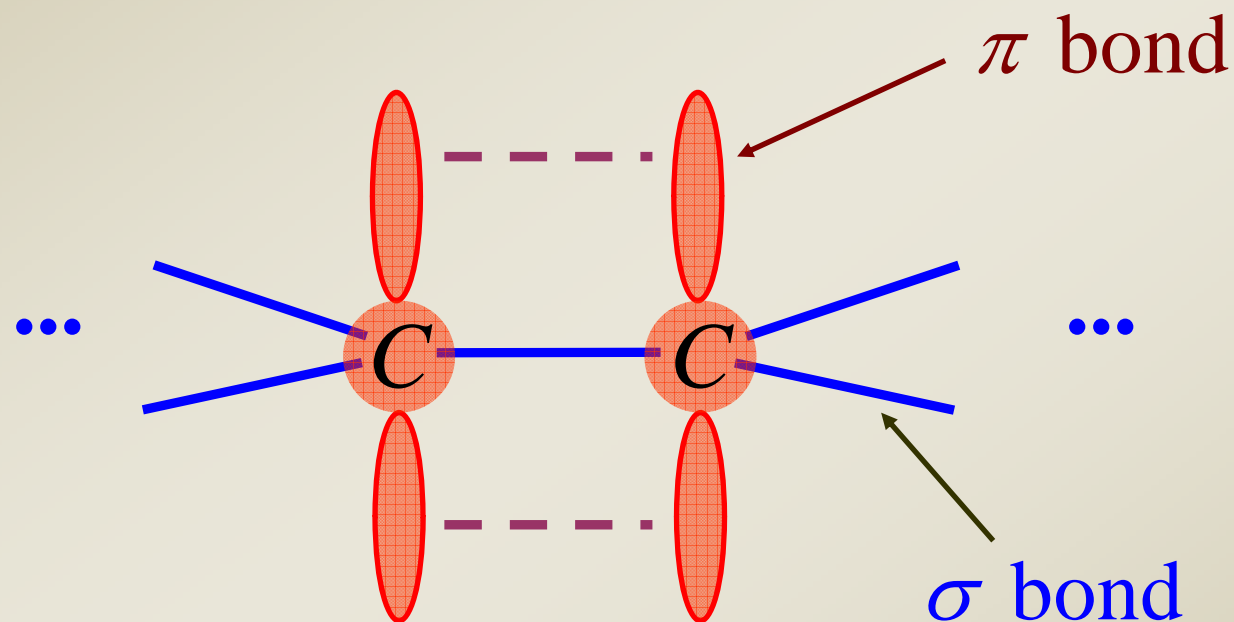


Fullerenes

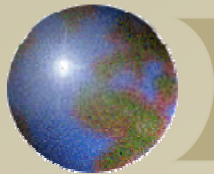
Architect: Buckminster Fuller

Orbits



Carbon $1S^2 2S^2 2P^2$

4 electrons in σ bonds (SP^2) + π bond or SP^3



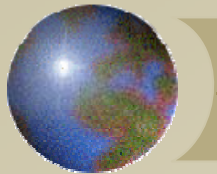
Euler's Theorem

$$F=E-V+2$$

F = number of faces

E = number of edges

V = number of vertices



C_n n = number of carbon atoms

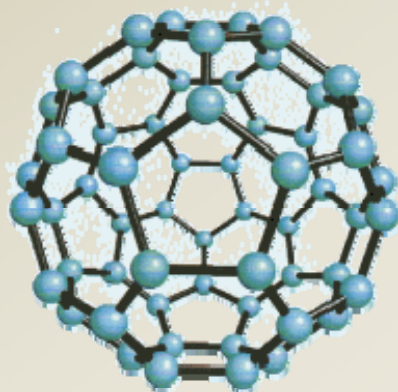
Each carbon has three edges.

$$\therefore \frac{3V}{2} = E \quad F = \frac{V}{2} + 2$$

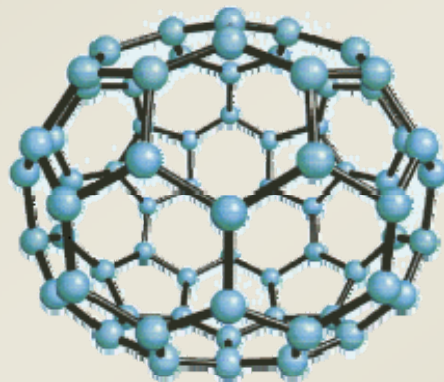
$$F_s = S \text{ 面形之數目} \Rightarrow \begin{cases} F = \sum_s F_s \\ E = \frac{1}{2} \sum_s S F_s \\ V = \frac{1}{3} \sum_s S F_s \end{cases} \Rightarrow \sum_s (6 - S) F_s = 12$$

