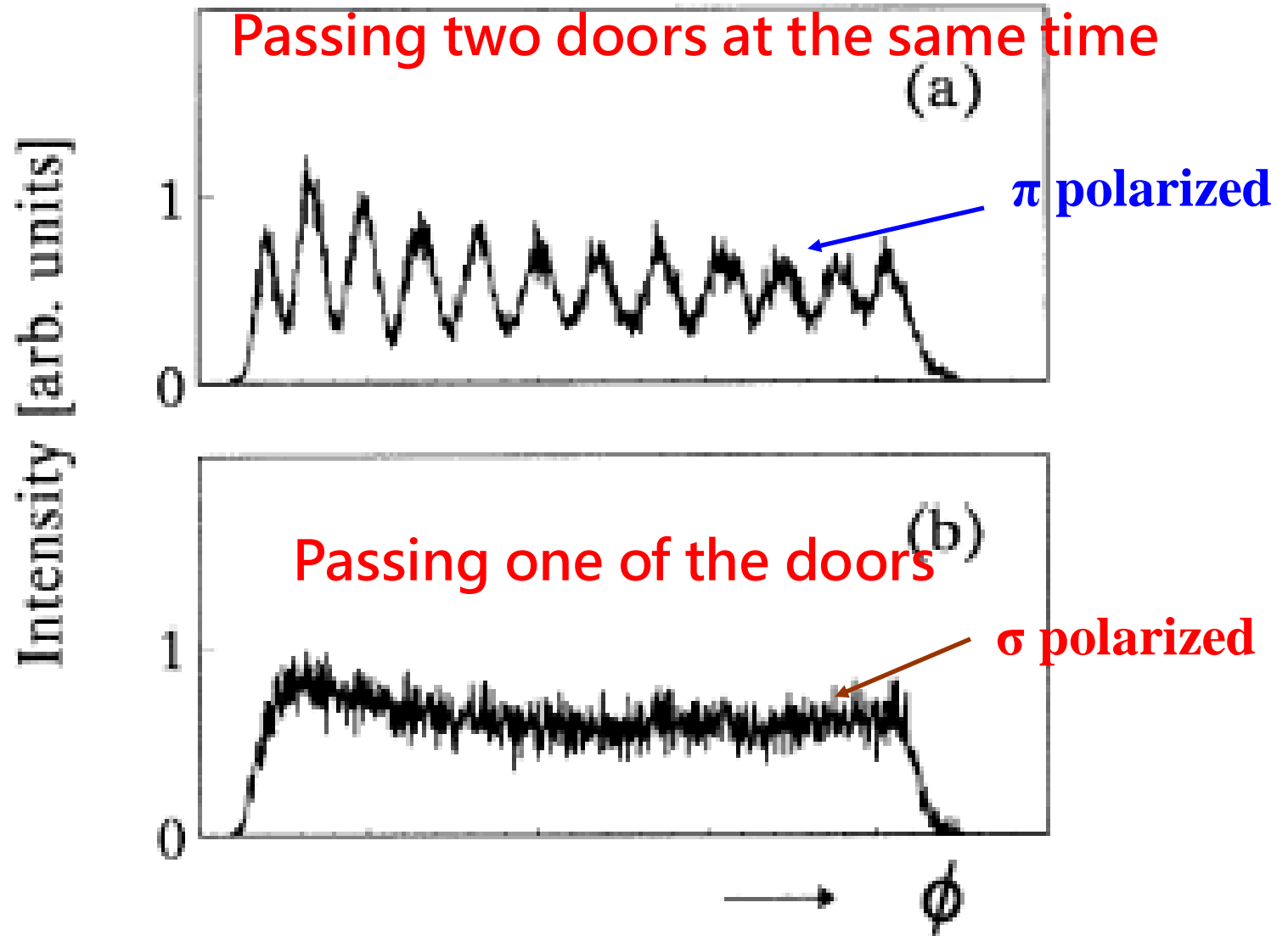
**Phys. Rev. Lett. 70,2359(1993)**

**Ground state:  $6s^2S_{1/2}$ , Excited state:  $6p^2P_{1/2}$   
degenerate:  $m_J$**

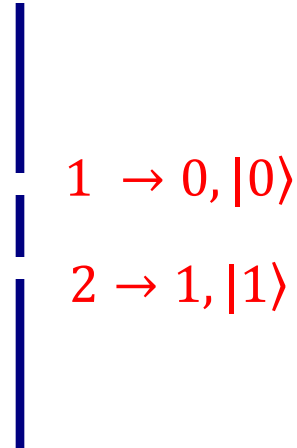
Photons:  $\sigma$  &  $\pi$  polarized

$\pi$ :  $\Delta m_J = 0$  two atoms are in the same state

$\sigma$ :  $\Delta |m_J| = 1$  two atoms are not in the same state



# Concept of quantum bit (qubit)



Class bit: 0 or 1

qubit: can be 0 and at the same time

When it is measured, only 0 or 1 is  
Obtained (collapse of state)



double slit  $\Rightarrow \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle)$   $\Leftrightarrow$  superposition  $\Psi = \Psi_1 + \Psi_2$

# Advantage of qubit

\* **0 and 1 can be input at once**

0 or 1 can only be input separately

Classical computer — 1 — 0 — 

Quantum computer —  $\alpha|0\rangle + \beta|1\rangle$  — 

\* **more manipulation space:**

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle = \cos\frac{\theta}{2}|1\rangle + e^{i\phi}\sin\frac{\theta}{2}|0\rangle$$

