

Optical Frequency Comb: A Journey for Precision Light



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Outline

- ◆ *Why Precision Light?*
- ◆ *Optical Frequency Measurement in Pre-OFC Era*
- ◆ *Understanding OFC*
- ◆ *NTHU OFC*
- ◆ *What can OFC do for us?*

Why Precision Light?

◆ *Metrology*

- ◆ *Frequency, Time and Length Standard*
- ◆ *Physical Constants*
- ◆ *Precision Probe for Small Effects and Internal Structure of Molecules*
- ◆ *Temporal Variation of Physical Constants, QED Test etc.*
- ◆ *Practical Applications*
- ◆ *DWDM for Optical Fiber Communication, Quantum Information?*

Optical Frequency Measurement in Pre-OFC Era

Frequency Chain for ${}^4\text{Ca}$ 657 nm

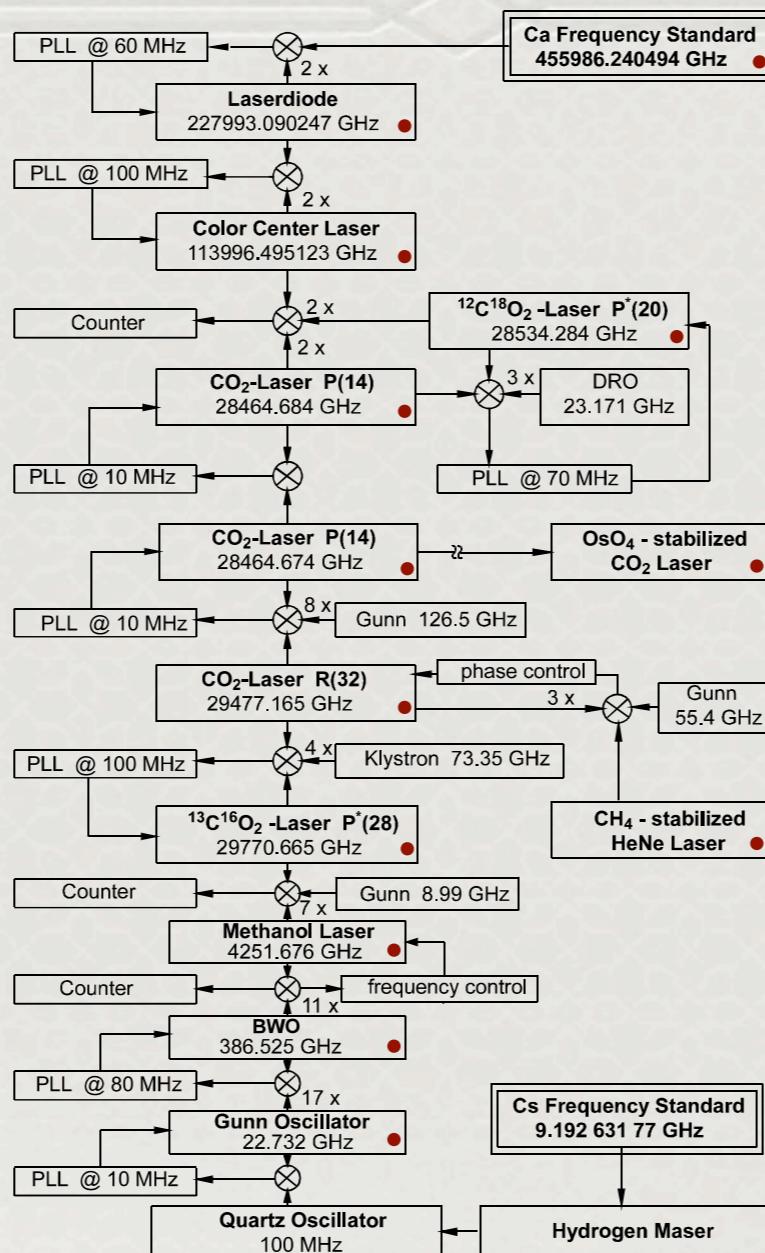


Fig. 17. Frequency-measurement chain to the Ca intercombination line

Frequency Chain for Hydrogen $1S-2S$

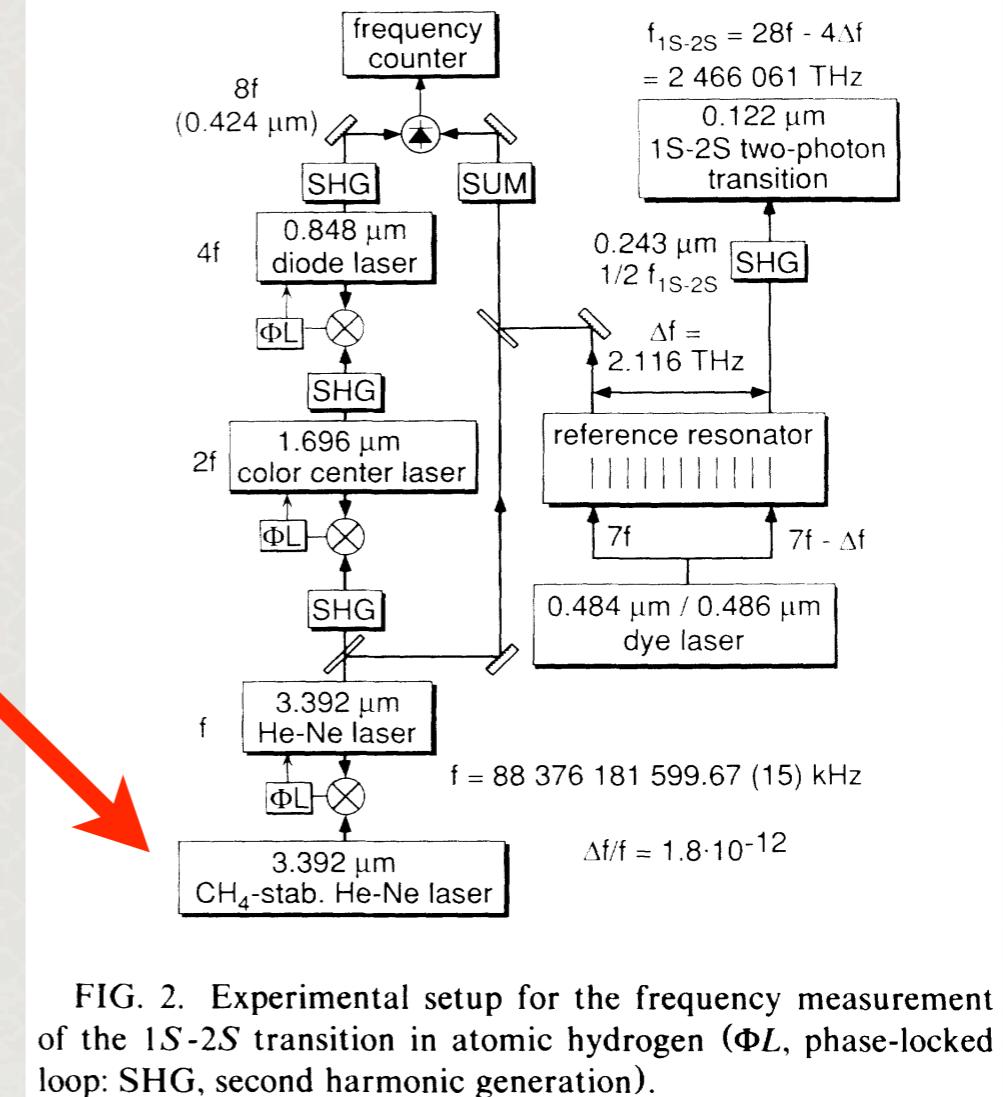
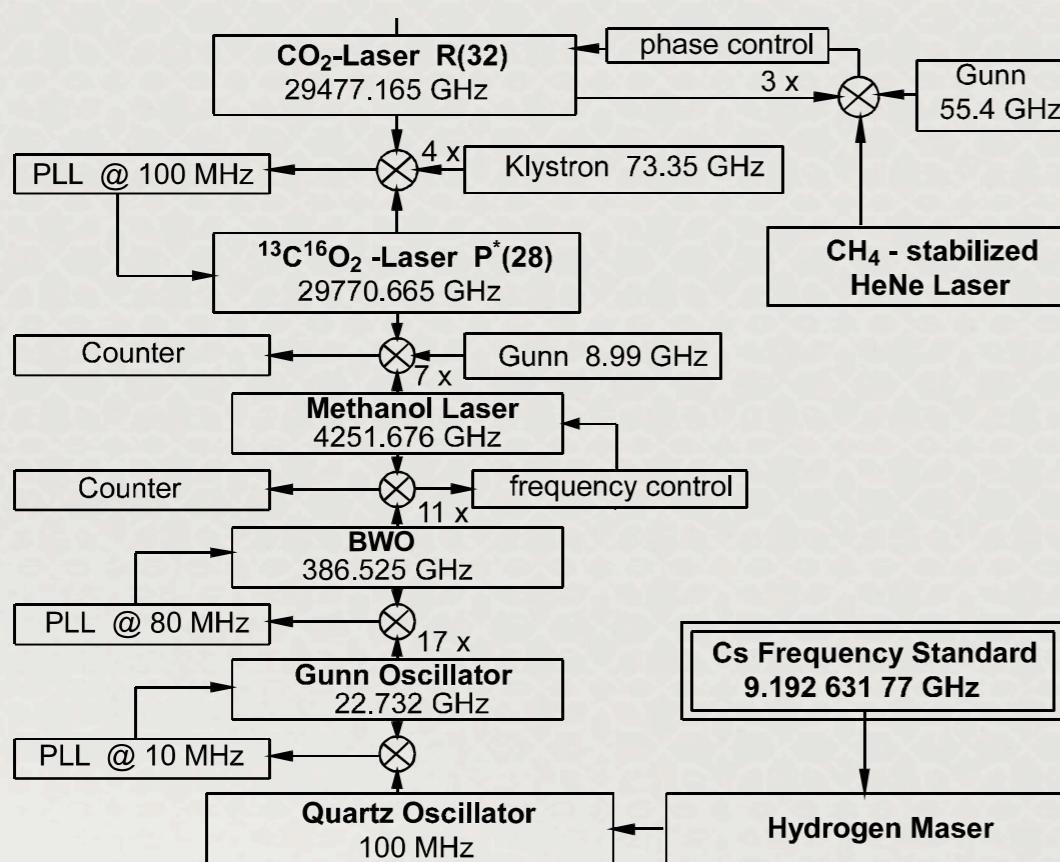
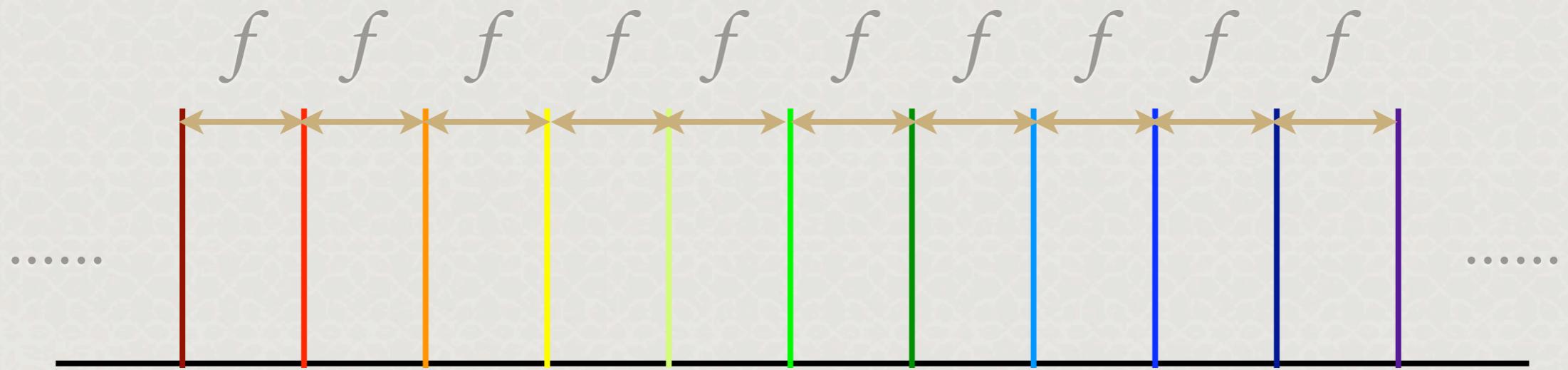


FIG. 2. Experimental setup for the frequency measurement of the $1S-2S$ transition in atomic hydrogen (ΦL , phase-locked loop; SHG, second harmonic generation).

Laser Shuttle between PTB & Hänsch's Group

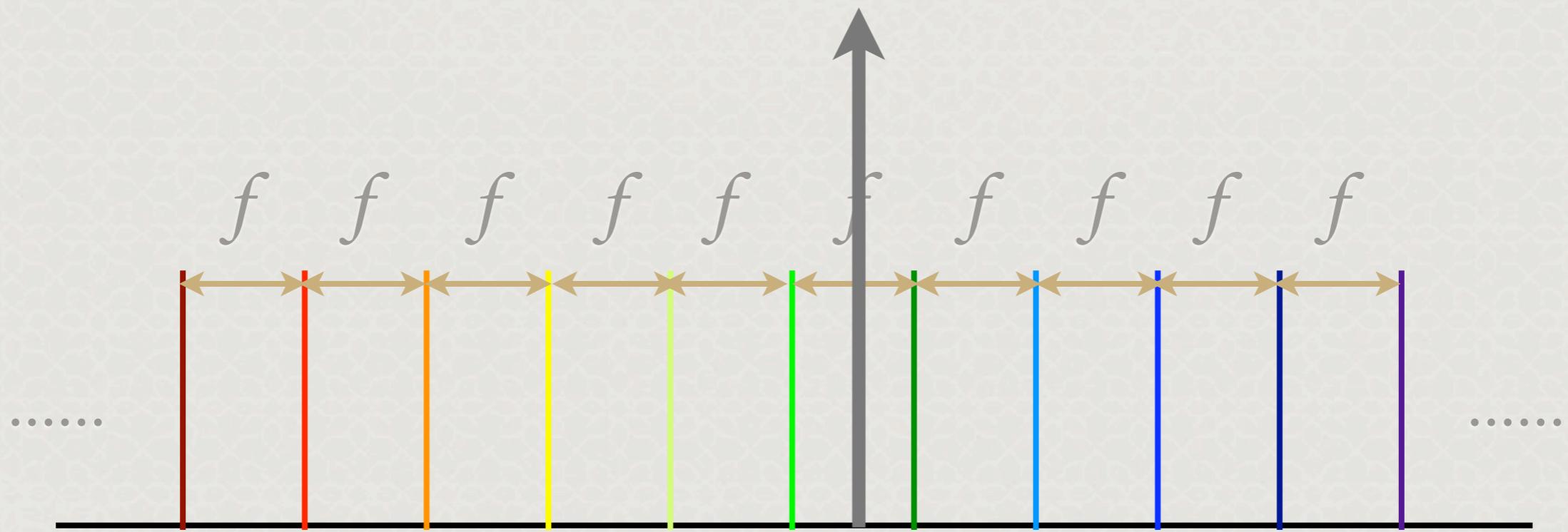
Understanding OFC

What is Optical Frequency Comb



A series of equal-spaced comb lines in frequency domain.

What is Optical Frequency Comb



A series of equal-spaced comb lines in frequency domain.

How to Build a OFC

How to Build a OFC

- ◆ *Cavity Enhanced Phase Modulation*

How to Build a OFC

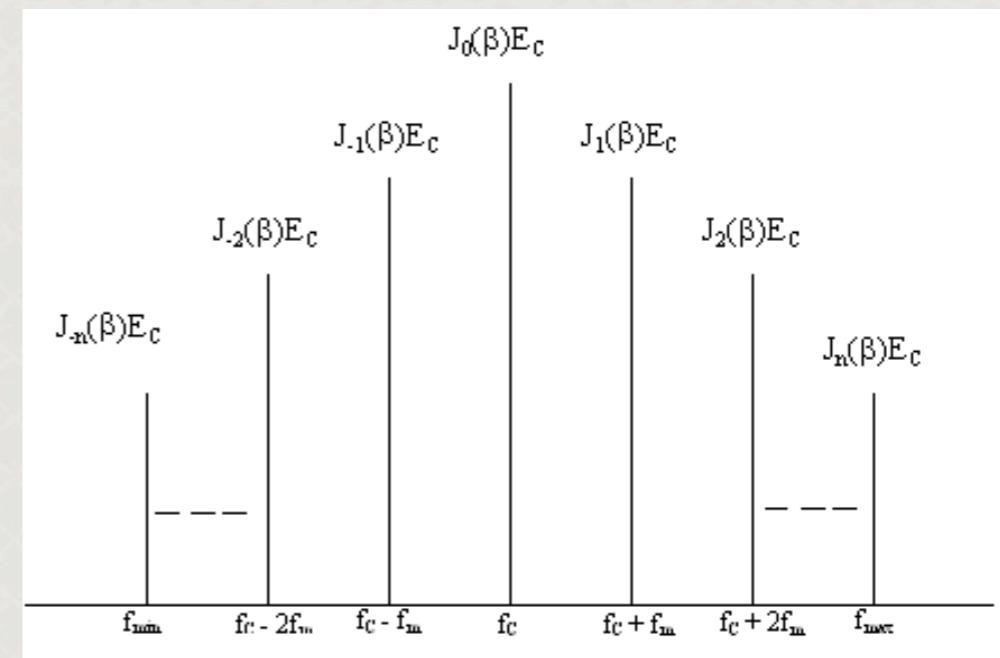
- ◆ *Cavity Enhanced Phase Modulation*
- ◆ *Mode-locking Lasers*
 - ◆ *Ti:sapphire ($Ti^{3+}:Al_2O_3$): 800 nm*
 - ◆ *Cr:forsterite ($Cr^{3+}:Mg_2SiO_4$): 1235 nm*
 - ◆ *Er-doped Fiber: 1550 nm*

