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Topological Phase and Strong Correlation in Rare-Earth Hexaborides XB_6 (X = La, Ce, Pr, Nd, Pm, Sm, Eu)

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Abstract: The rare-earth hexaboride SmB_6 , known as the topological Kondo insulator, has attracted tremendous attention in recent years. It was revealed that the topological phase of SmB_6 is insensitive to the value of on-site Coulomb interactions (Hubbard U), indicating that the topological phase in SmB_6 is robust against strong correlations. On the contrary, the isostructural YbB_6 displays a sensitivity to the Hubbard U value. As U increases, YbB_6 transforms from topological Kondo insulator to trivial insulator, showing the weak robustness of the topological phase of YbB_6 against U. Consequently, the dependence of the topological phase on Hubbard U is a crucial issue in the rare-earth hexaboride family. In this work, we investigate the structural and electronic properties of rare-earth hexaboride compounds through first-principles calculations based on density functional theory. By taking the strong correlations into consideration using a wide range of on-site U values, we study the evolution of the topological phases in rare-earth hexaboride (XB_6 , X = La, X = L

Keywords: topological phase; strong correlation; Hexaboride; first-principles calculations; electronic structures

1. Introduction

The discovery of the topological phase in condensed matter paved the way to classify electronic states [1,2]. Topological insulators have been attracting world-wide extensive attention in recent research [3–6]. Three dimensional materials with time reversal symmetry and inversion symmetry may harbor a topologically nontrivial phase if a band gap and band inversion emerge owing to spin–orbit interaction (SOI) [7].

The rare earth hexaboride XB₆ crystallizes in the CaB₆-structure, as shown in Figure 1. Its lattice structure is similar to a body-centered cubic such as the CsCl-type lattice with Cs replaced by rare earth ions, and with Cl substituted by B₆ octahedra. The variety of the physical properties observed in these compounds is intriguing. For example, the application of LaB₆ has been paid attention due to its low work function, which is suitable for thermionic emission. LaB₆ is metallic and becomes superconducting at $T_C = 0.45$ K [8]. CeB₆ is considered as a Kondo system. CeB₆ presents an antiferro-quadrupolar ordering in the paramagnetic phase between $T_q = 3.3$ K (quadrupolar ordering temperature) and $T_N = 2.4$ K (Neel's Temperature) [9,10]. PrB₆ has been confirmed that negative quadrupolar pair interactions exist in the paramagnetic phase ($T_N = 6.9$ K) [11]. NdB₆ is a localized 4f

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system that orders ferro-magnetically at low temperatures [12]. SmB₆ is a well-known topological Kondo insulator [1,13,14]. EuB₆ orders ferro-magnetically below 15.1 K with a huge decrease of resistivity and a significant blue shift of the reflectivity plasma edge [15–17]. At 12.7 K, another phase transition takes place, which is observed as a broad peak in the specific heat or an anomaly in the resistivity [18]. GdB₆ is a localized 4f system with a ferromagnetic order at low temperatures [19]. YbB₆ is a topology Kondo insulator at low temperatures, and is a classical mixed valence narrow band gap semiconductor [1,20,21]. Structural studies are also presented in Ref. [22,23]. As reported in Ref. [1], the topological phase of YbB₆ is sensitive to the Hubbard U value. As U increases, YbB₆ transforms from topological Kondo insulator to trivial insulator, showing the weak robustness of the topological phase of YbB₆ against U.

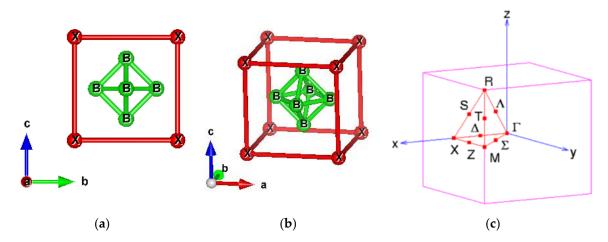


Figure 1. CsCl-type cubic crystal structure and Brillouin Zone of rare-earth hexaboride XB₆. (a) Side view. (b) Oblique view. (c) Brillouin Zone and high symmetry k-points.