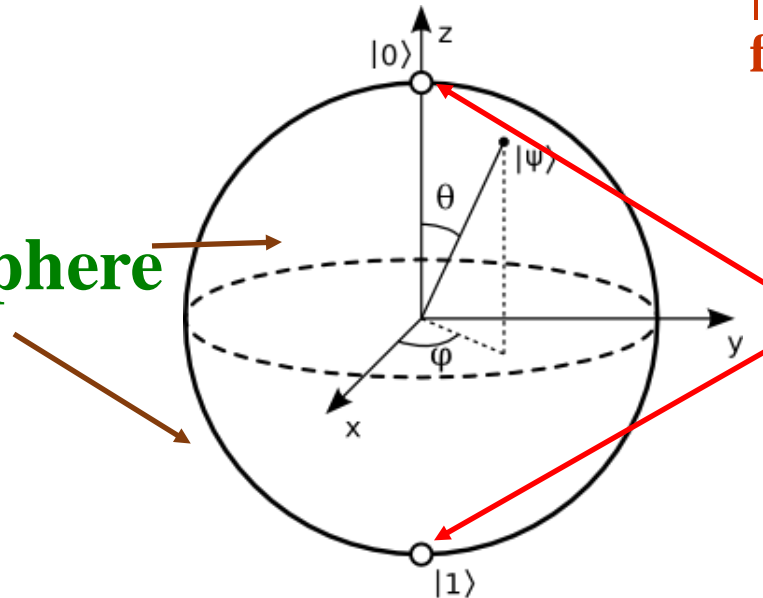
$|\alpha|^2$  is the probability for finding 0