Cavity Enhanced Phase Modulation

- ◆ *Frequency sidebands are generated by phase modulator and enhanced by Fabry-Pérot cavity*
- ◆ *Originally constructed for picosecond pulse generation in 1972 and re-implemented by M. Kurogi, K. Nakagawa, M. Ohtsu in 1993 for frequency measurement*

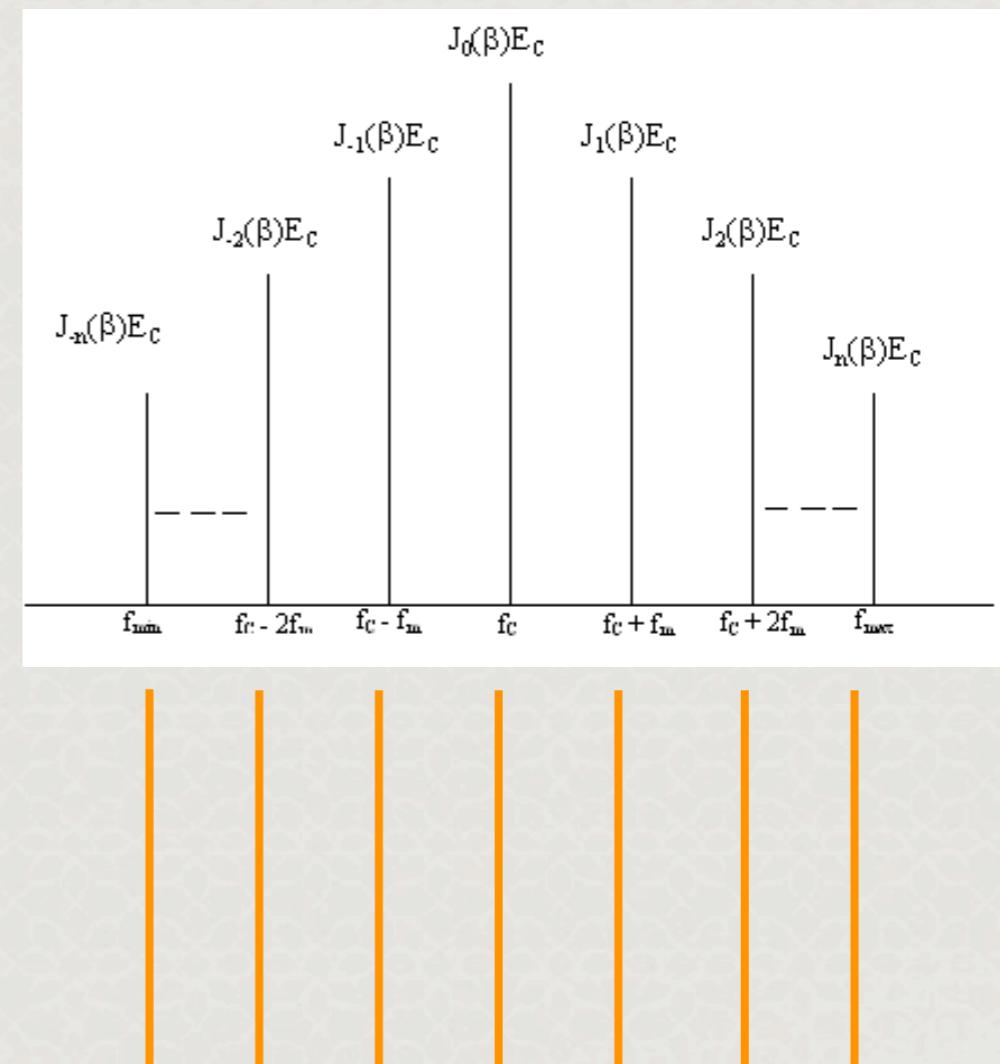
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Cavity Longitudinal Modes

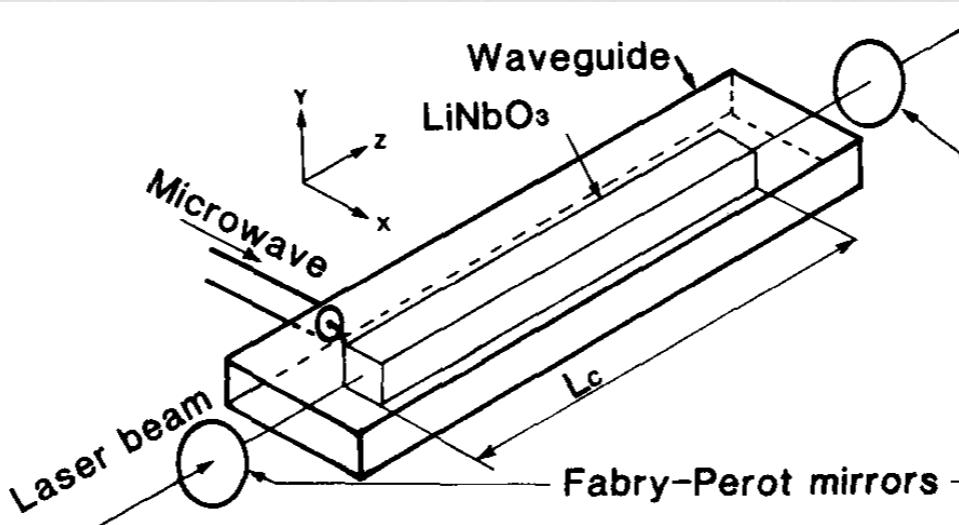
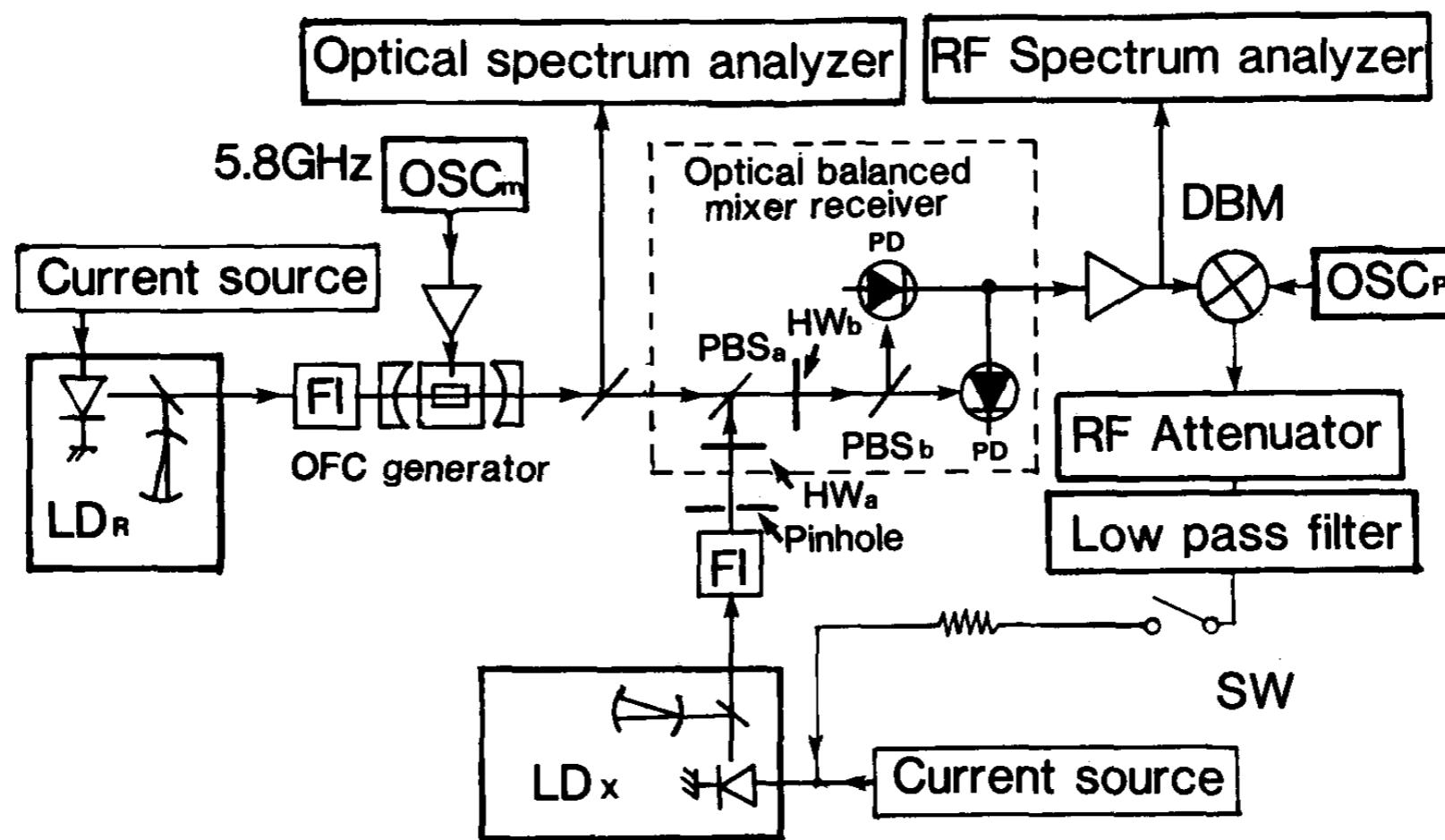
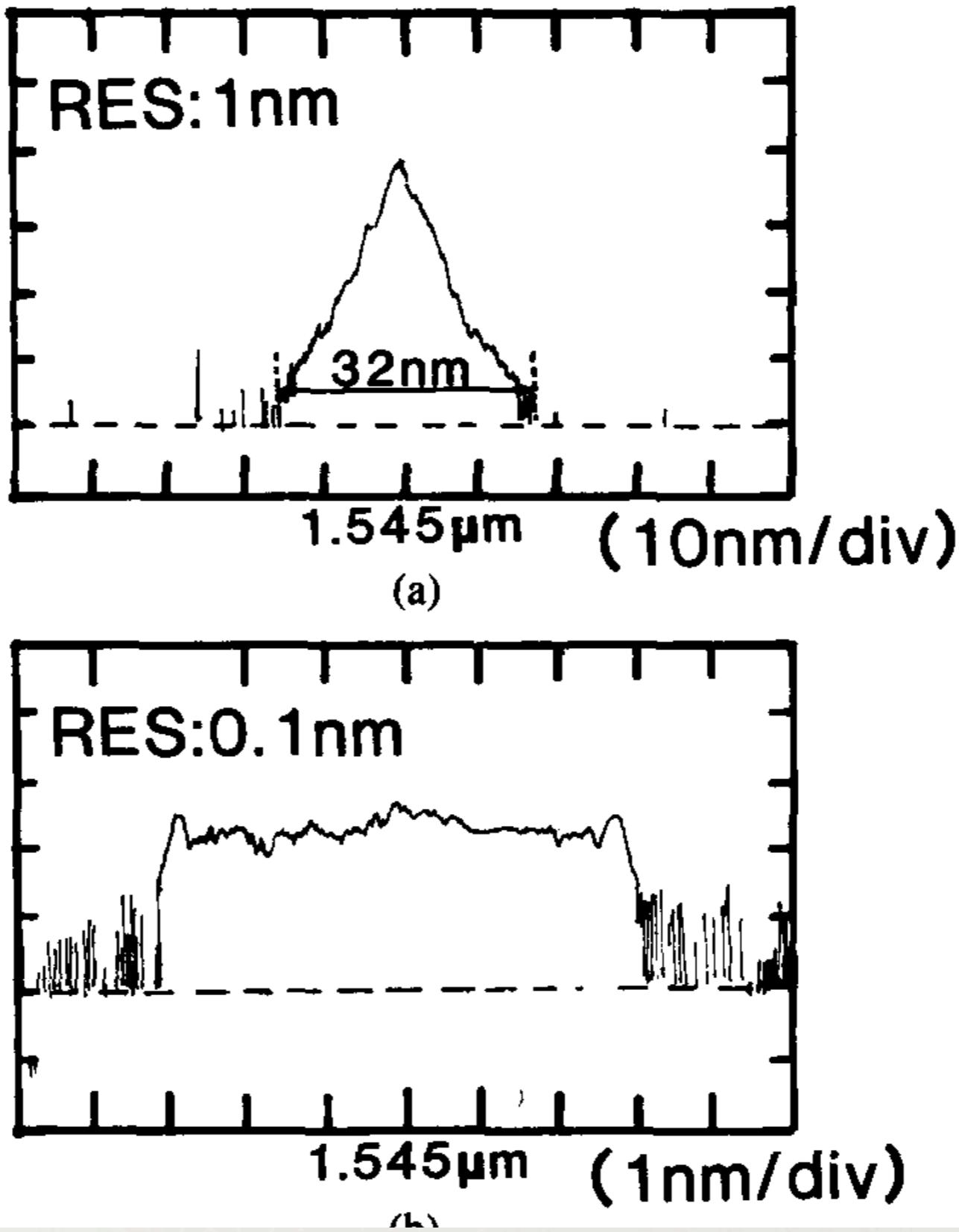


Fig. 2. The construction of the present optical frequency comb generator.



Intensity(10dB/div)

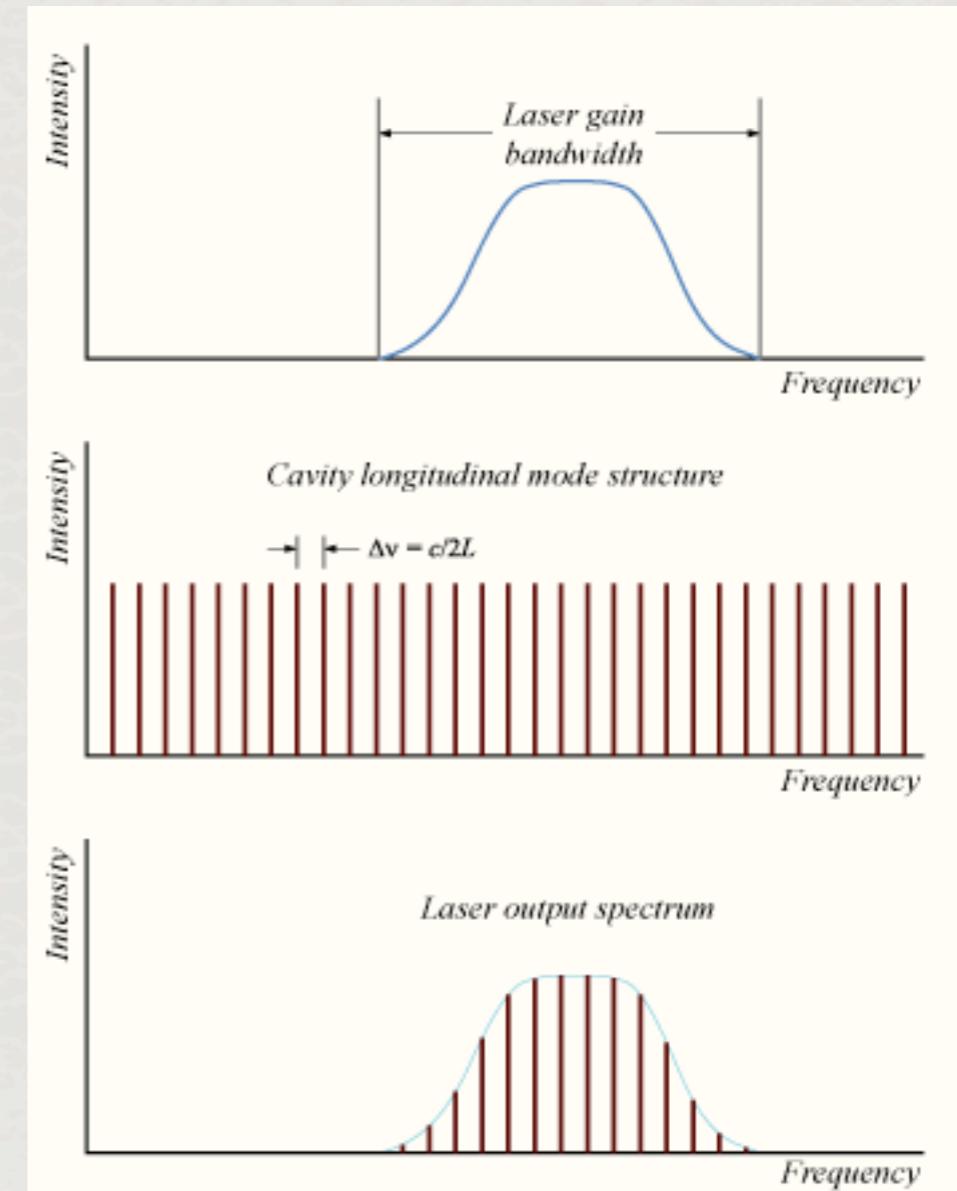


Mode-locked Lasers

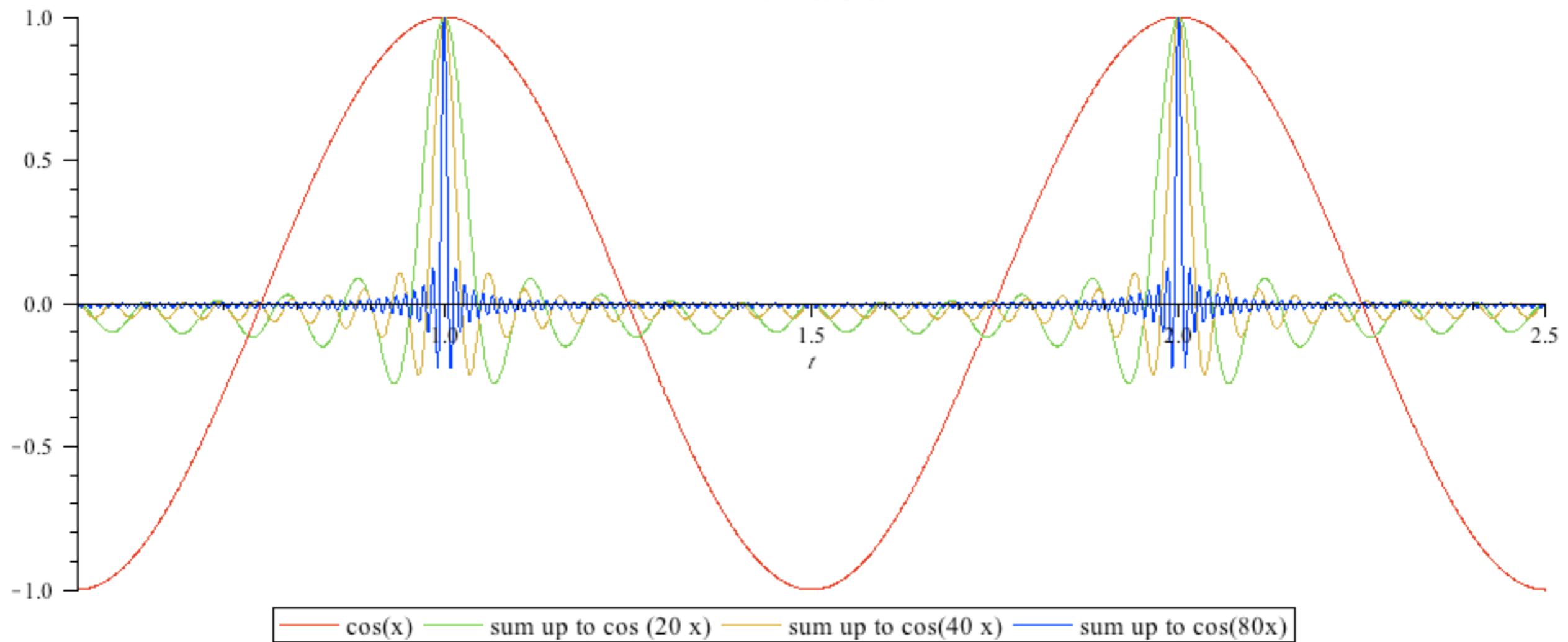
- ◆ *Multi-longitudinal-mode in frequency domain and pulse operation in time domain*
- ◆ *The modes are equal-spaced in frequency and phase-coherent*
- ◆ *The frequency of each mode can be written as:*

$$F_n = n \times F_r + F_o$$

- * *F_r : Repetition Frequency
=Longitudinal Mode Spacing*
- * *F_o : Offset Frequency*