Molecules with 5-fold symmetry

$$\sum_S (6 - S) F_S = 12 \Rightarrow F_6 \text{ is arbitrary.}$$



C_{60}



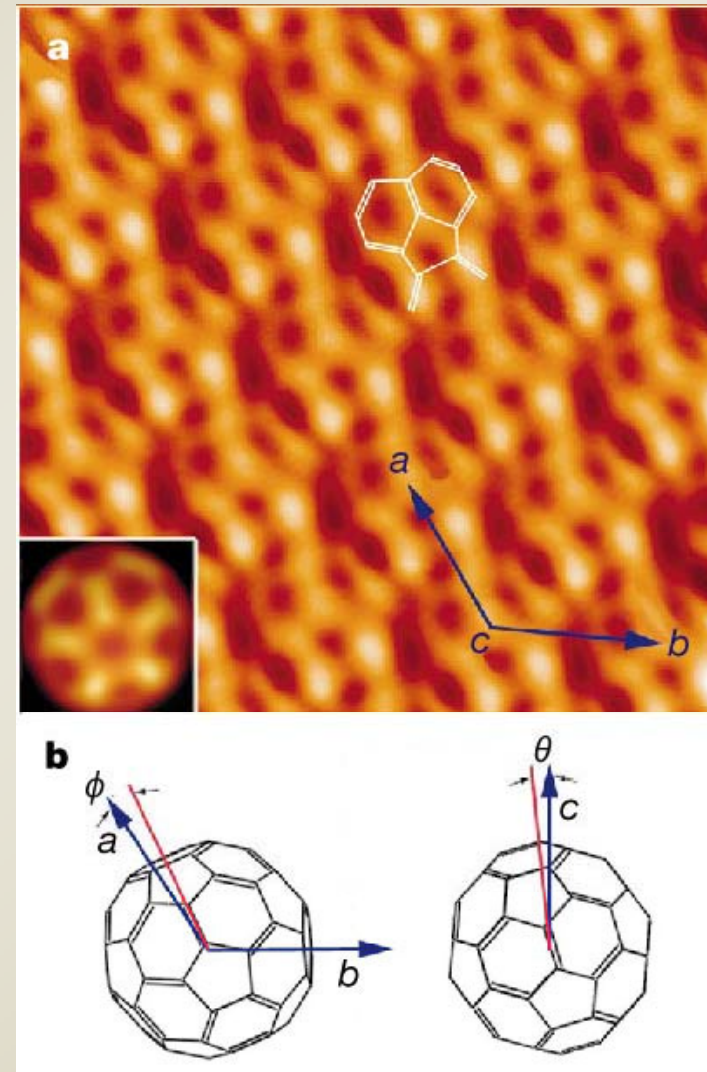
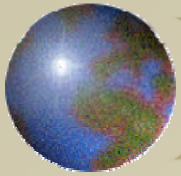
C_{70}

$$C_{60} \text{ 12個pentagon } \therefore 3V = 5F_5 + 6F_6$$

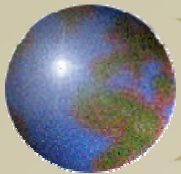
$$\therefore 3 \times 60 = 5 \times 12 + 6F_6 \quad F_6 = 20$$