$|\beta|^2$  is the probability for finding 1

$$|\alpha|^2 + |\beta|^2 = 1$$

**Quantum: whole sphere**

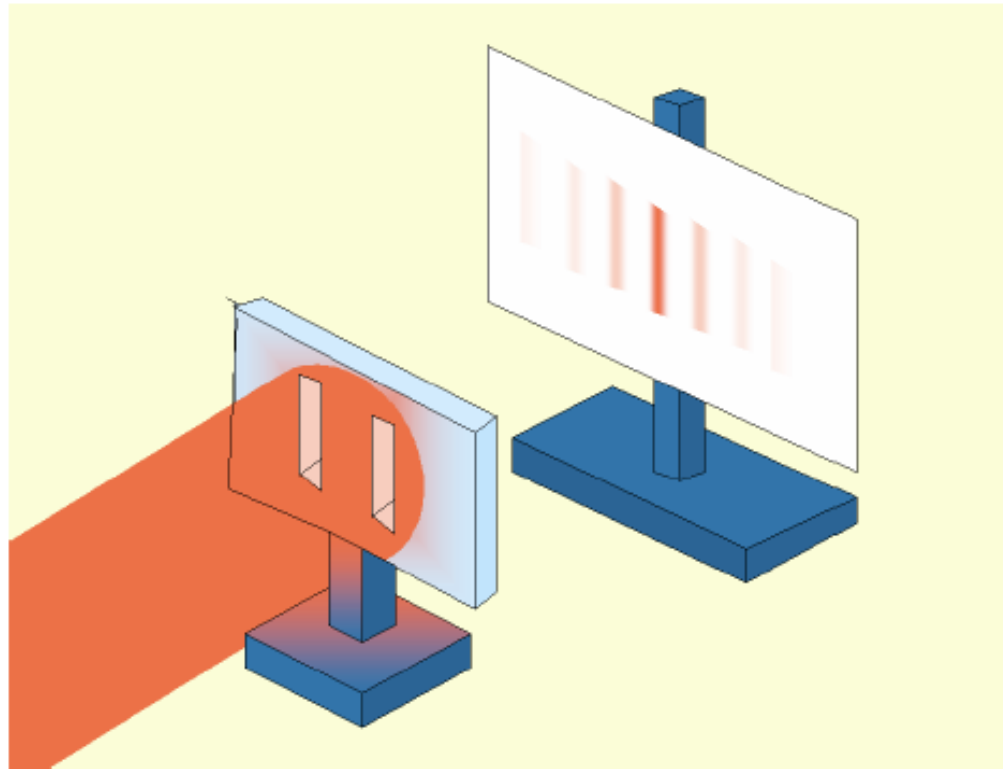
**classical: 2 points**





# Puzzles in Double-slit quantum eraser experiment

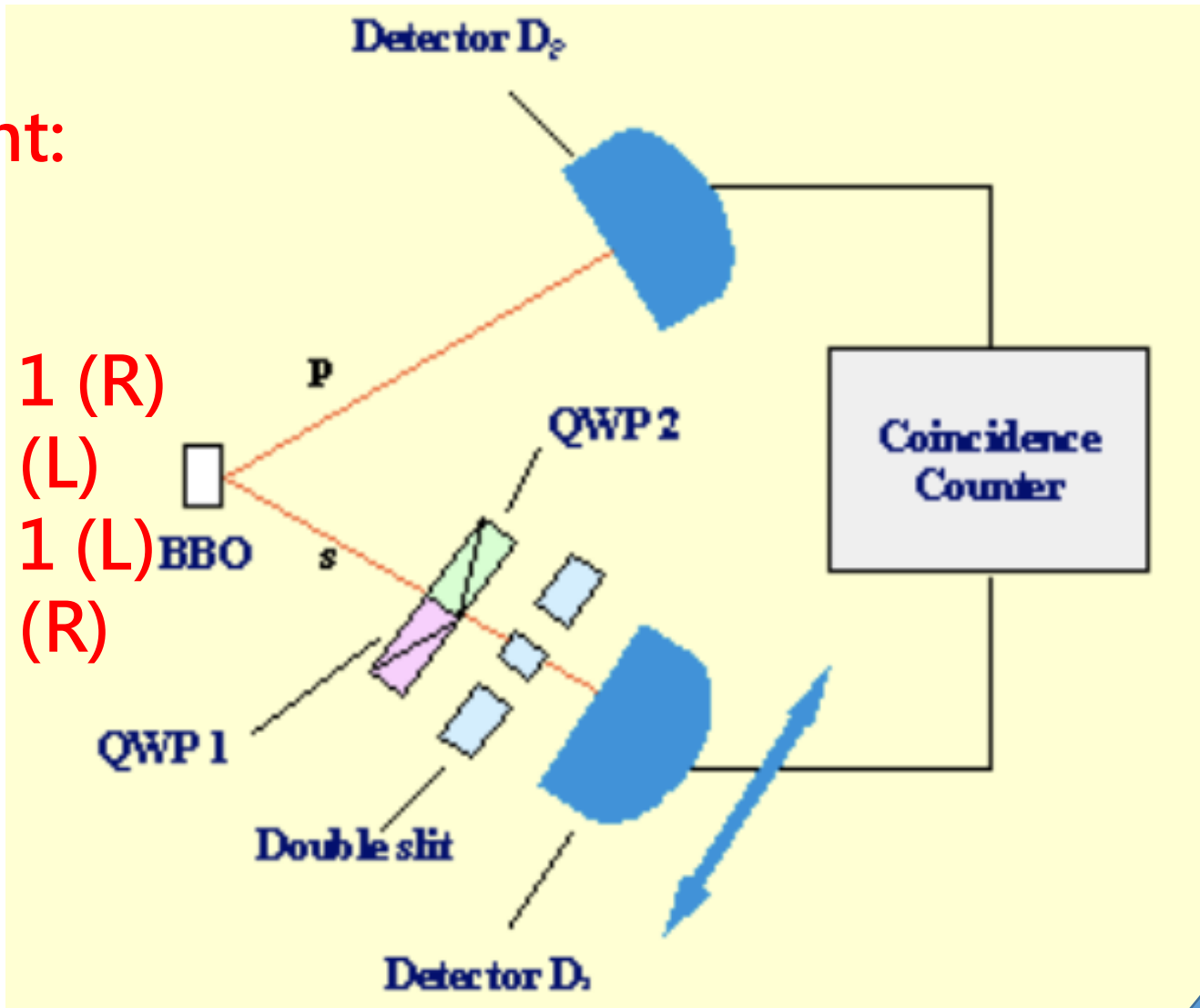
Using photons



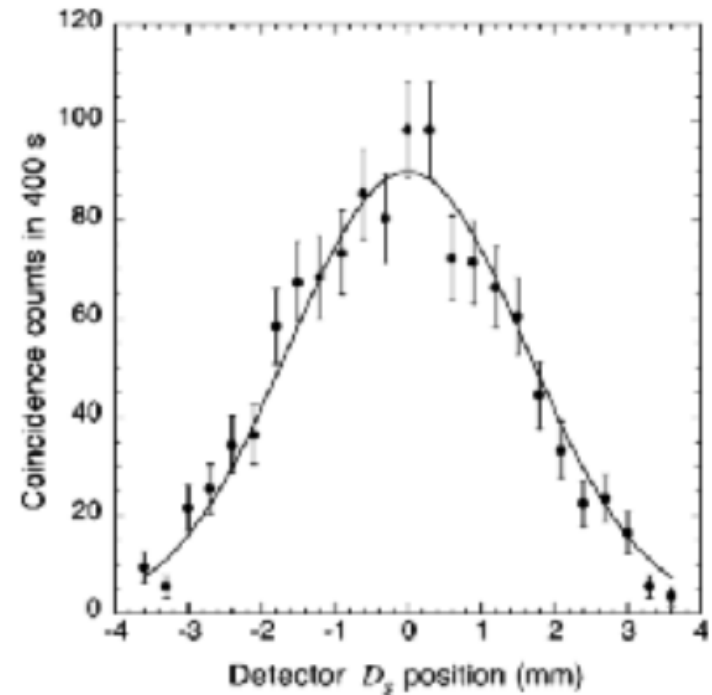
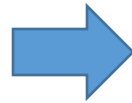
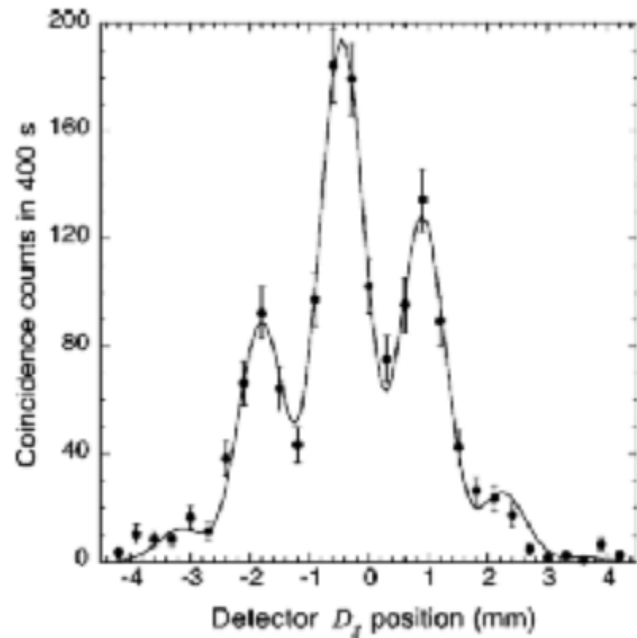
# Which way experiment by using entangled photon s