With Zero Phase Offset

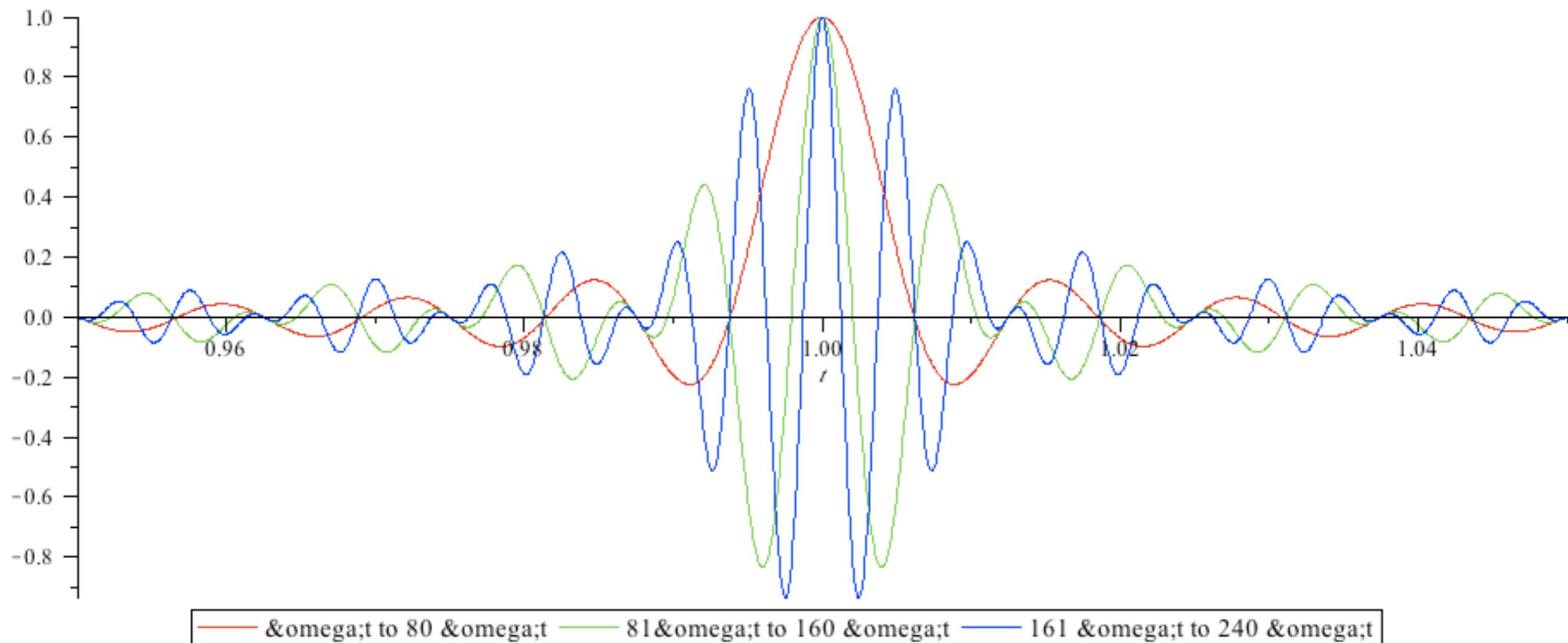


$$\sum_{N=1}^{10} \cos(N\omega t)$$

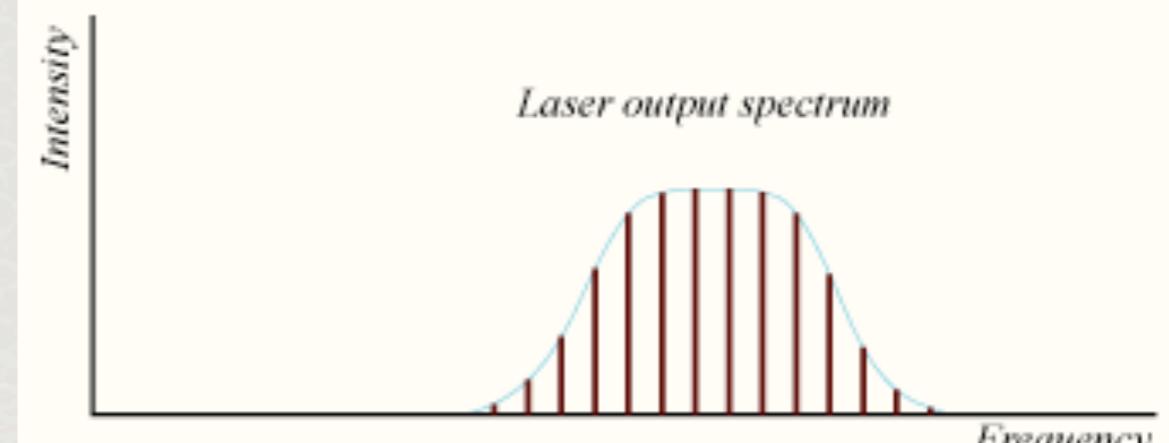
$$\sum_{N=1}^{20} \cos(N\omega t)$$

$$\sum_{N=1}^{80} \cos(N\omega t)$$

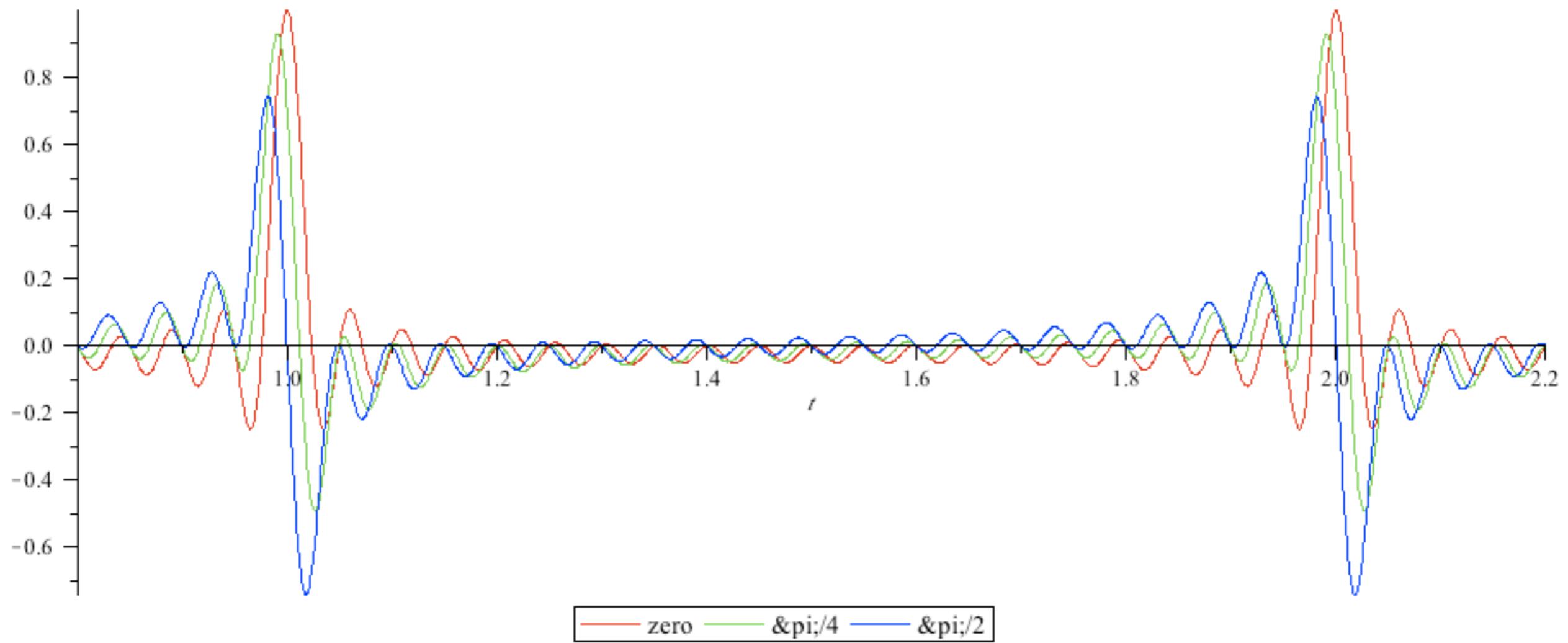
With Zero Phase Offset



$$\begin{aligned}
 & \sum_{N=1}^{80} \cos(N\omega t) \\
 & \sum_{N=81}^{160} \cos(N\omega t) \\
 & \sum_{N=161}^{240} \cos(N\omega t)
 \end{aligned}$$



With Constant Phase Shift

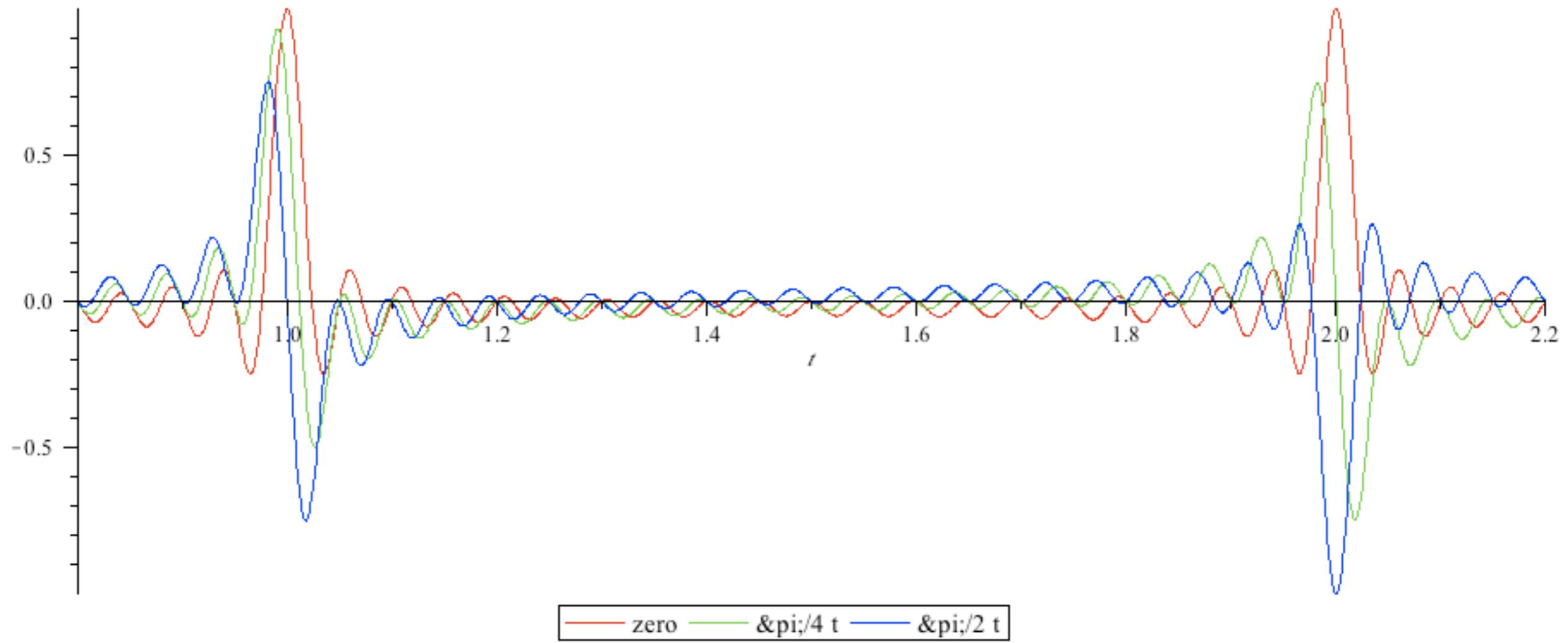


$$\sum_{N=1}^{20} \cos(N\omega t)$$

$$\sum_{N=1}^{20} \cos\left(N\omega t + \frac{\pi}{4}\right)$$

$$\sum_{N=1}^{20} \cos\left(N\omega t + \frac{\pi}{2}\right)$$

With Linear Phase Shift in Time



$$\sum_{N=1}^{20} \cos(N\omega t)$$

$$\sum_{N=1}^{20} \cos(N\omega t + \frac{\pi}{4}t)$$

$$\sum_{N=1}^{20} \cos(N\omega t + \frac{\pi}{2}t)$$

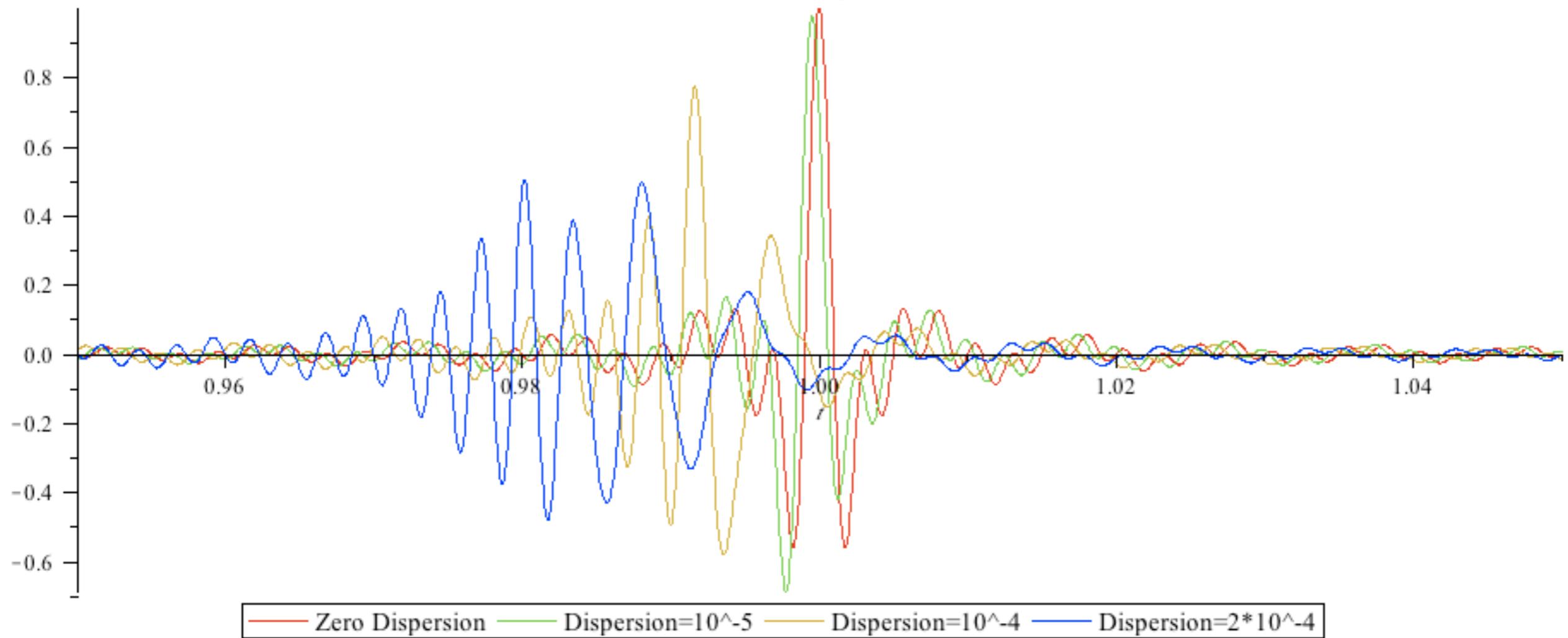
$$f = \frac{d\phi}{dt}$$

$$\omega_1 = \omega, 2\omega, \dots, 20\omega$$

$$\omega_2 = \omega + \frac{\pi}{4}, 2\omega + \frac{\pi}{4}, \dots, 20\omega + \frac{\pi}{4}$$

$$\omega_3 = \omega + \frac{\pi}{2}, 2\omega + \frac{\pi}{2}, \dots, 20\omega + \frac{\pi}{2}$$