In this study, the lattice structures of rare-earth hexaboride (XB_6 , X = La, Ce, Pr, Nd, Pm, Sm, Eu) are fully optimized through first-principles calculations. We then perform self-consistent field electronic structure calculations with and without SOI. To reveal the topological phases, we analyze if SOI would open up a continuous energy gap at the Fermi level with band inversion around the energy gap. To examine the robustness of the topological phase upon the strong correlation in XB_6 , we trace the evolution of its electronic structure by tuning the on-site U of the f electrons. We demonstrate that besides SmB_6 , PmB_6 , NdB_6 and EuB_6 are also topologically nontrivial compounds, while the others are topologically trivial normal metals.

2. Computational Details

First-principles calculations were performed using the Vienna Ab initio Simulation Package (VASP) with the Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional used in the generalized gradient approximation (GGA) as well as the GGA plus Hubbard U (GGA + U) schemes [24–27] based on density functional theory (DFT). The cut-off energy of 500 eV was adopted for the plane-wave basis. A Γ -centered 15 \times 15 \times 15 k-mesh was used in geometry optimization and self-consistent field calculations. The geometry optimization converged until all residual forces remained below 0.01 eV/Å. Table 1 compares the experimental lattice parameters of rare-earth hexaboride with our geometrically optimized ones. Good agreement between experimental and theoretical results can be found with deviations, in general, of less than 1%.

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Table 1. Experimental (exp) and theoretical (the) lattice parameters. The rare-earth hexaboride crystalizes in a bcc-like structure with space group of $Pm\overline{3}m$ (No. 221), in which metal ions are located at the Wyckoff position 1a(0,0,0) and octahedral B_6 at the Wyckoff position 6f(1/2,1/2,z). The subscripts "exp" and "the" indicate experimental and theoretical results, respectively.

	a _{exp} (Å)	a _{the} (Å)	Error of a	B(z) _{exp}	B(z) _{the}	B–B Bond Length _{exp} (Å)	B–B Bond Length _{the} (Å)
LaB ₆ [15]	4.1527	4.1553	0.06%	0.1993	0.1997	1.7660	1.7647
CeB ₆ [16]	4.14	4.1130	-0.65%	0.1992	0.1984	1.7611	1.7543
PrB ₆ [22]	4.13	4.1024	-0.67%	0.2	0.1984	1.7522	1.7498
NdB_{6} [16]	4.127	4.1007	-0.64%	0.1989	0.1987	1.7574	1.7473
PmB ₆ [23]	4.128	4.1131	-0.36%	0.2	0.1990	1.7514	1.7508
SmB ₆ [28]	4.1346	4.1087	-0.63%	0.2018	0.1993	1.7436	1.7474
EuB ₆ [29]	4.1849	4.1325	-1.25%	0.2027	0.1999	1.7595	1.7539
YbB ₆ [29]	4.1444	4.1325	-0.29%	0.207	0.2007	1.7173	1.7492

3. Results and Discussion

3.1. Topologically Trivial Normal Metal LaB₆, CeB₆, and PrB₆

Figure 2a,b show the PBE band structures of LaB₆ without and with SOI, respectively. The atom-orbital decomposition demonstrates that the valence bands below -1.5 eV are mainly composed of B-p orbital, while the conduction La-f bands (blue curves) are located mainly from 0.5 eV to 2.5 eV above the Fermi level (E_f). In between, there is a dispersive band composed of La-d orbital connecting the valence and conduction bands, resulting in an overall semimetal character. This in-gap La-d band also gives an electron pocket at E_f along Γ M. A comparison of band structures without SOI (a) and with SOI (b) shows that the SOI in LaB₆ is weak and has no significant effect on band structure. Consequently, the semimetal character remains as SOI is included. Without any continuous gap, LaB₆ is therefore a topologically trivial normal metal. On the other hand, the band structures remain more or less the same when the on-site Coulomb repulsion U is taken into account for the strong correlation in f orbitals, as can be seen in Figure 3. This constitutes preassembly, owing to the empty f states that have no effect near E_f.