$$C_{70} \text{ 12個pentagon } \therefore 3V = 5F_5 + 6F_6$$

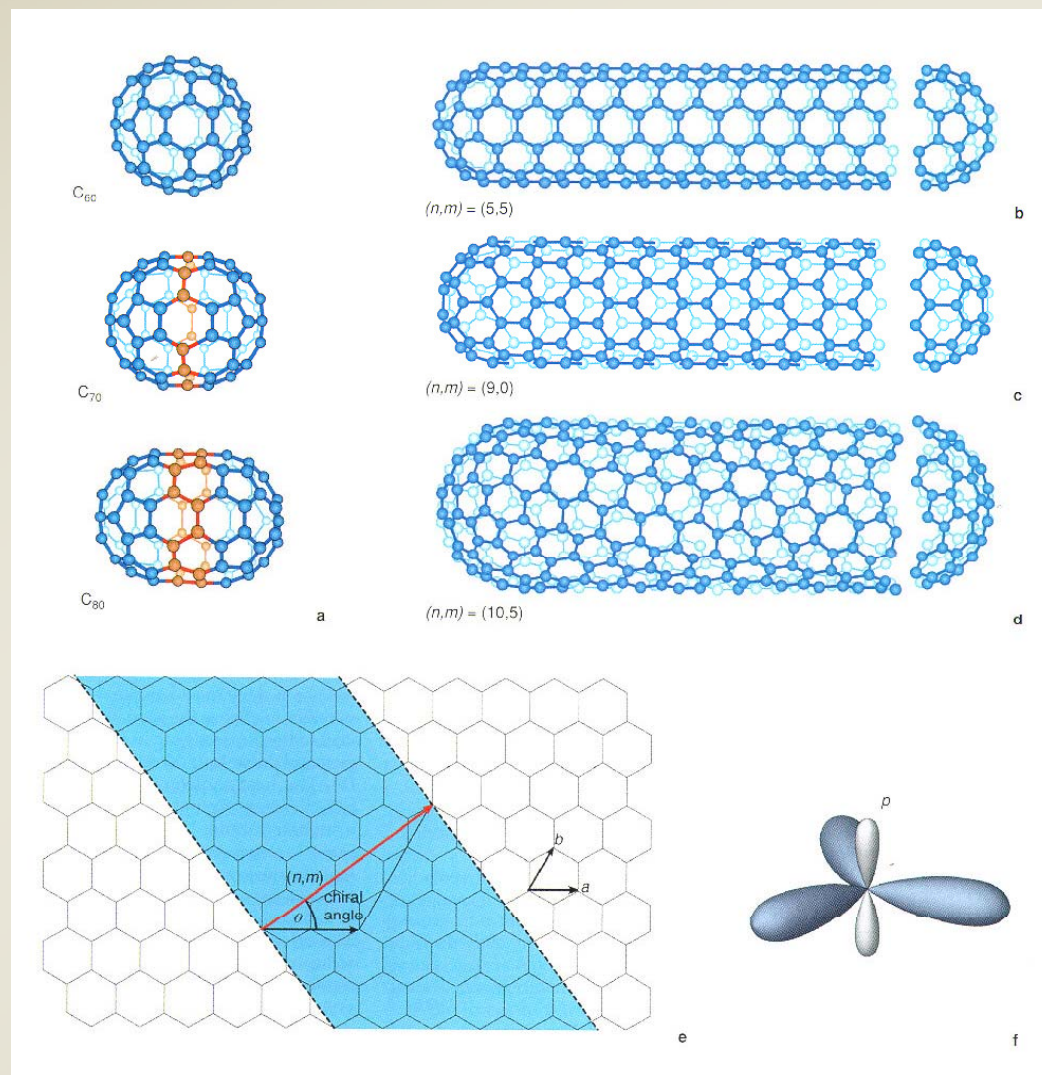
$$\therefore 3 \times 70 = 5 \times 12 + 6F_6 \quad F_6 = 25$$

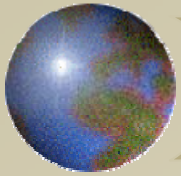


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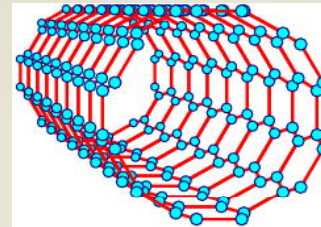
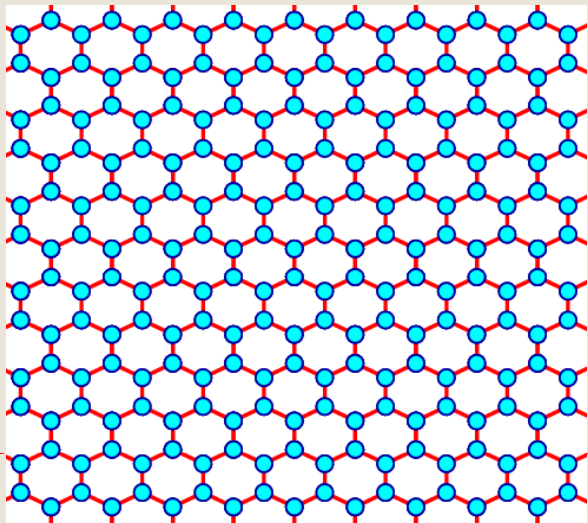