With Constant Disperison



$$\sum_{N=101}^{400} \frac{1}{300} \cos(N\omega t)$$

$$\sum_{N=101}^{400} \frac{1}{300} \cos(N\omega t + 10^{-5}\omega^2)$$

$$\sum_{N=101}^{400} \frac{1}{300} \cos(N\omega t + 10^{-4}\omega^2)$$

$$\sum_{N=101}^{400} \frac{1}{300} \cos(N\omega t + 2 \times 10^{-4}\omega^2)$$

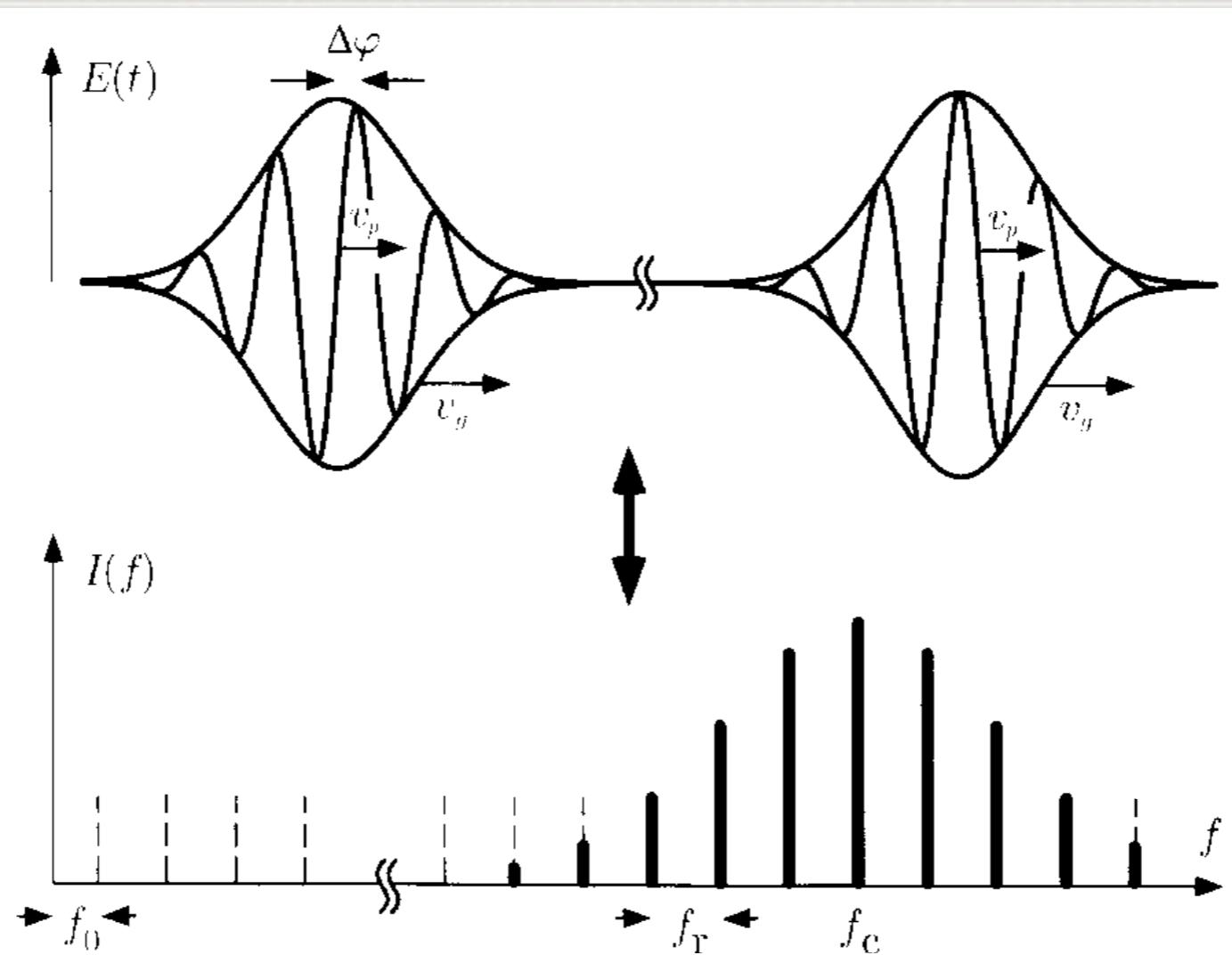
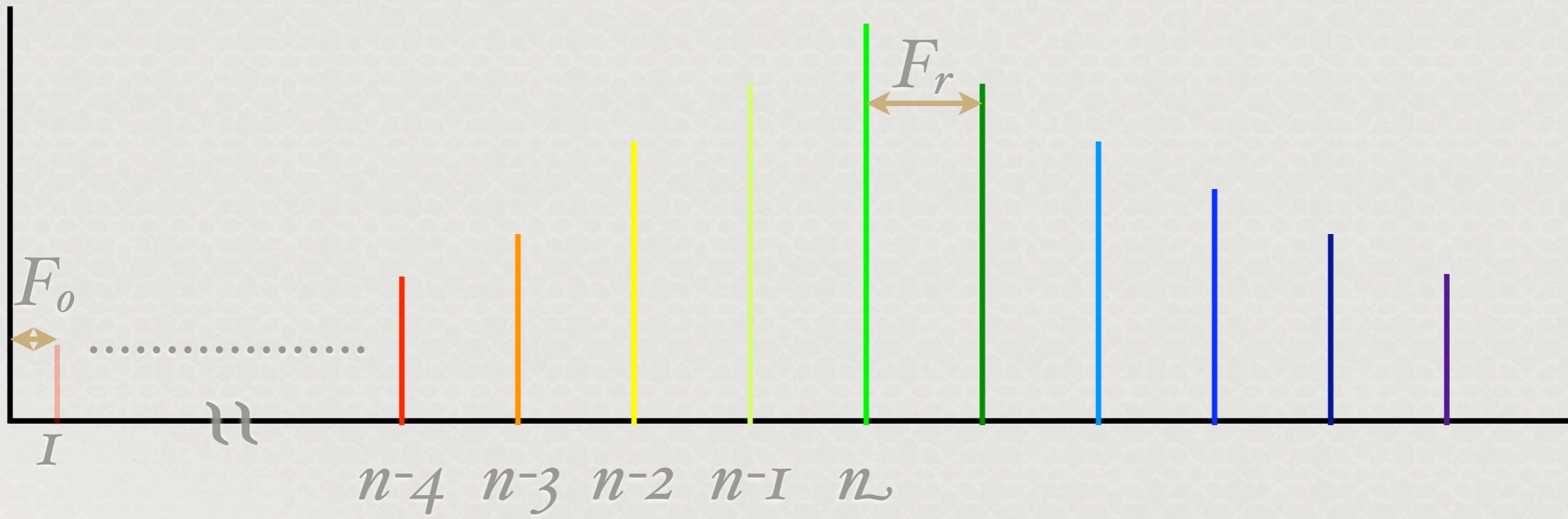


Fig. 1. Two consecutive pulses of the pulse train emitted by a mode-locked laser and intensity spectrum of the train. Within the cavity, the envelope is traveling with the group velocity v_g which, in general, differs from the phase velocity of the carrier v_p . The carrier phase relative to the envelope changes from pulse to pulse by $\Delta\varphi$. The modes are offset from being integer multiples of the pulse repetition rate f_r by $f_0 = (\Delta\varphi/2\pi)f_r$.

J. Reichert et al. Opt. Comm. 172, 59 (1998)

Controlling Frequency of Mode-locked Laser

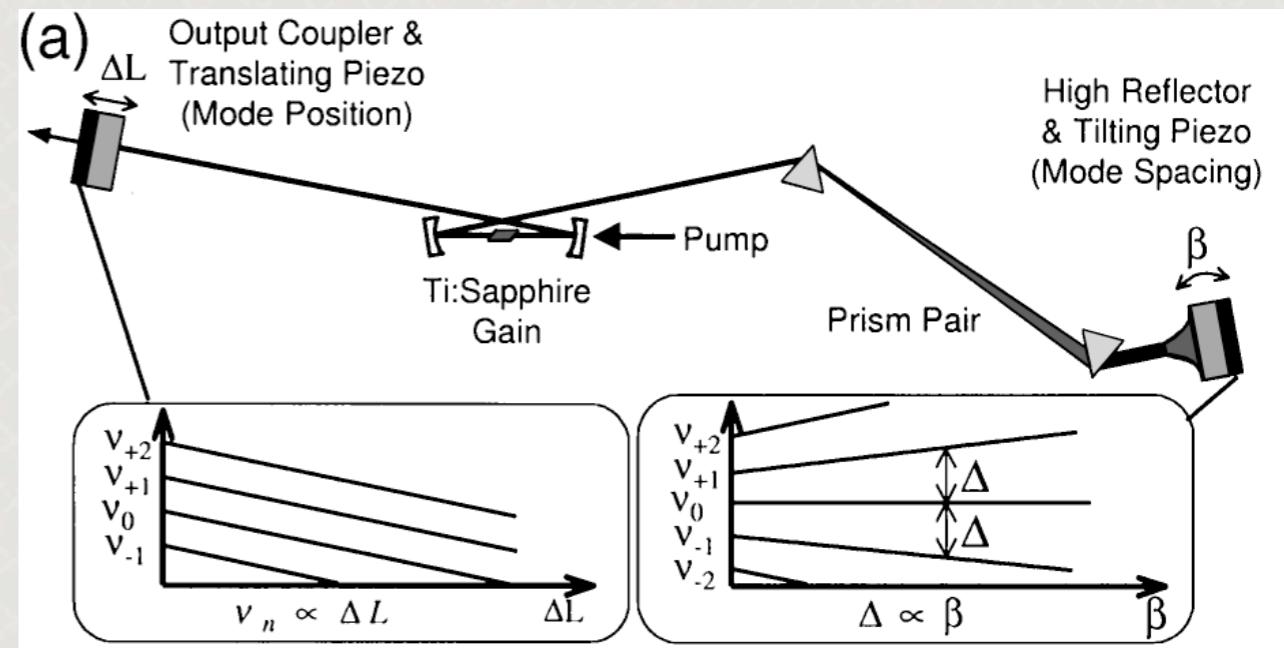


$$F_n = n \times F_r + F_o$$

Controlling F_r and F_o , F_n is fixed

Controlling Frequency of Mode-locked Laser

- Repetition frequency Fr , equal to longitudinal mode spacing, can be controlled via round-trip path length
- Controlling the phase revolution to fix offset frequency



J. Ye et al., Opt. Lett. 25, 1675 (2000)

Another Way to Control Offset Frequency

High intensity within the cavity of mode-locked laser



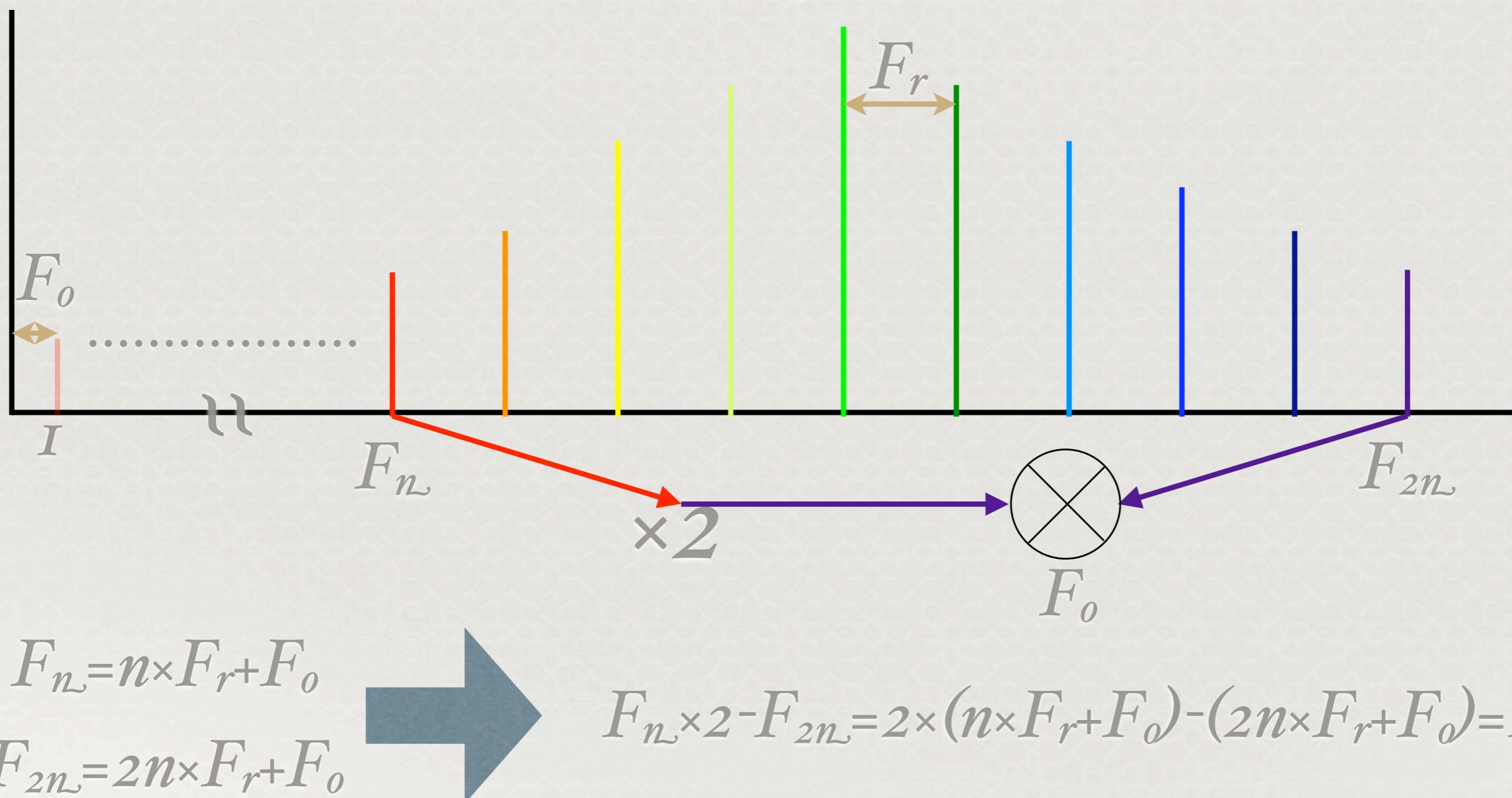
Optical Kerr Effect, $n=n_0+n_2I$



Change intracavity intensity to control the offset frequency

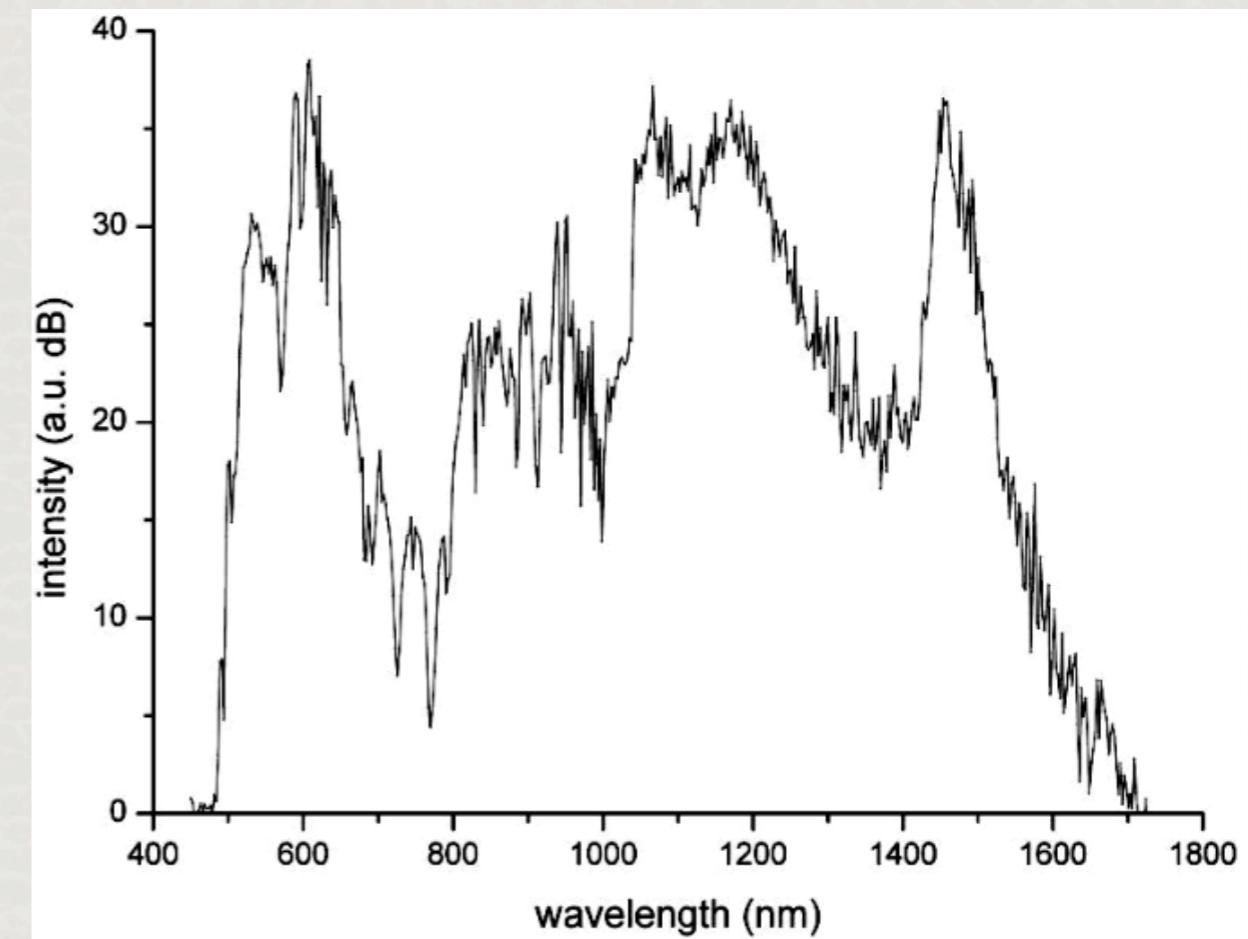
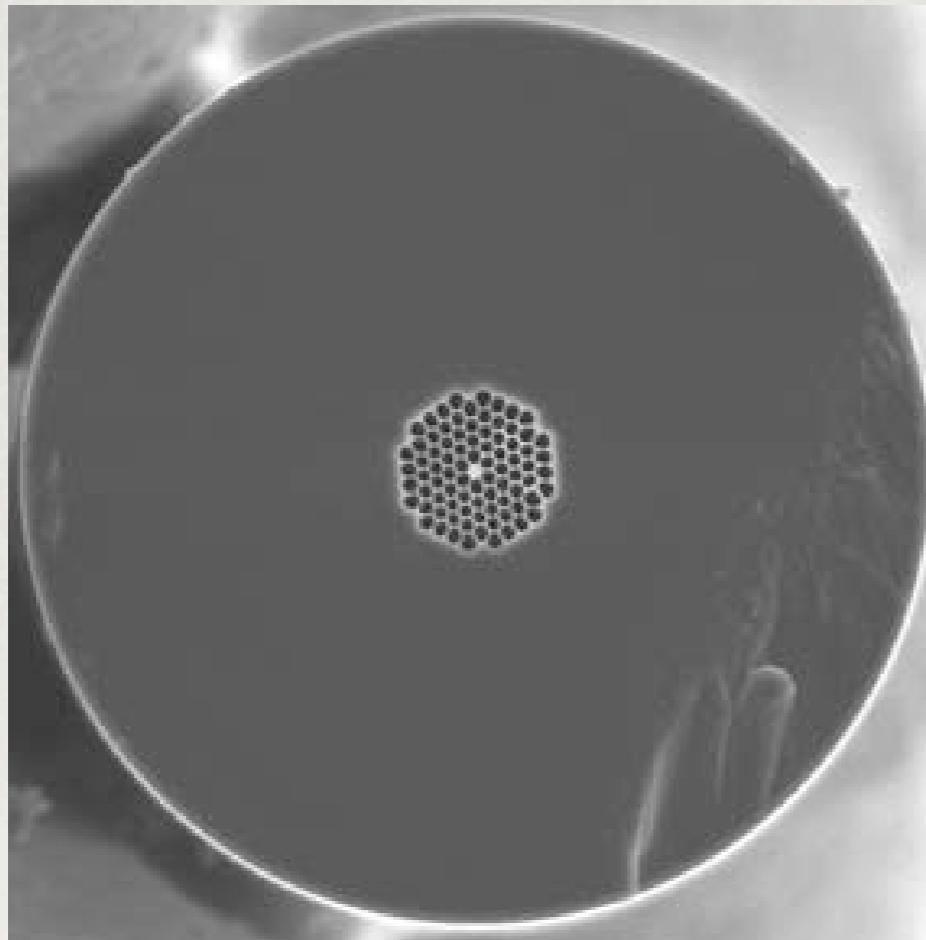
J. Stenger et al., Opt. Lett. 25, 1553 (2000)