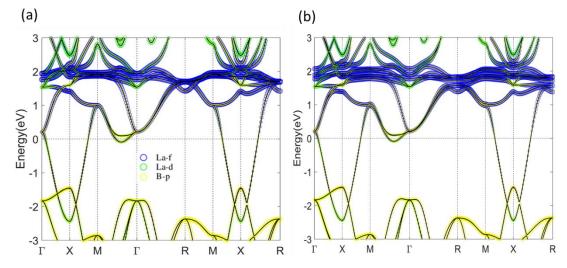


Figure 2. Atom-orbital decomposed band structure of LaB₆ calculated using Perdew–Burke–Ernzerhof (PBE) functional without spin–orbit interaction (SOI) (**a**) and with SOI (**b**). The size of blue, green and yellow circles indicates components from La-f, La-d and B-p orbitals, respectively.

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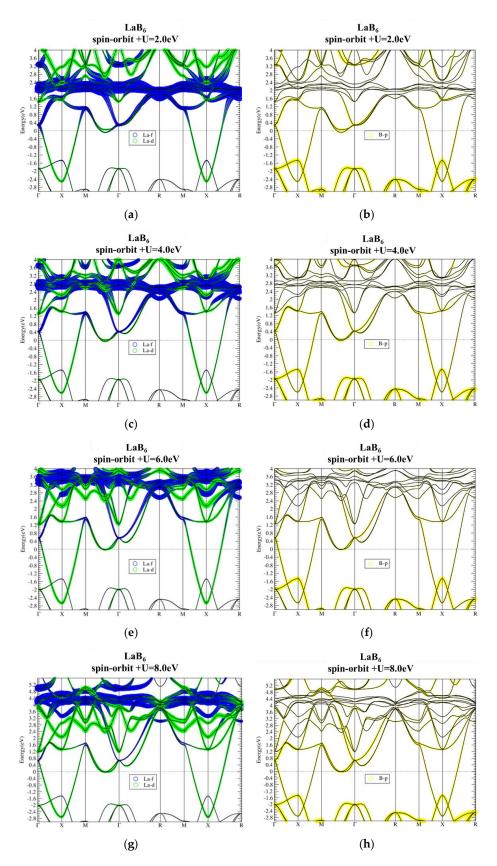


Figure 3. Atom-orbital decomposed band structures of LaB₆ with on-site $U = 2 \text{ eV } (\mathbf{a}, \mathbf{b})$, $4 \text{ eV } (\mathbf{c}, \mathbf{d})$, $6 \text{ eV } (\mathbf{e}, \mathbf{f})$, and $8 \text{ eV } (\mathbf{g}, \mathbf{h})$.

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With one more electron than La, the Fermi level of CeB_6 is thus raised up to the bottom of Ce-f bands, as shown in Figure 4. The flat Ce-f conduction bands are located around E_f from 0.6 eV below to 1.2 eV above E_f . As shown in Figure 5, for all the four cases with U=2, 4, 6, 8 eV studied, there are no significant changes in band structures. Similar to LaB_6 , CeB_6 is also insensitive to the on-site U values. Although the SOI is included in the calculations and the degeneracy at M is lifted by SOI, there is no continuous gap in all cases, leading to topologically trivial normal metal ground state for CeB_6 .

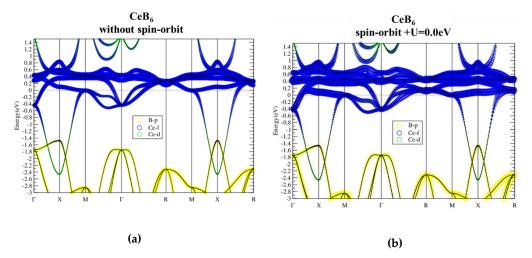


Figure 4. Band structure of CeB₆ without (a) and with (b) spin-orbit interaction.