奈米碳管

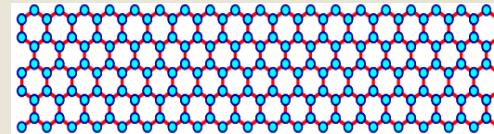




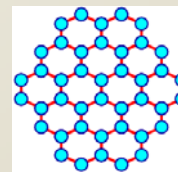
Graphene: Graphite sheet



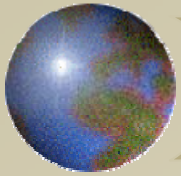
Nanotube



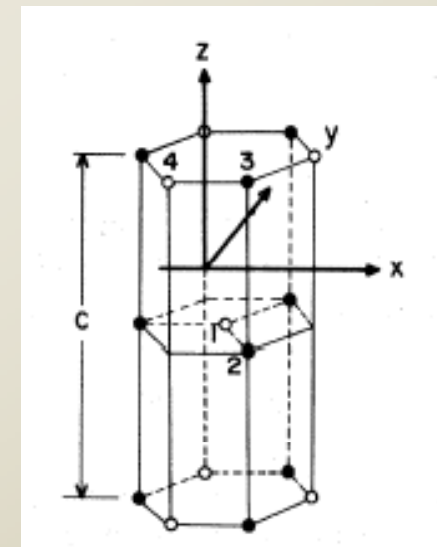
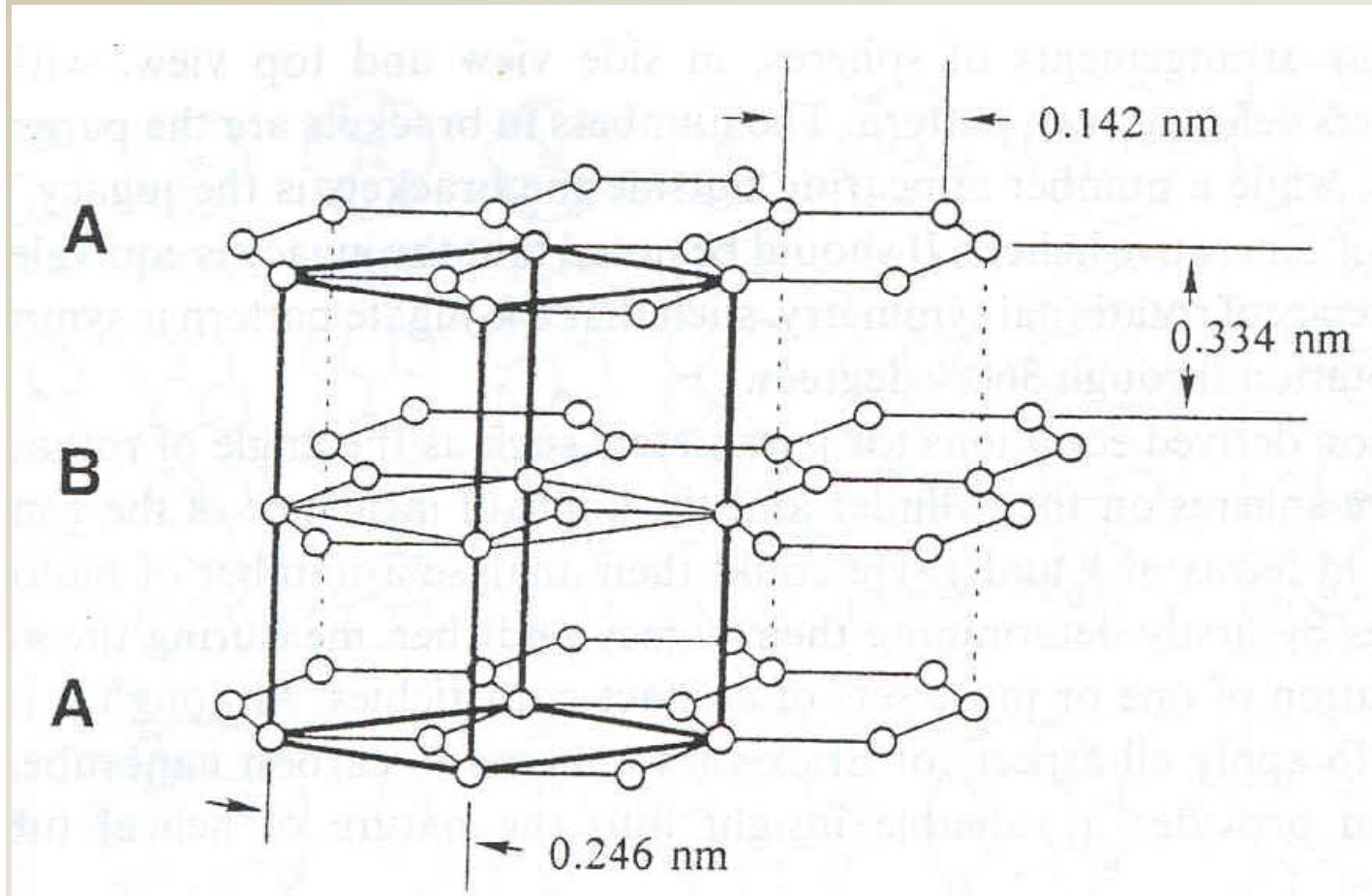
Nanoribbon