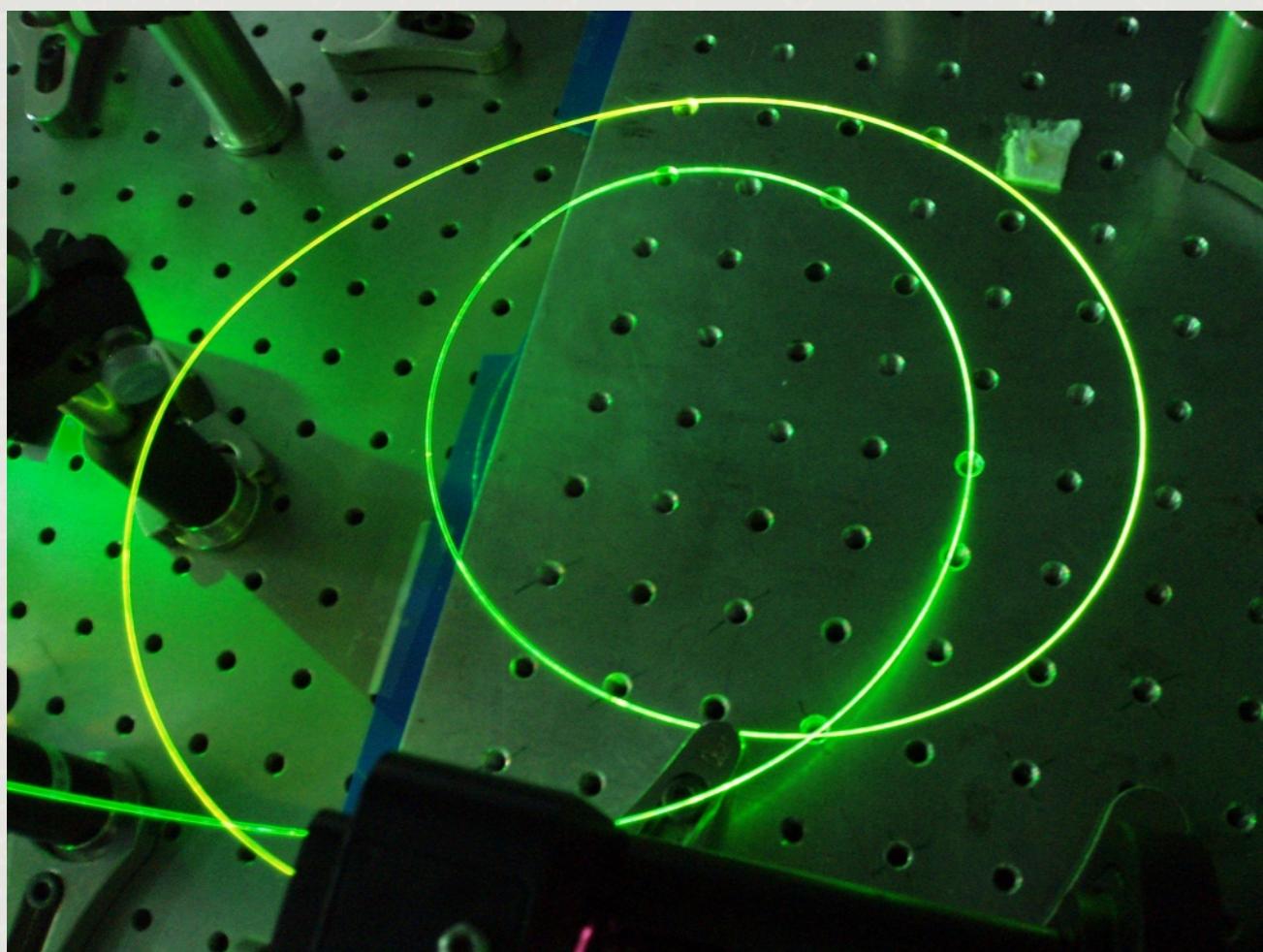
Detecting Offset Frequency: f-2f Self-Referencing



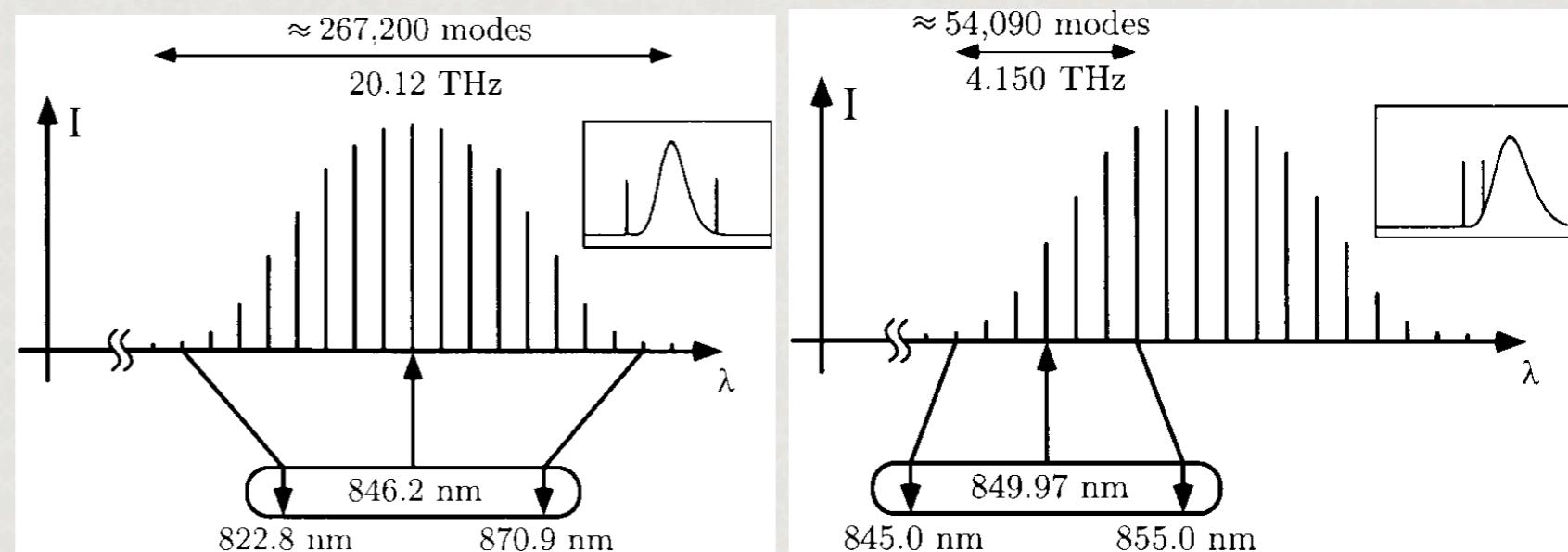
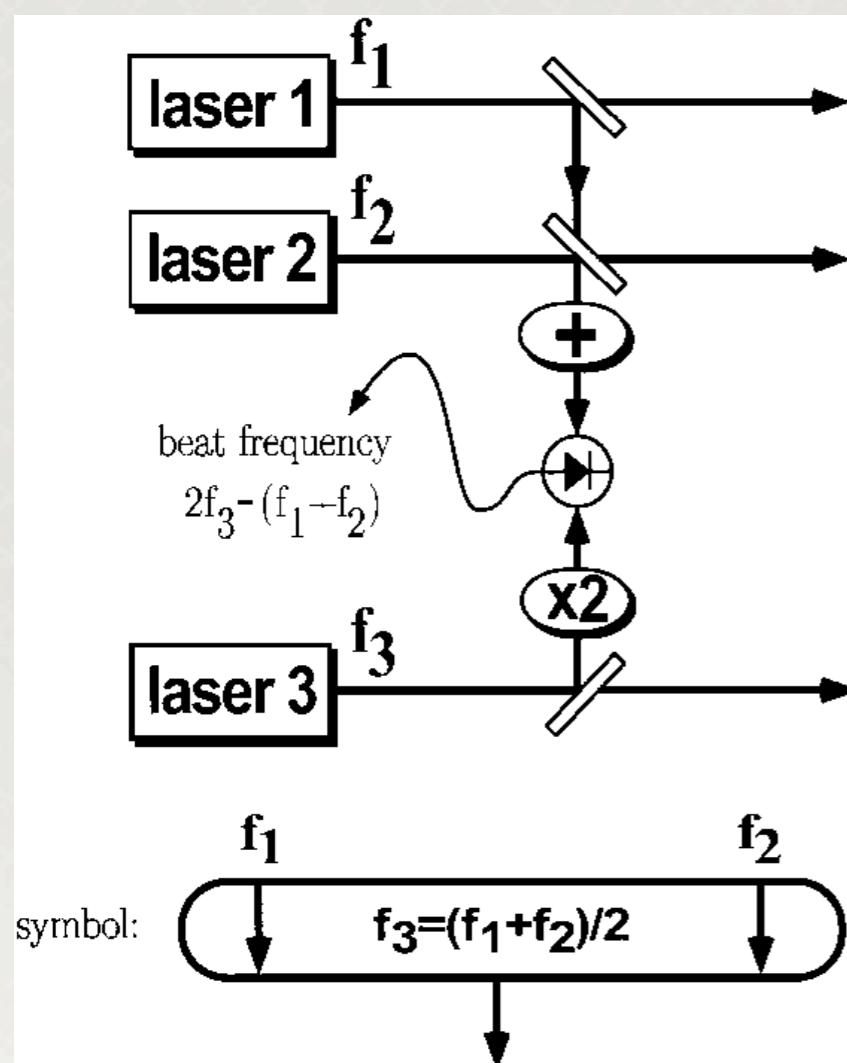
J. Reichert et al., Opt. Comm. 172, 59 (1999)

Spectrum Broadening via Microstructure Fiber





Uniformity of OFC Mode Spacing



Uniformity is within the experimental limit 6×10^{-16}

Th. Udem et al., Opt. Lett. 24, 881 (1999)

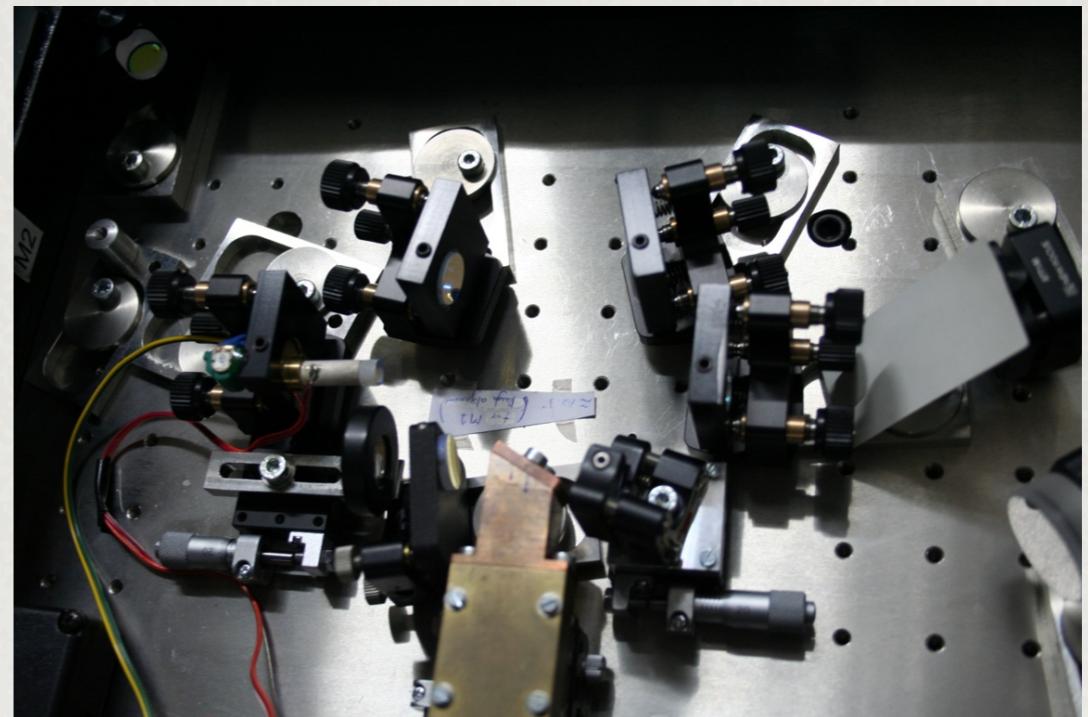
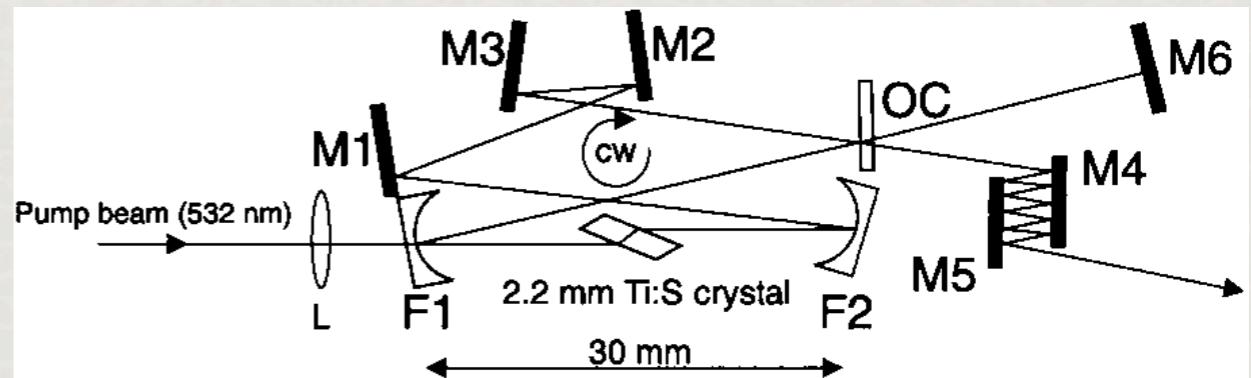
OFC in NTHU