## Polarization Entanglement:

p s  
x y => QWP 1 (R)  
          QWP 2 (L)  
y x => QWP 1 (L)  
          QWP 2 (R)



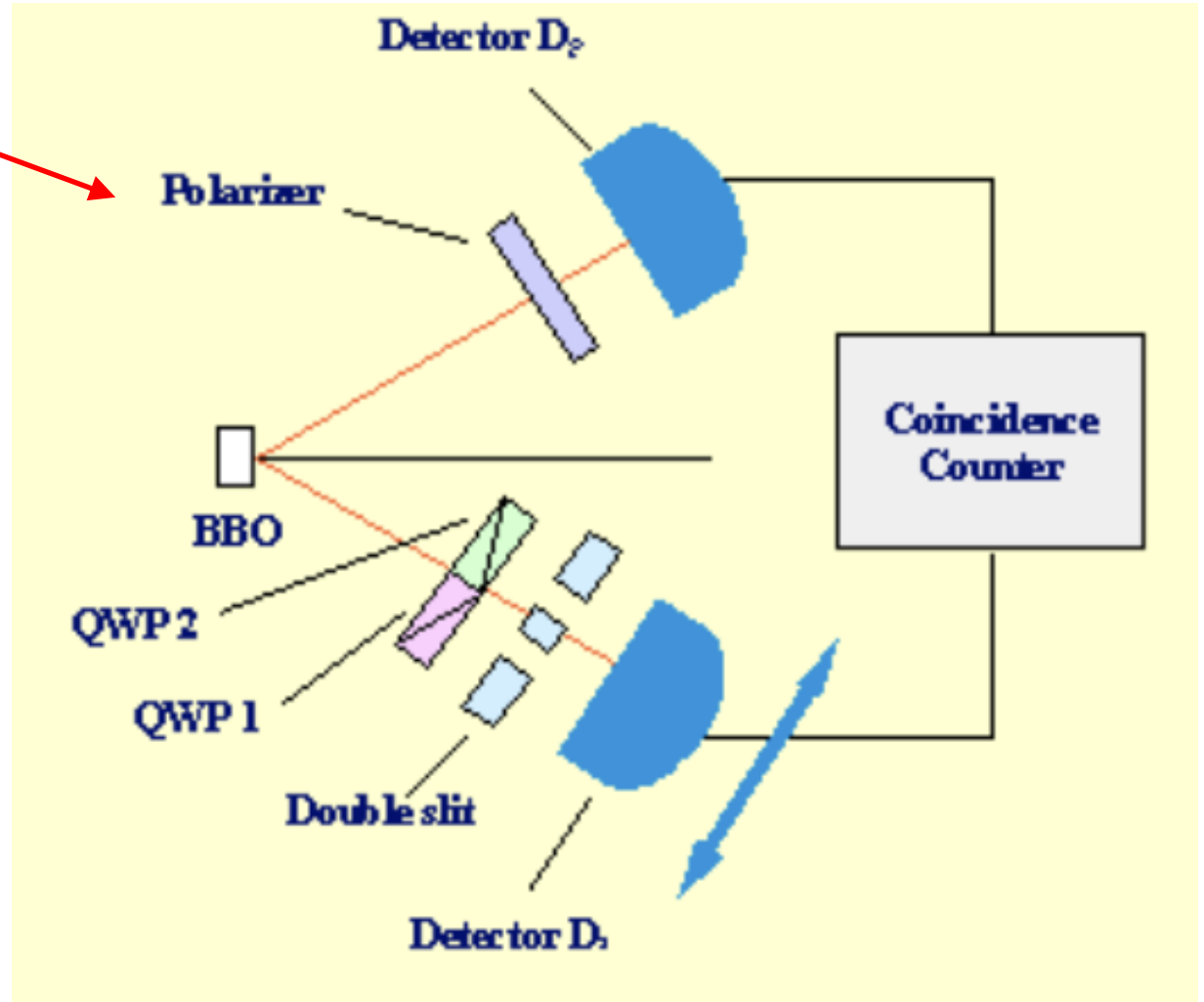
# Which way experiment by detecting polariza