Nanoparticle



石墨的結構



Unit cell

Crystal and Orientations of C_{60}

$T > 250^\circ C$

Free rotational motion

→ isotropic



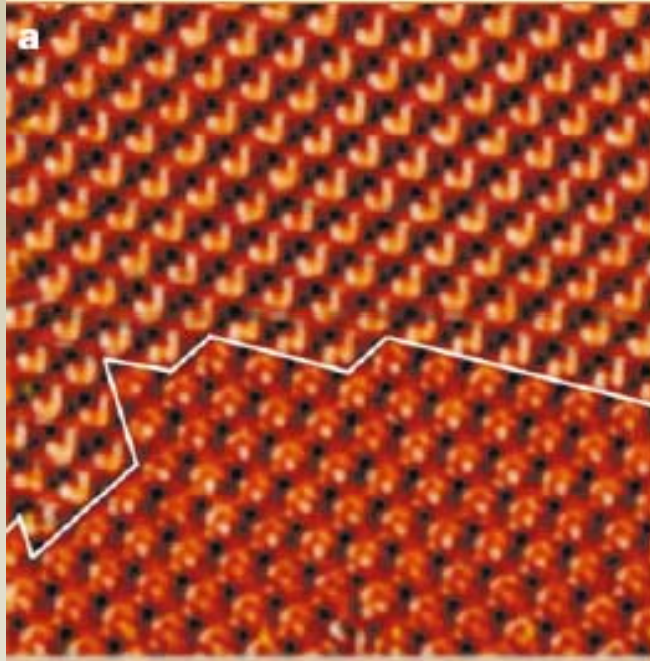
$T < 250^\circ C$ corner, 3 face atoms form

4 penetrating Simple Cubic lattices

with 4 different orientation of 3-fold axes along 4 $\langle 111 \rangle$

(rotation about these axes smeared out 5-fold symmetry)

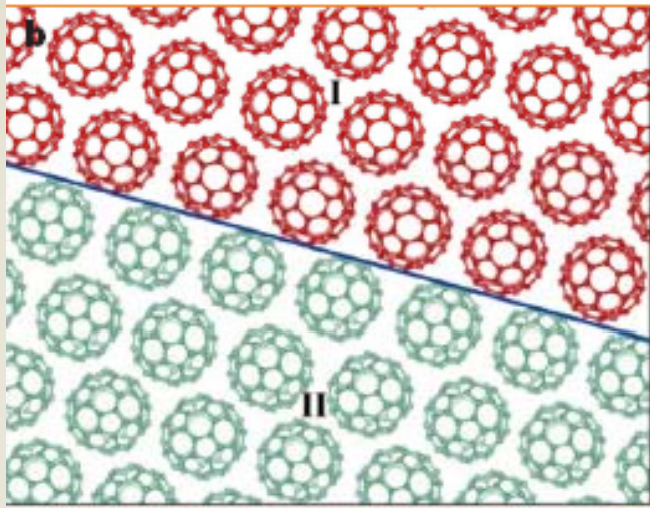
2D Crystal with 5-fold symmetric molecules



$100\text{\AA} \times 100\text{\AA}$

Orientation Sudden

Changed across domain



Nature 409, 304(2001)