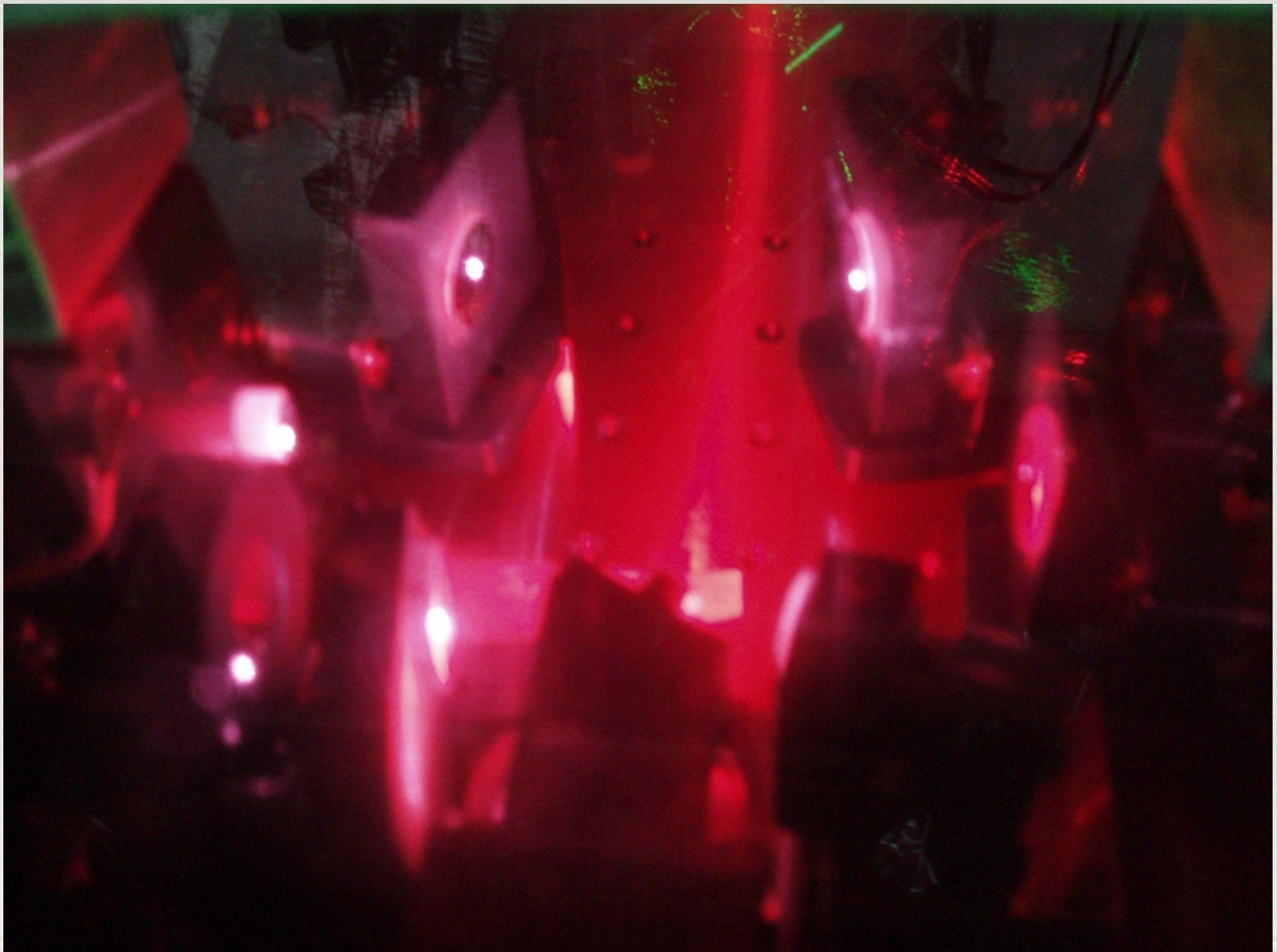
Brief of NTHU OFC

- ✿ *Based on 1 GHz repetition frequency Kerr-lens mode-locked Ti:sapphire laser*
- ✿ *Spectrum broadened by a polarization maintaining microstructure fiber; coverage: 500-1650 nm*
- ✿ *f-2f self-referencing scheme for offset frequency stabilization*

1-GHz KLM Laser

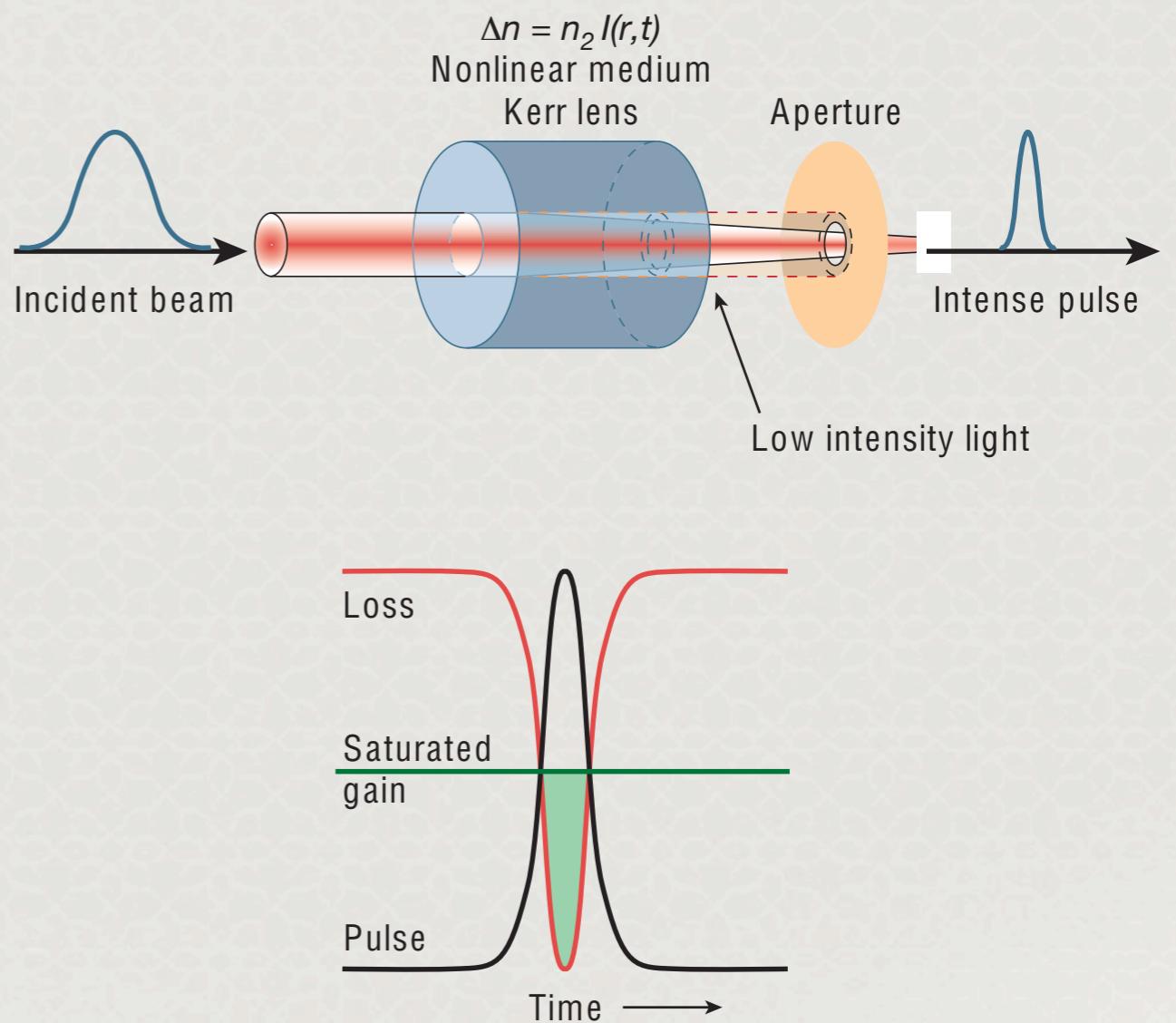
- ◆ *Ring cavity, soft aperture*
- ◆ *Chirped mirror dispersion compensation*
- ◆ *1 GHz repetition frequency*
- ◆ *> 730 mW @ 5 W 532 nm pumping, mode-locked operation*

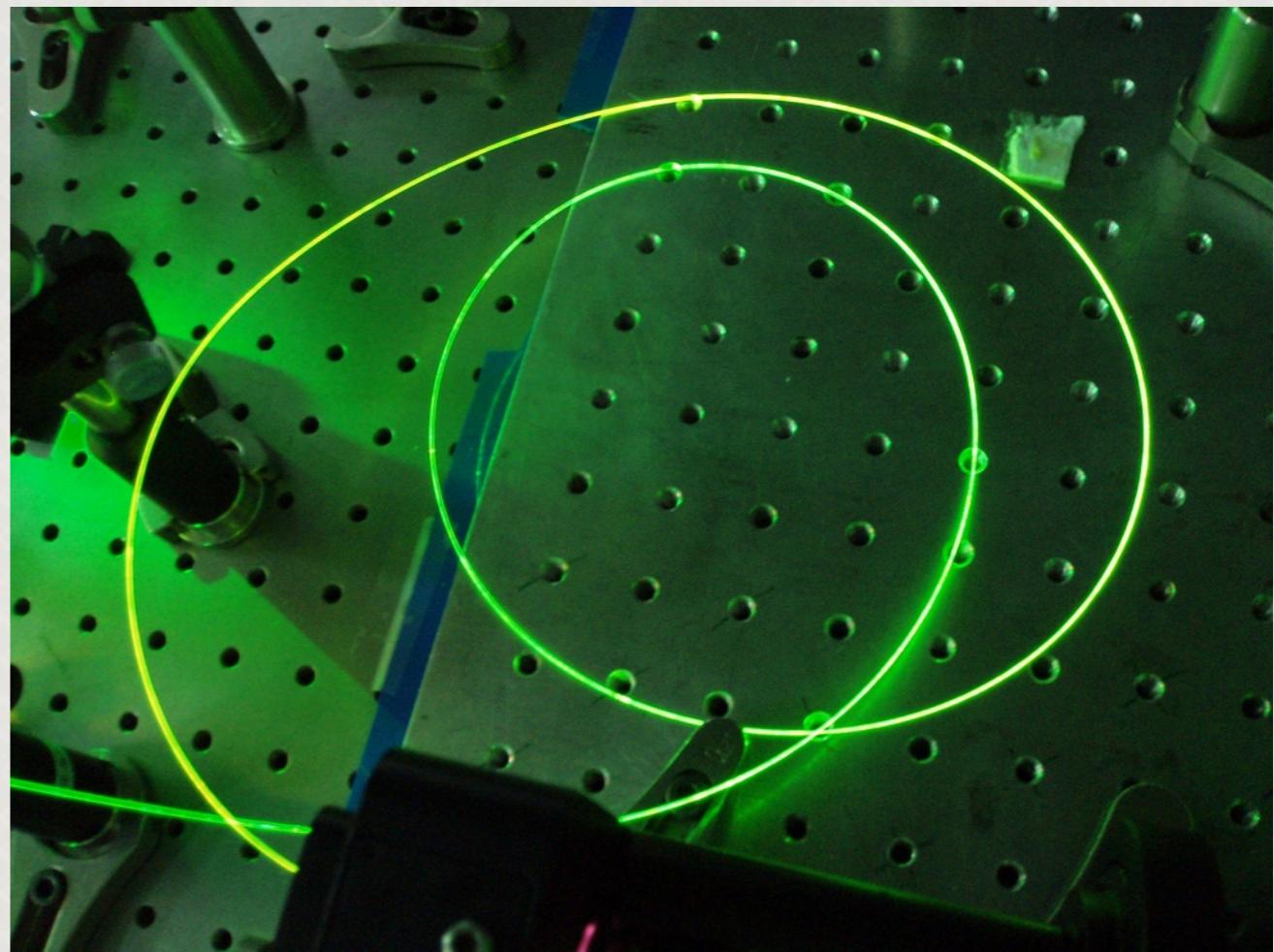
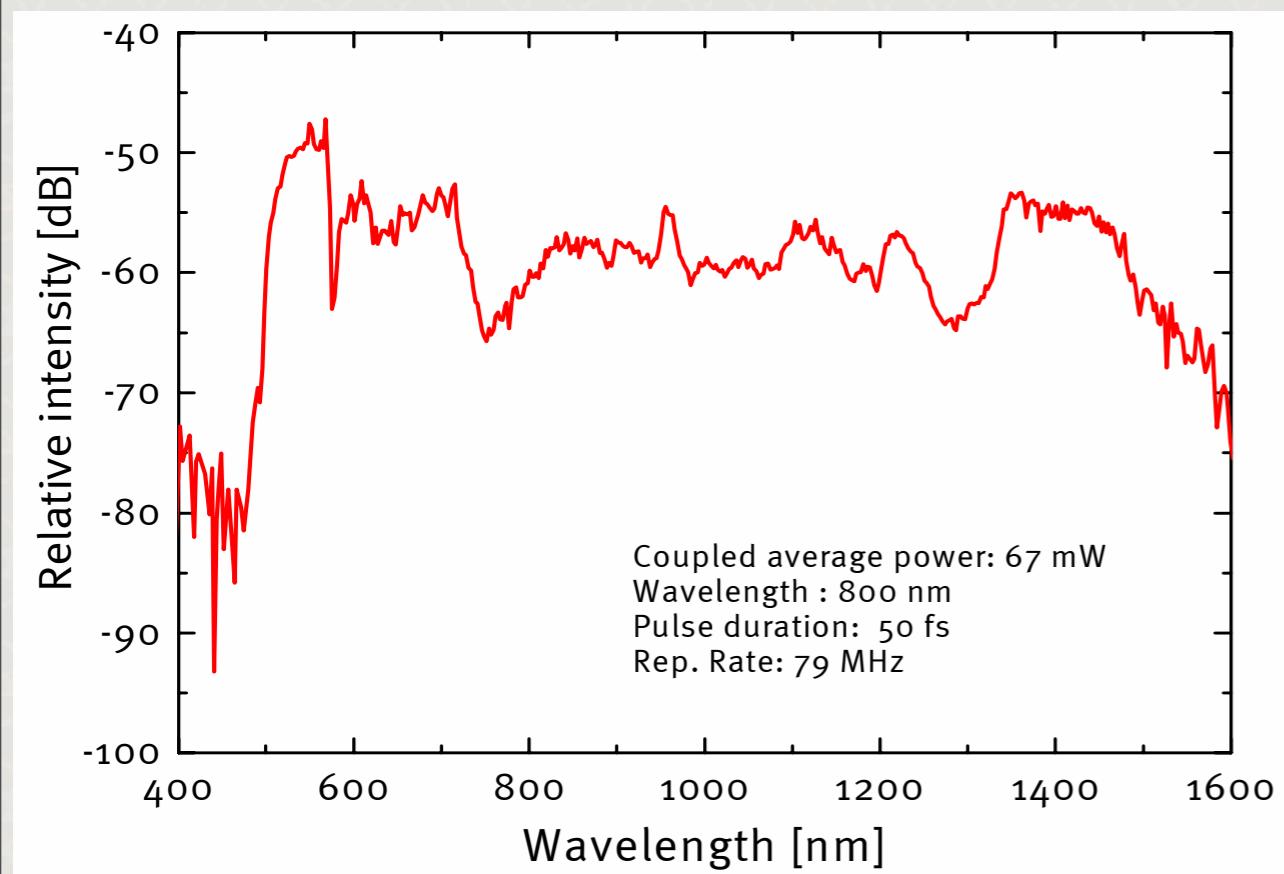




Kerr-lens Mode-locking

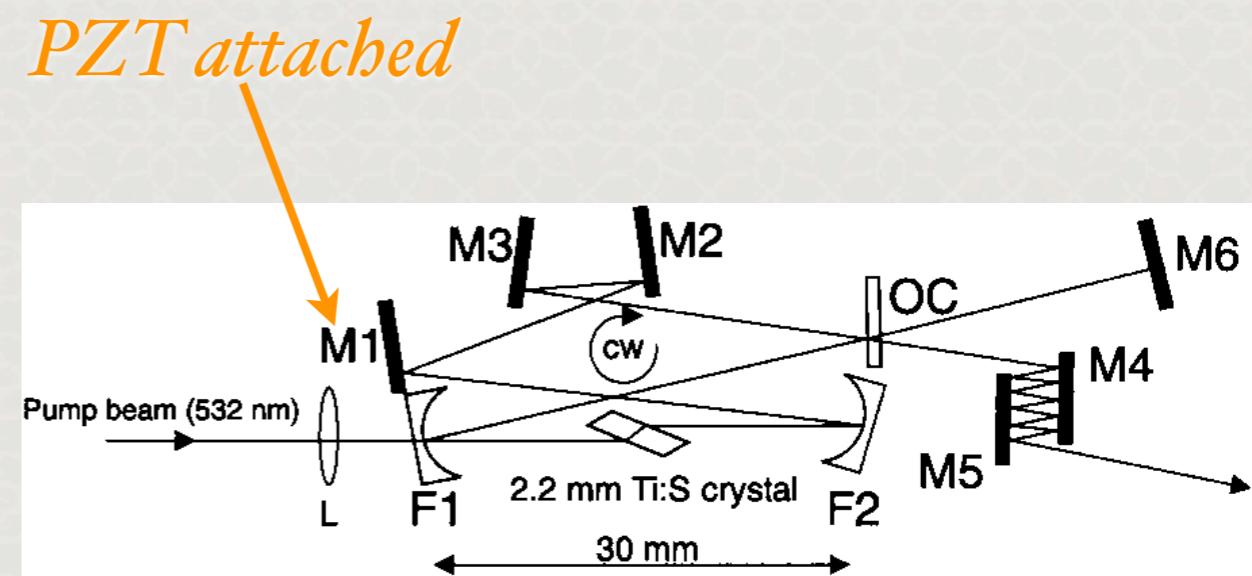
- ◆ *No mode-locking \rightarrow Weak Kerr effect \rightarrow High cavity loss \rightarrow Power decrease*
- ◆ *Mode-locking \rightarrow Strong Kerr effect \rightarrow Low cavity loss \rightarrow Power increase*
- ◆ *Kerr medium: Ti:sapphire laser crystal*
- ◆ *Aperture: Pump beam spot*





Control Repetition Frequency of OFC

- ◆ Detect the repetition frequency by fast silicon PD and lock the frequency to the signal from 1-GHz RF synthesizer by analog phase-locked loop
- ◆ PZT controls cavity length



Control Offset Frequency of OFC

- ◆ Detect the offset frequency via f_2f self-referencing scheme and lock the frequency to the frequency from low frequency synthesizer by digital phase-locked loop
- ◆ AOM controls pumping power