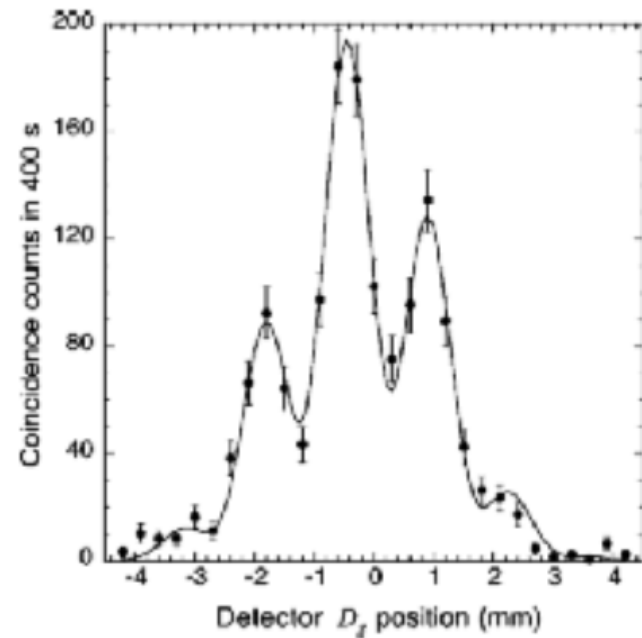
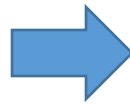
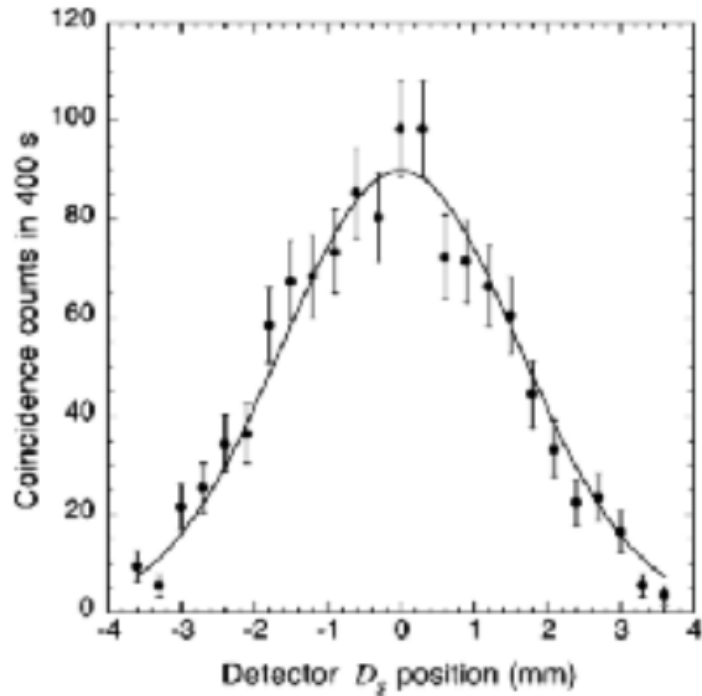
# Quantum eraser