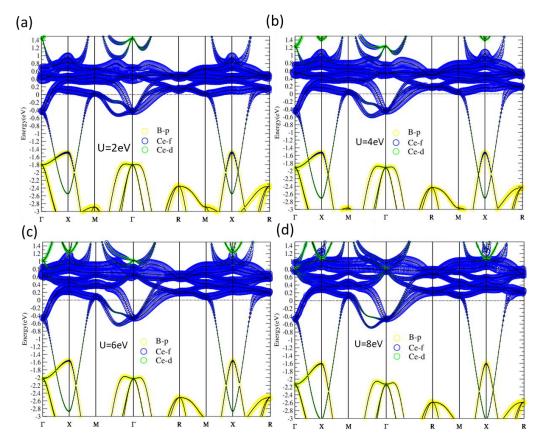


Figure 5. (\mathbf{a} – \mathbf{d}) CeB₆ band structures given from PBE + SOI + U with U = 2, 4, 6, 8 eV, respectively. The sizes of blue, green and yellow circles indicate components from Ce-f, Ce-d and B-p orbitals, respectively.

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Elementary Pr has three electrons occupying the f-orbitals in the ground state. Therefore, in PrB_6 the Pr-f conduction band is occupied by one more f electron than CeB_6 through the rigid-band shift, as shown in Figure 6. The band dispersions remain similar with different on-site U values. However, because the Fermi level is raised to the middle of the Pr-f conduction band, on-site U affects the bandwidth more significantly than that in the previous two species. With U = 8.0 eV, the f bandwidth is enhanced by about 0.5 eV. On the other hand, gapless ground state remains in PrB_6 even when the SOI is taken into consideration. Consequently, the same as LaB_6 and CeB_6 , PrB_6 is also a topologically trivial normal metal.

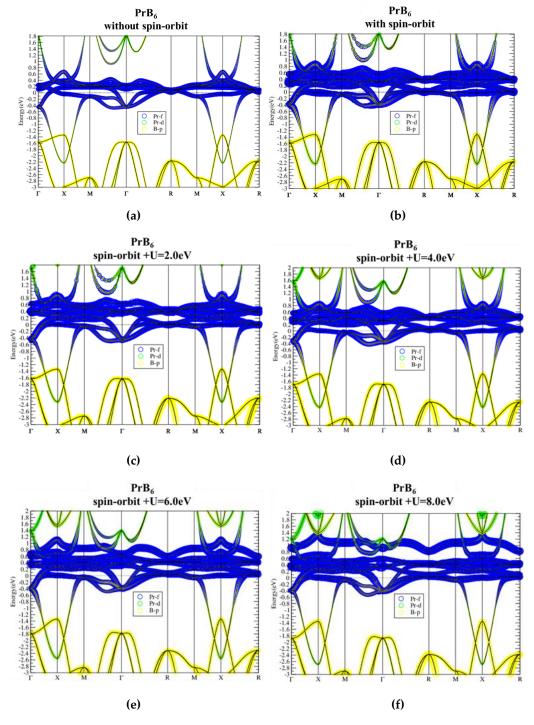


Figure 6. PrB_6 band structure without (a) and with (b) spin-orbit interaction (noted in the figures), and with spin-orbit interaction plus on-site U = 2, 4, 6, 8 eV (c-f, respectively) as noted in the figures.

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3.2. Topologically Nontrivial Kondo Insulator SmB₆, PmB₆, NdB₆ and EuB₆

Figure 7 shows our calculated band structures of the well-known topological Kondo insulator. The relatively flat La-f bands locate around Ef, with a much more dispersive La-d band crossing all these f bands. The spin–orbit interaction splits the f bands and opens up a continuous energy gap (see Figure 8) with band inversion between Sm-f/d characters flipping around the SOI-induced gap. These results agree well with those presented in previous works [1]. Band structures of SmB $_6$ with SOI and on-site U ranging from 2 to 8 eV are shown in Figure 9. There are no significant changes in band structures due to all the different U values used. Similar to previous study, the SOI-induced band gap and the band inversion behavior remain, indicating the robust topological phase against strong correlations in SmB $_6$.