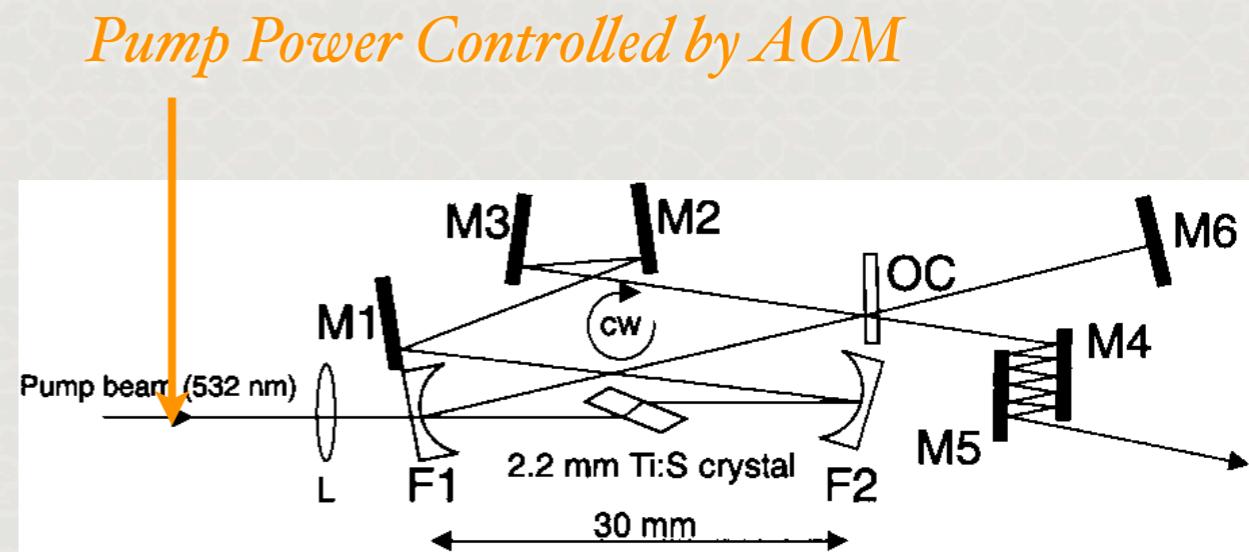
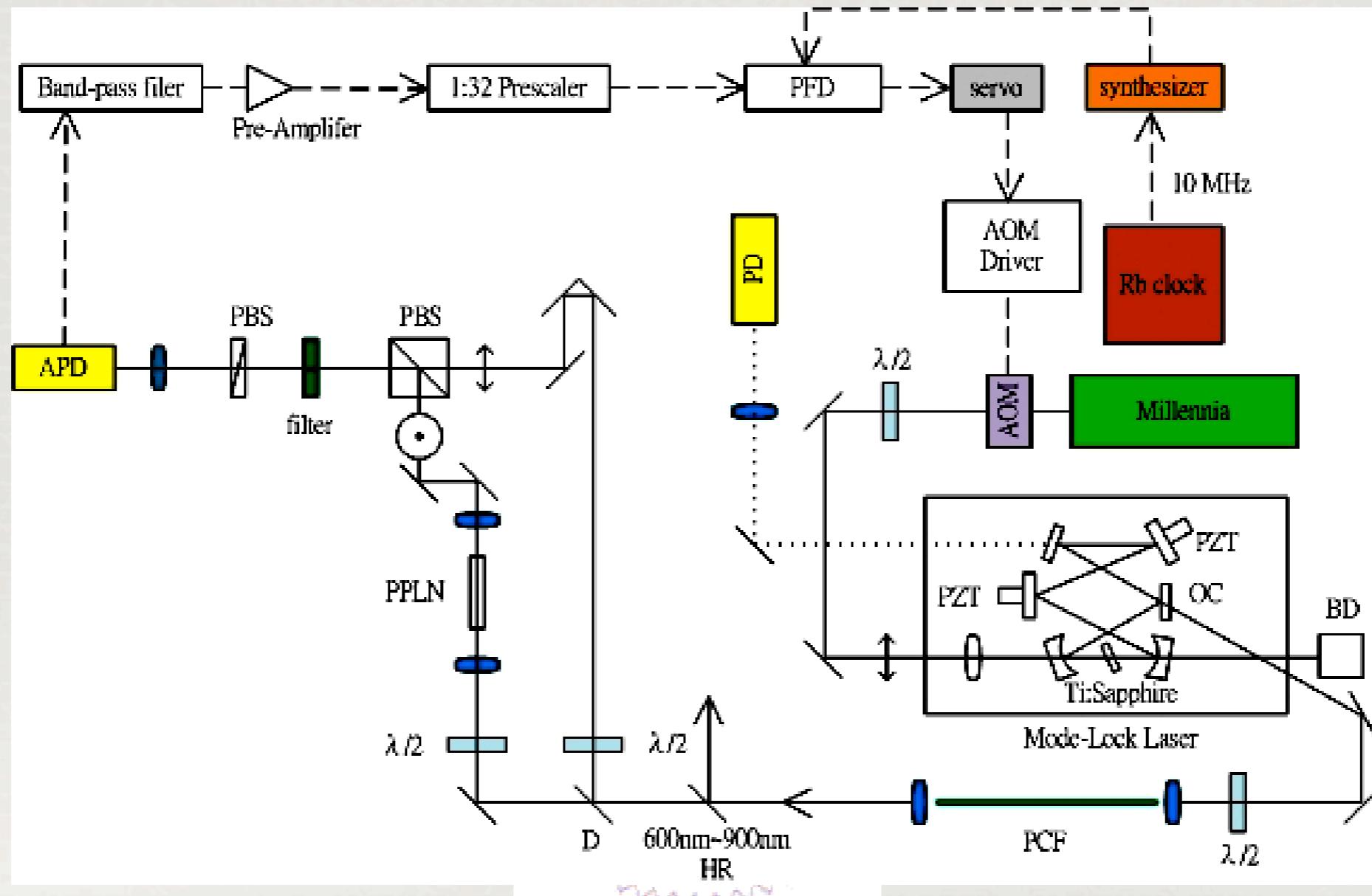


Diagram of NTHU OFC



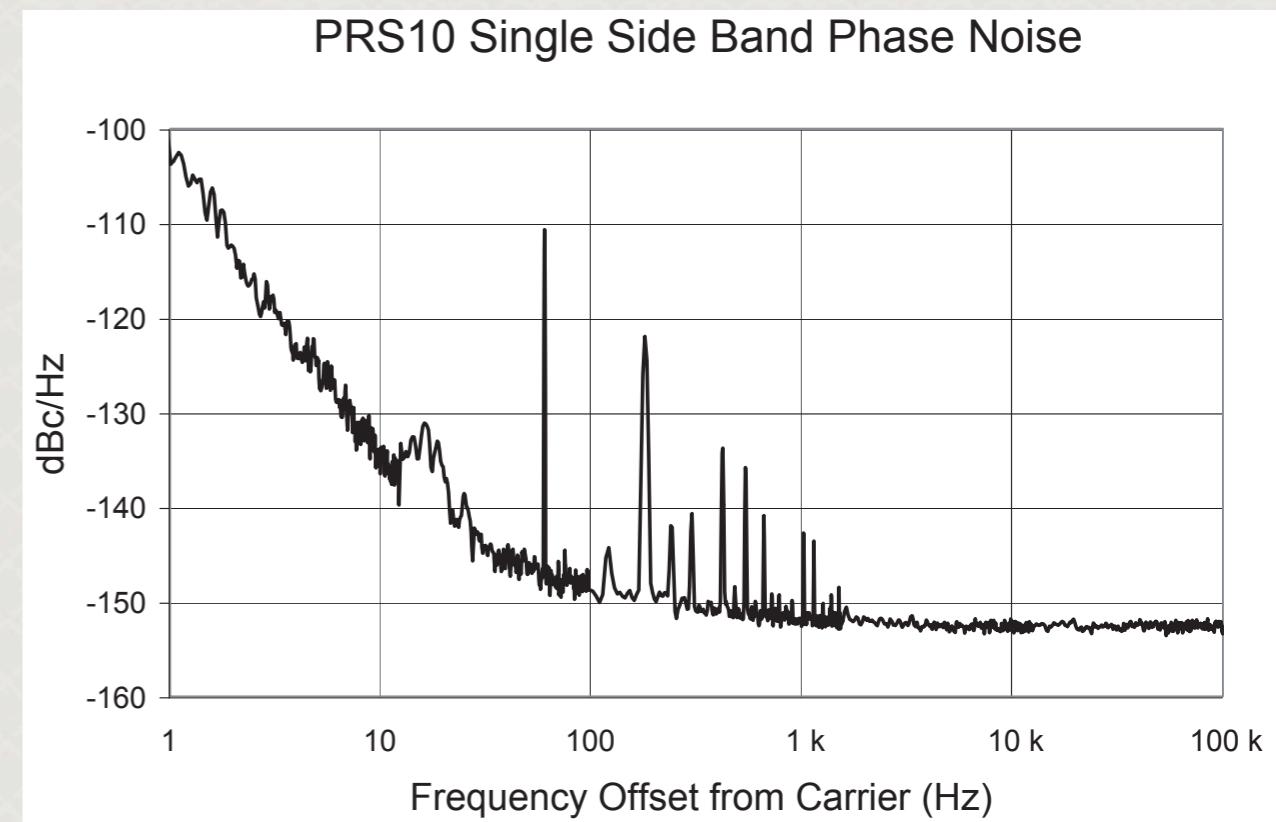
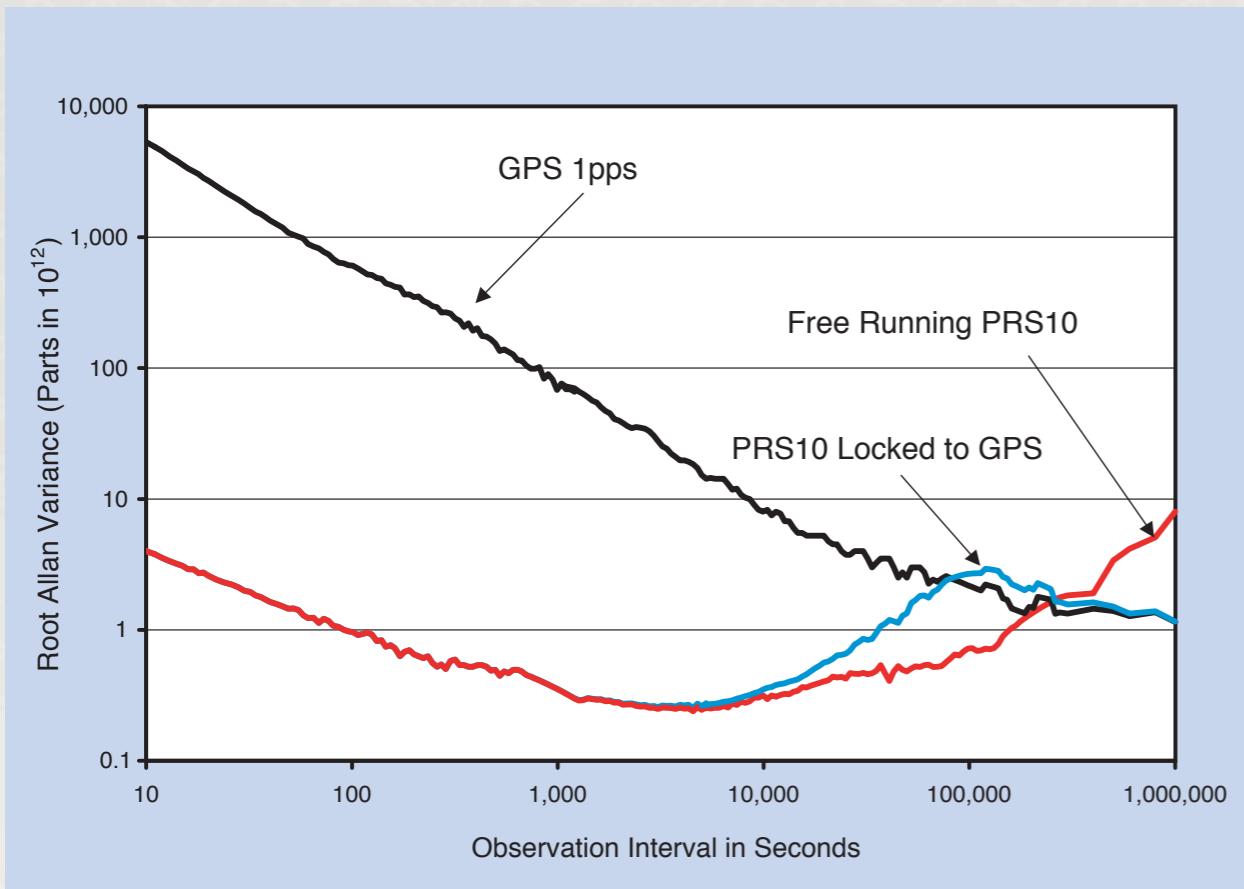
High Precision Local Oscillator

◆ *GPS Disciplined Rb Frequency Standard*

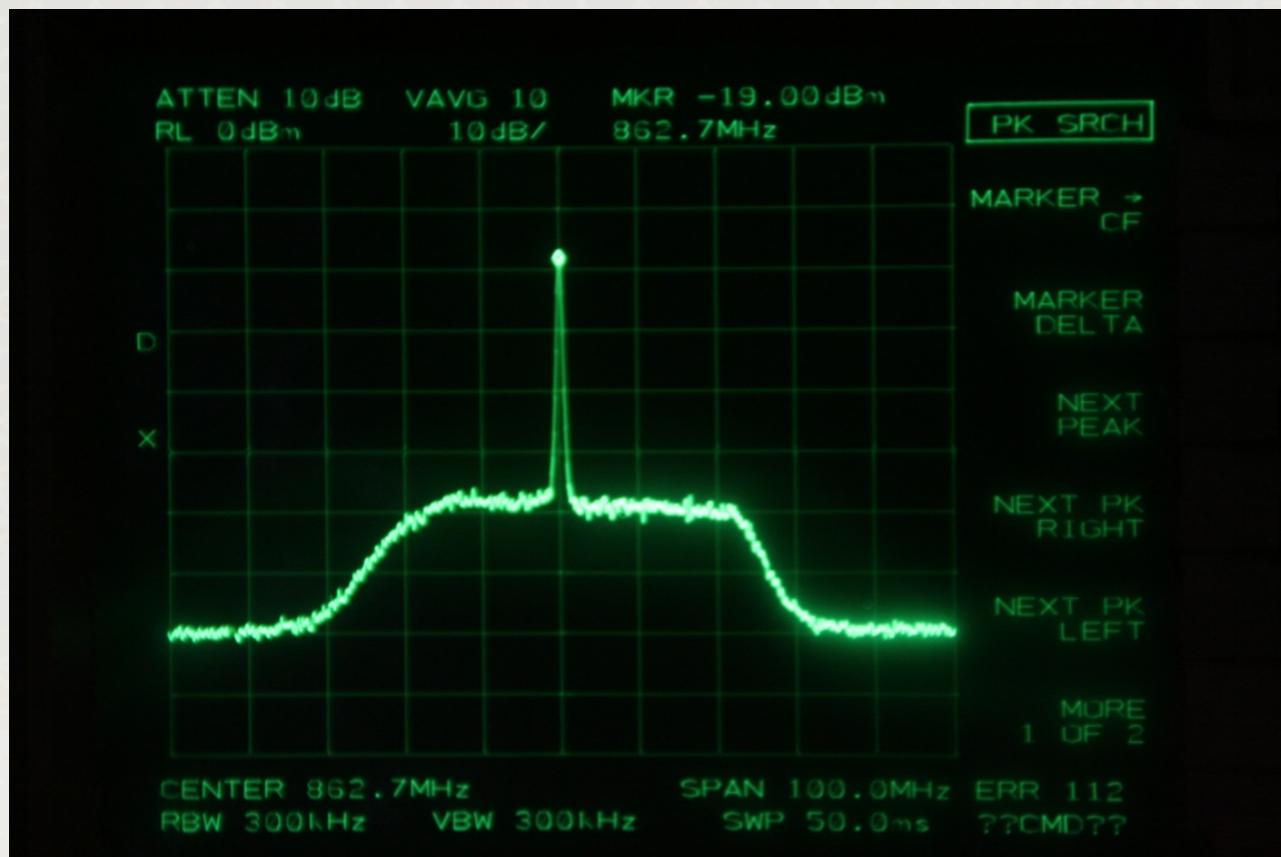
◆ *Allan variance:
 2×10^{-12} @ 1000 s*



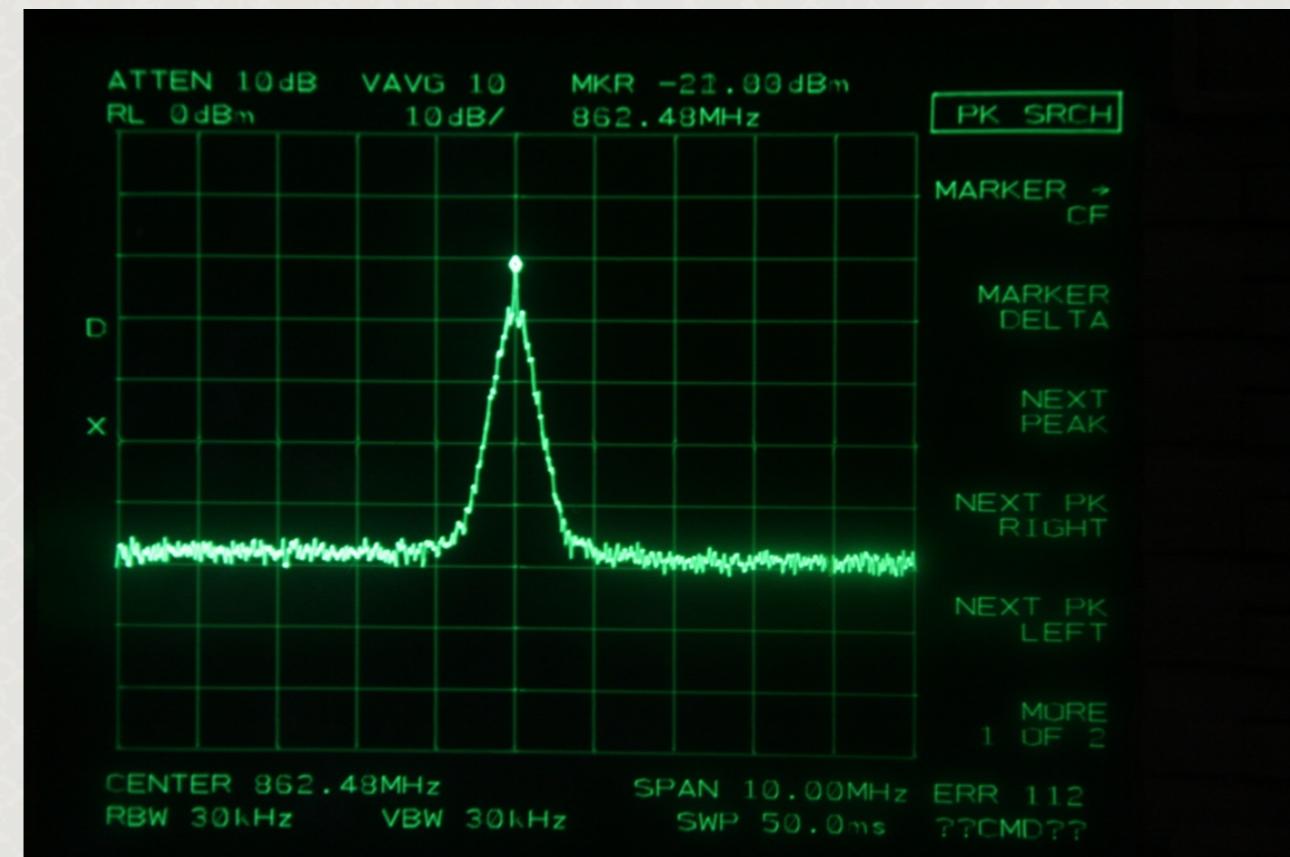
Performance of GPS Disciplined Rb Frequency Standard