Linear  
polarized  
along  $\frac{\pi}{4}$

$$\frac{1}{\sqrt{2}}(E, E)e^{(i\omega t - kz)}$$

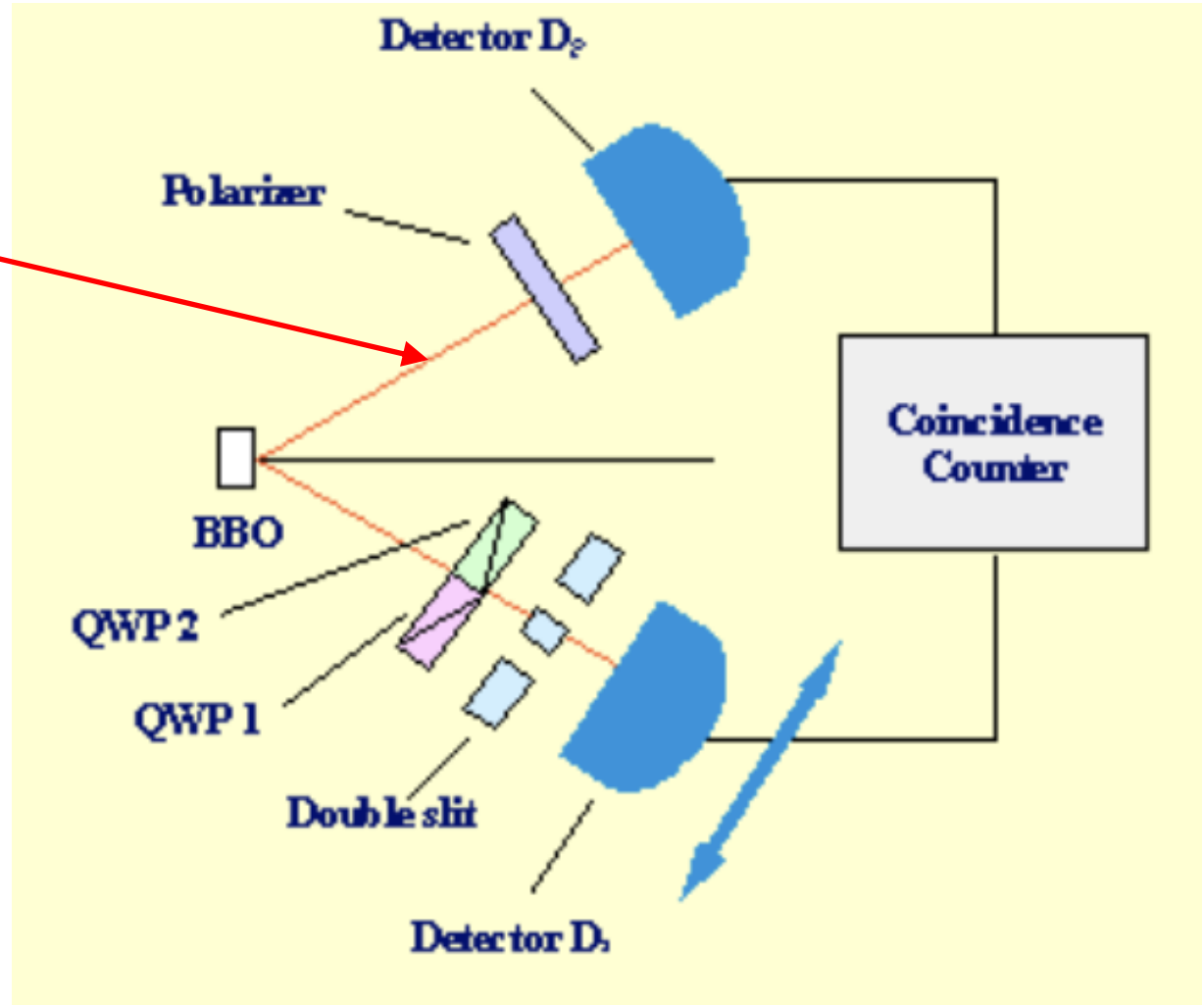


# Quantum eraser



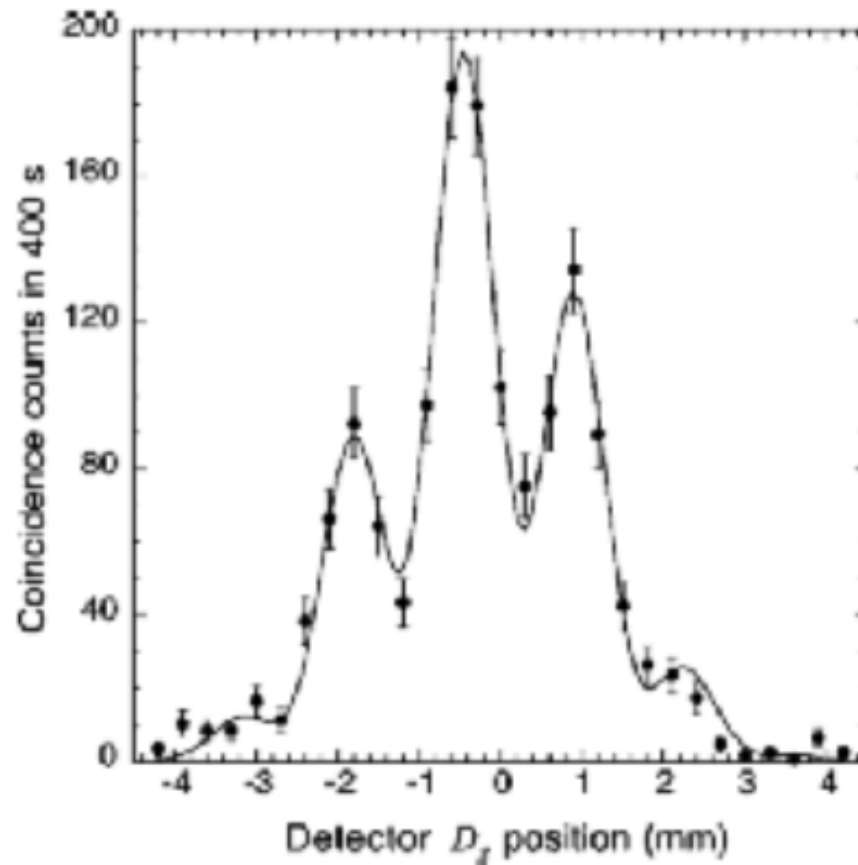
# Delayed Quantum eraser

Make it very long  
Before p photon encounter the polarizer, s photon will be detected first.





# Future affects past?



- ## 有趣的物理問題

- 電磁學(I)(II) 2014-2015

- 筆記

- ## 習題 (I)

- ### ● 第3版與第4版習題對照表

# Principle and Application of Quantum Technology (量子科技的原理與應用) 2025 Spring

- 課程大綱(Syllabus)