Signal of Offset frequency



Span: 100 MHz



Span: 10 MHz

CO₂ Transitions Absolute Frequency Measurement

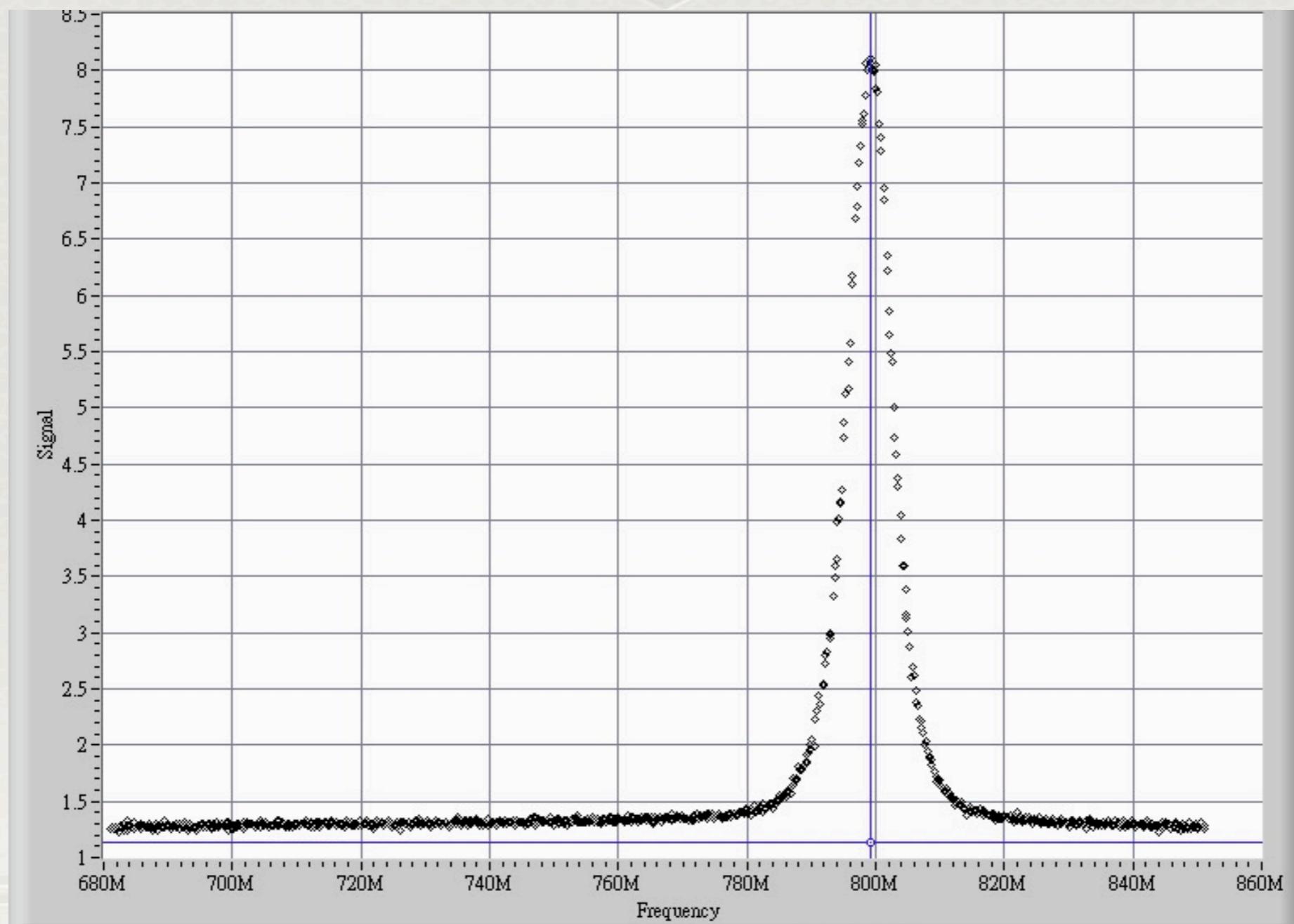
Table 4.4: Measured *P*-branch lines on (00⁰1-00⁰0) band

<i>P</i> branch line	Gas pressure (mTorr)	Present result (kHz)	HITRAN04 (MHz)	difference (kHz)
<i>P</i> (56)	40	68 834 038 921(15)	68 834 039(3)	-775
<i>P</i> (54)	40	68 900 642 151(11)	68 900 642(3)	-667
<i>P</i> (52)	40	68 966 529 482(10)	68 966 530(3)	-463
<i>P</i> (50)	30	69 031 700 054(9)	69 031 700(3)	-184
<i>P</i> (48)	30	69 096 152 910(9)	69 096 153(3)	81
<i>P</i> (46)	30	69 159 887 185(9)	69 159 887(3)	338
<i>P</i> (44)	30	69 222 902 134(9)	69 222 901(3)	652
<i>P</i> (42)	30	69 285 196 804(10)	69 285 196(3)	937
<i>P</i> (38)	30	69 407 621 923(9)	69 407 620(3)	1459
<i>P</i> (36)	2	69 467 750 707(9)	69 467 749(3)	1709
<i>P</i> (34)	2	69 527 155 865(11)	69 527 154(3)	1972
<i>P</i> (30)	2	69 643 791 832(10)	69 643 789(3)	2334
<i>P</i> (28)	2	69 701 020 989(10)	69 701 019(3)	2490
<i>P</i> (26)	2	69 757 523 218(12)	69 757 521(3)	2655
<i>P</i> (22)	2	69 868 343 412(10)	69 868 341(3)	2828
<i>P</i> (20)	2	69 922 659 782(9)	69 922 657(3)	3130
<i>P</i> (18)	2	69 976 245 898(12)	69 976 243(3)	2963
<i>P</i> (16)	2	70 029 101 083(14)	70 029 098(3)	3089
<i>P</i> (14)	2	70 081 224 268(12)	70 081 221(3)	3068
<i>P</i> (12)	2	70 132 614 878(10)	70 132 612(3)	3075
<i>P</i> (10)	2	70 183 272 067(10)	70 183 269(3)	3103
<i>P</i> (8)	2	70 233 195 001(10)	70 233 192(3)	3098
<i>P</i> (4)	2	70 330 835 136(10)	70 330 832(3)	3108
<i>P</i> (2)	30	70 378 550 790(10)	70 378 548(3)	3135

Table 4.5: Measured *R*-branch lines on 00⁰1 ← 00⁰0 band

<i>R</i> branch line	Gas pressure (mTorr)	Present result (kHz)	HITRAN04 (MHz)	difference (kHz)
<i>R</i> (62)	40	71 523 708 501(11)	71 523 709(3)	-386
<i>R</i> (60)	40	71 500 327 965(15)	71 498 830(3)	-620
<i>R</i> (58)	40	71 476 187 894(11)	71 476 189(3)	-710
<i>R</i> (56)	40	71 451 288 976(10)	71 451 290(3)	-695
<i>R</i> (54)	40	71 425 631 898(11)	71 425 632(3)	-516
<i>R</i> (52)	40	71 399 217 159(10)	71 399 217(3)	-331
<i>R</i> (50)	20	71 372 045 466(11)	71 372 046(3)	-125
<i>R</i> (48)	20	71 344 117 501(10)	71 344 117(3)	126
<i>R</i> (46)	20	71 315 433 898(9)	71 315 434(3)	365
<i>R</i> (44)	20	71 285 995 348(10)	71 285 995(3)	655
<i>R</i> (42)	20	71 255 802 495(10)	71 255 802(3)	920
<i>R</i> (40)	20	71 224 856 328(8)	71 224 855(3)	1489
<i>R</i> (38)	20	71 193 156 751(9)	71 193 155(3)	1577
<i>R</i> (36)	2	71 160 704 945(10)	71 160 703(3)	1705
<i>R</i> (34)	2	71 127 501 715(12)	71 127 500(3)	1928
<i>R</i> (32)	2	71 093 547 578(17)	71 093 545(3)	2135
<i>R</i> (30)	2	71 058 843 255(10)	71 058 841(3)	2327
<i>R</i> (28)	2	71 023 389 424(10)	71 023 387(3)	2462
<i>R</i> (26)	2	70 987 186 808(9)	70 987 184(3)	2603
<i>R</i> (24)	2	70 950 236 211(9)	70 950 233(3)	2776
<i>R</i> (22)	2	70 912 538 109(9)	70 912 535(3)	2826
<i>R</i> (20)	2	70 874 093 451(11)	70 874 091(3)	2953
<i>R</i> (18)	2	70 834 903 061(8)	70 834 900(3)	3262
<i>R</i> (16)	2	70 794 966 952(8)	70 794 964(3)	3016
<i>R</i> (14)	2	70 754 286 639(8)	70 754 284(3)	3040
<i>R</i> (12)	2	70 712 862 655(9)	70 712 860(3)	3119
<i>R</i> (10)	2	70 670 695 563(9)	70 670 692(3)	3095
<i>R</i> (8)	2	70 627 786 288(10)	70 627 783(3)	3145
<i>R</i> (6)	2	70 584 135 435(12)	70 584 132(3)	3093
<i>R</i> (4)	2	70 539 743 863(9)	70 539 741(3)	3109
<i>R</i> (2)	2	70 494 612 370(8)	70 494 609(3)	3212
<i>R</i> (0)	20	70 448 741 463(8)	70 448 738(3)	3130

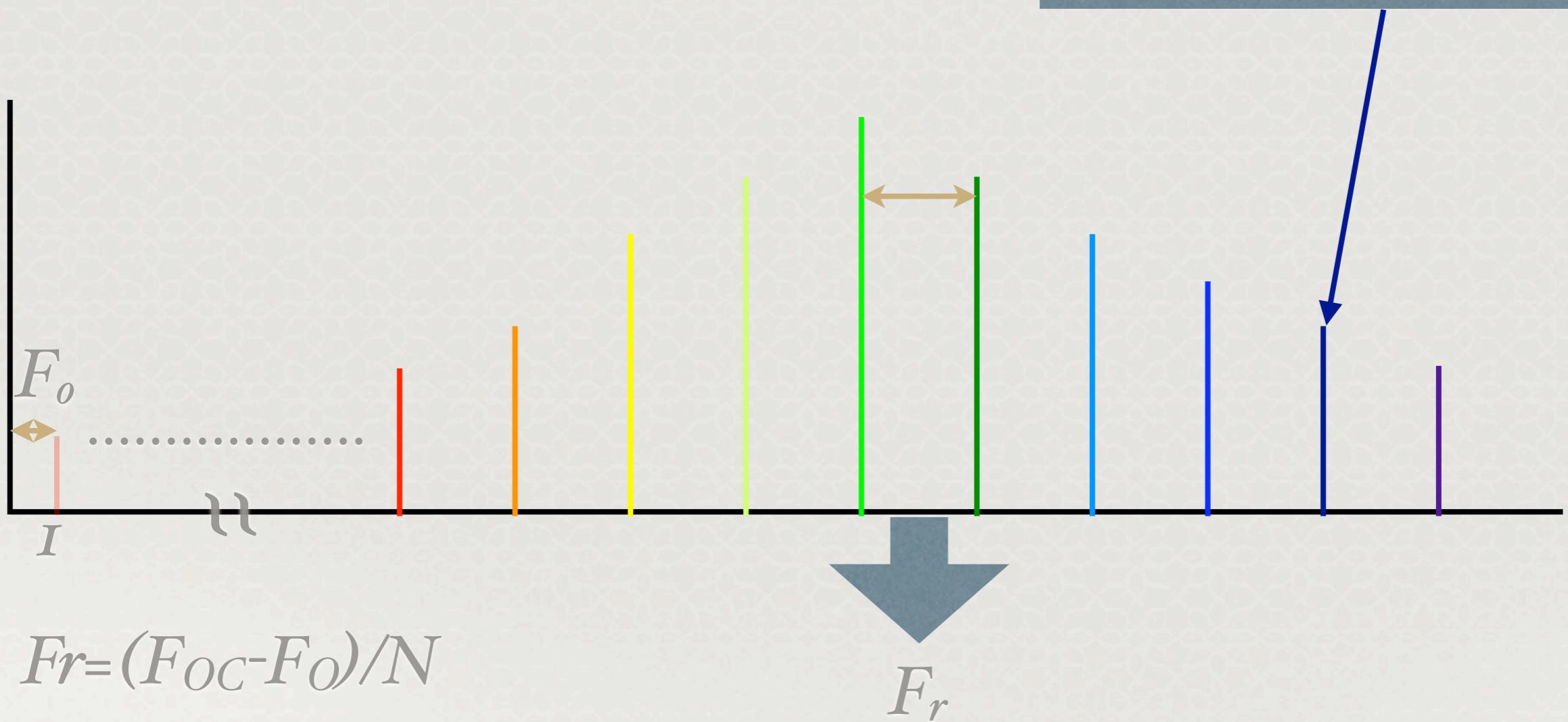
$^{6,7}\text{Li}$ 2S - 3S Two-photon Transitions



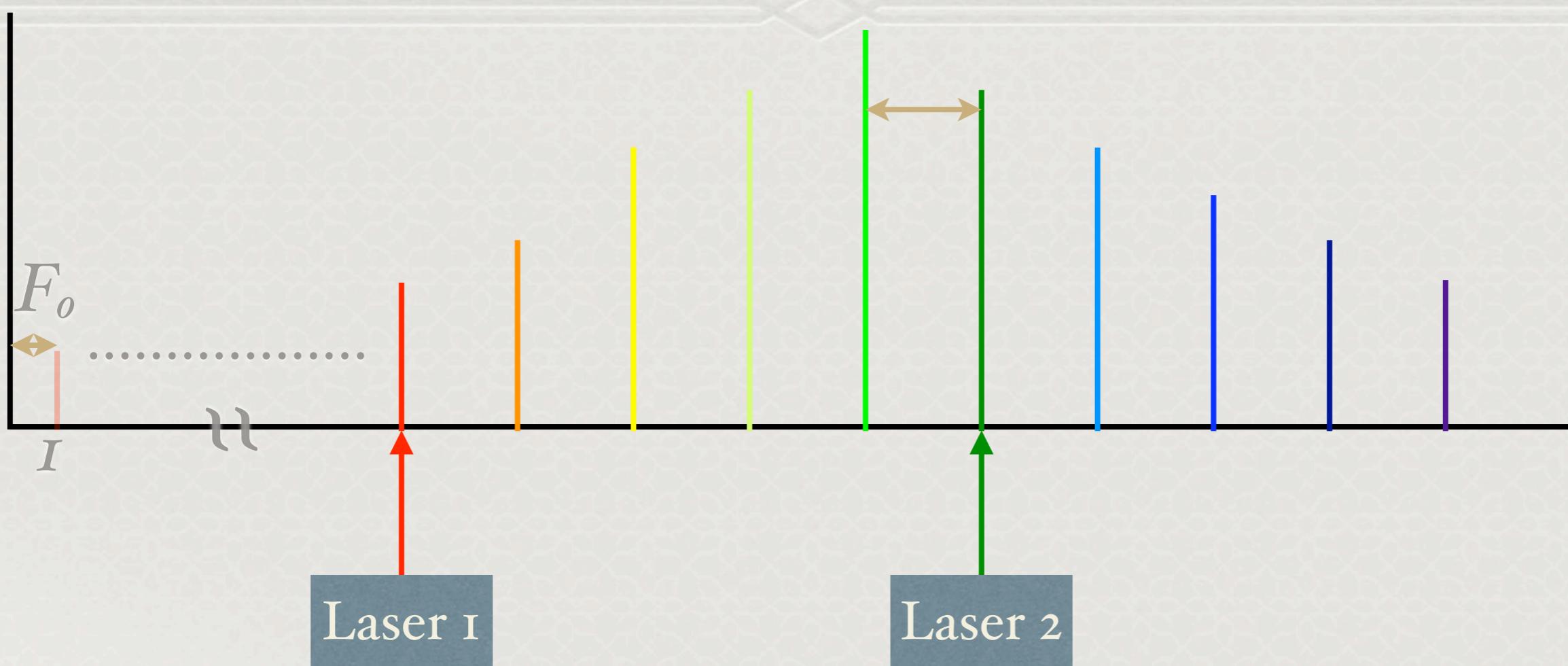
What can OFC do for us?

Optical Clock

Optical Clock Transition FOC



Coherence Link between Far Separated Lasers



Potential Applications: EIT, CARS, DFG, OPO

Direct Frequency Comb Spectroscopy (DFCS)

- ◆ *Direct absorption spectroscopy*
- ◆ *Cavity enhanced spectroscopy*
- ◆ *Cavity ringdown spectroscopy*
- ◆ *Two-photon spectroscopy*

References

- ◆ *Laser Physics at the Limits, Ed. by H. Figger, D. Meschede, and C. Zimmermann, Springer 2002*
- ◆ *Femtosecond Optical Frequency Comb: Principle, Operation and Applications, Ed. by J. Ye and S. T. Cundiff, Springer 2004*