## 習題

- Homework 1

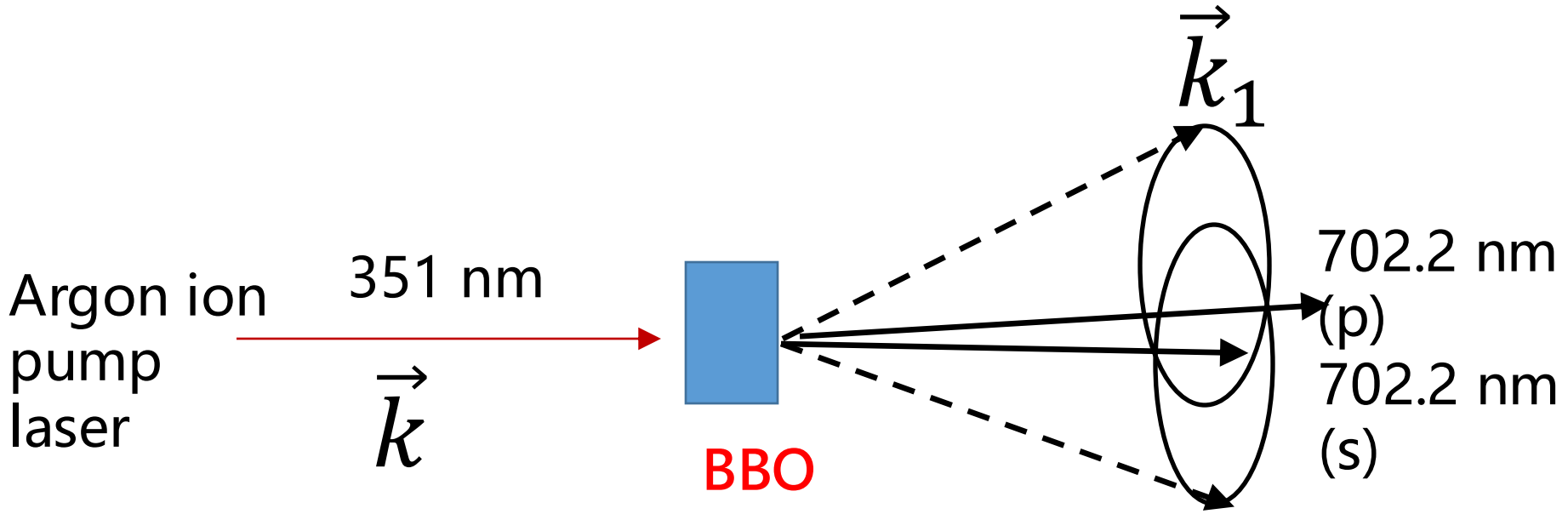
## Slides

## Chung-Yu Mou

- Introduction to quantum phenomena and quantum mechanics
  - interfere and basic quantum mechanics
- Double-slit and related experiments (Hamiltonian and Schrodinger Equation, Dirac Notation Operators in Quantum Mechanics, Heisenberg Uncertainty Wave Particle Duality, Coherence)
  - quantization
  - tunneling effect
  - two-level system and spin (quantum bit and measurement, Rabi. Oscillation, Ramsey oscillation)
  - Many-particle state and entanglement (density matrix and decoherence)
  - Quantum measurement and quantum bit
- Typical applications of quantum technology
  - Quantum algorithm and universal quantum computer
  - Quantum communication
  - Quantum simulation and method of quantum annealing
  - Quantum sensing
- Technique of quantum qubit
  - Construction and manipulation of superconducting transmon qubit
  - Construction and manipulation of qubit based on ion trap
  - Construction and manipulation of silicon-based qubit
  - Principle, construction and manipulation of topological qubit
  - Principle and technique of photon-based qubit
  - Other relevant qubit technique such as vacancy-based qubit in diamond
- Quantum communication
  - Protocols of quantum key distributions and relevant technique for their realizations
  - Single photon source, entangled-photon source, and single photon detector

# Entangled photon source

Nonlinear crystal: BBO (beta-barium borate)



$$\hbar\omega = \hbar\omega_1 + \hbar\omega_2$$

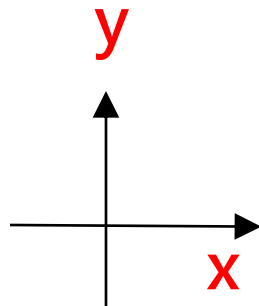
(energy conservation)

$$\hbar\vec{k} = \hbar\vec{k}_1 + \hbar\vec{k}_2$$

(momentum conservation)

Polarization  
Entanglement:

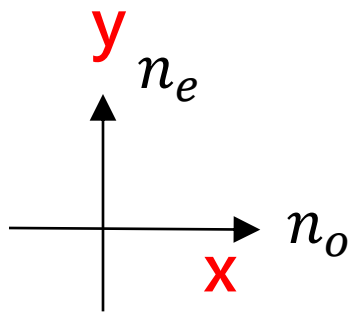
p s s p  
x y + y x



# Quarter wavelength plate (QWP)

Convert linearly polarized light into circularly polarized light and vice versa

Using birefringent material (different indices of refraction associated with different crystallographic directions.)

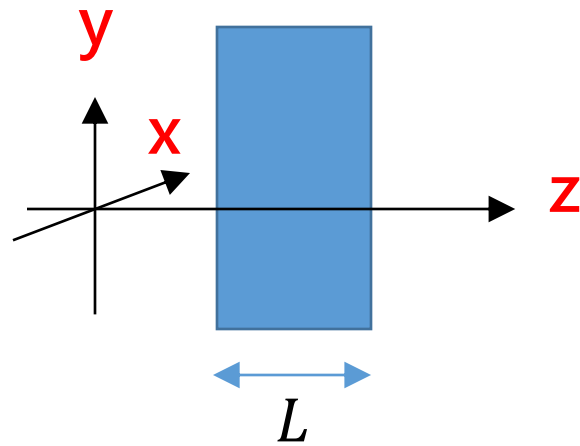


Linear Polarized along x

$$(E, 0)e^{i(\omega t - kz)}$$

Circular polarized

$$\frac{1}{\sqrt{2}} (E, \pm iE)e^{i(\omega t - kz)} \quad (+ \text{ right} - \text{ left})$$



$$\text{Phase difference: } \Gamma = \frac{2\pi\Delta nL}{\lambda_0}$$

$$\text{Quarter wave: } \Gamma = \frac{\pi}{2}$$



# Route and obstacles to large scale quantum computing

## Quantum error correction (量子除錯)

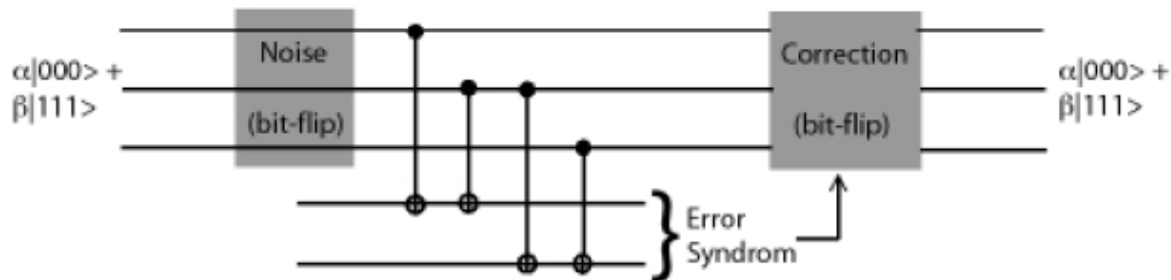
Classical error correction: repeat bits & majority vote

$0 \rightarrow 000, 1 \rightarrow 111$

Quantum: no clone theorem

$$\alpha |0\rangle + \beta |1\rangle \mapsto \alpha |000\rangle + \beta |111\rangle$$

+ two ancillary qubits



Need more physical qubits than the logical qubits!

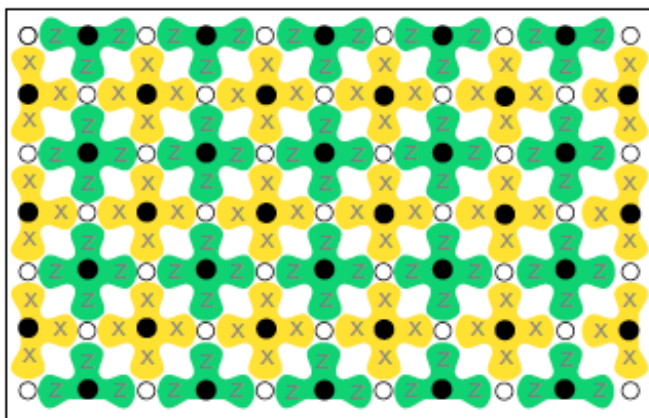
Error Location	Final State, $ data\rangle  ancilla\rangle$
No Error	$\alpha  000\rangle  00\rangle + \beta  111\rangle  00\rangle$
Qubit 1	$\alpha  100\rangle  11\rangle + \beta  011\rangle  11\rangle$
Qubit 2	$\alpha  010\rangle  10\rangle + \beta  101\rangle  10\rangle$
Qubit 3	$\alpha  001\rangle  01\rangle + \beta  110\rangle  01\rangle$



# Stabilizer codes (surface code)

Best code for tolerance of error (up to 1%): surface code (one of stabilizer codes)

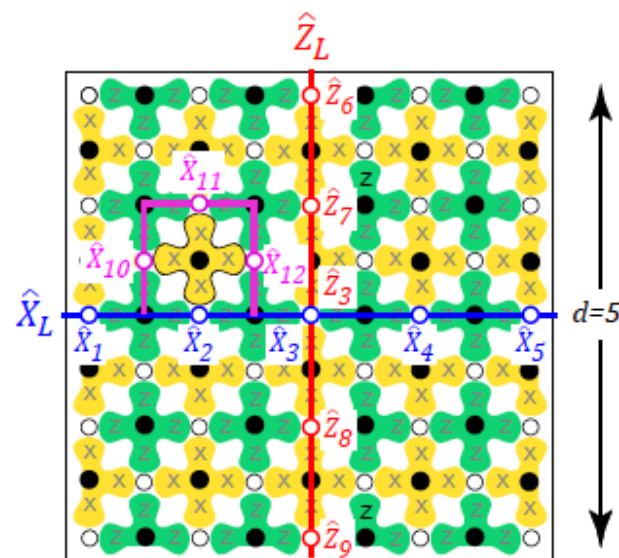
Repeat measurement of a quantum system using a complete set of commuting stabilizer (operators), the system is forced to be simultaneous and unique eigenstate of all stabilizers.



(open circles: data qubits,  
filled circles: measurement qubits)

$$X = \sigma_x, Z = \sigma_z$$

(Fowler et al .Phys. Rev. A 86, 032324, 2012)



41 data qubits but only 40 stabilizers X and Z

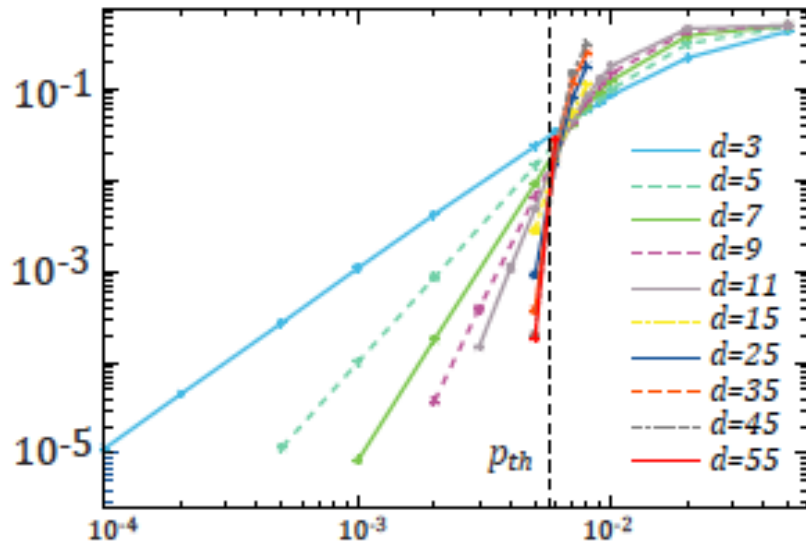
$$X_L = X_1 X_2 X_3 X_4 X_5$$

$$Z_L = Z_6 Z_7 Z_8 Z_9$$

# Thresholds for large scale quantum computation

Best code for tolerance of error (up to 1%): surface code

However, this is at the sacrifice of many physical qubits for logical qubits: one logical qubit needs  $10^3$ - $10^4$  physical qubits



Error probability  $p < p_{th}$ ,  $P_L$  decreases with increasing number ( $d$ ) of physical qubits that define operator of logical qubit.

(Fowler et al .Phys. Rev. A 86, 032324, 2012)

Factorize a number of 6000 bits (~ 600 decimal digits)

⇒ 4000 logical qubits and 130 Millions physical qubits, roughly 26.7 hours to do (100ns gate time) (classical THz computer, >150000years)

# Reference: Google 72 qubit and strategy