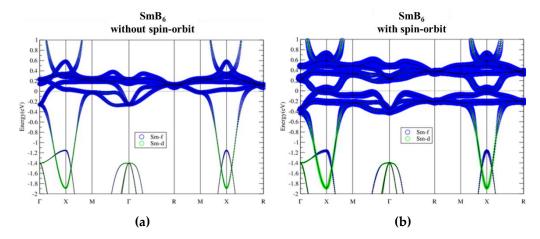


Figure 7. Band structures of SmB₆ without (**a**) and with (**b**) spin-orbit interaction projected by f and d electrons of Sm.

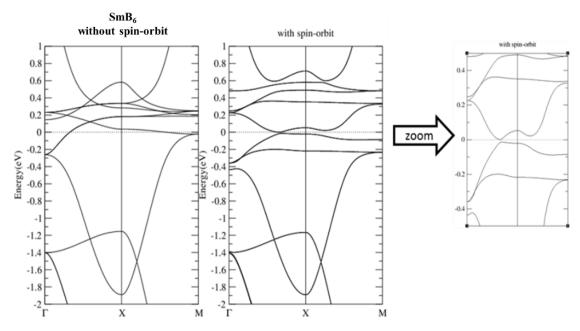


Figure 8. Band structure of SmB_6 without and with spin-orbit coupling. The right panel is the zoom-in view of the middle panel around E_f .

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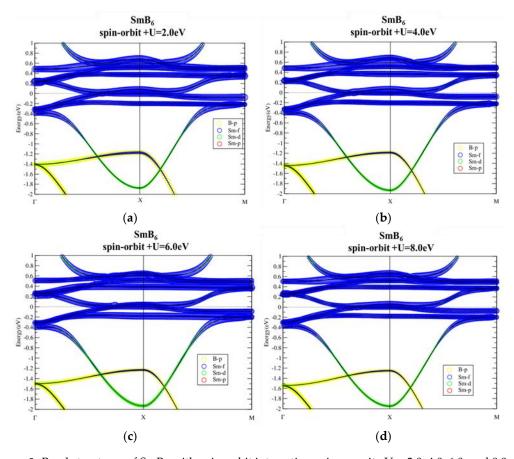


Figure 9. Band structures of SmB₆ with spin–orbit interaction using on-site U = 2.0, 4.0, 6.0, and 8.0 eV (a–d, respectively) projected by f and d electrons of Sm.

In comparison with the well-known topological Kondo insulator SmB_6 , the overall band dispersion of PmB_6 as shown in Figure 10 is similar to those of SmB_6 (Figures 7–9). Since PmB_6 has one less valence electron than SmB_6 , the Fermi level of PmB_6 is relatively lower than that of SmB_6 . With SOI taken into consideration, PmB_6 opens up a continuous gap around Ef, as shown in Figure 10b,d. In addition, there is a band inversion around Ef0 point with Ef1 pand Ef2 point with Ef3 around Ef4. Therefore, Ef4 pmB6 can host topological nontrivial state, giving rise to the topological Kondo insulator similar to Ef5. The electronic structure of Ef6 around Ef7 is not sensitive to various Ef8. The overall topological properties, indicating the topological phase is robust in Ef3 against strong correlations.

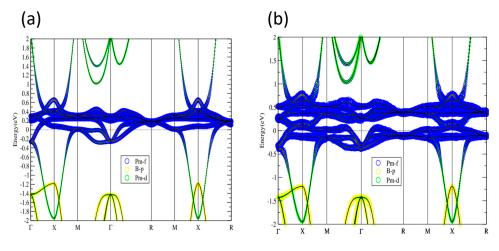


Figure 10. Cont.

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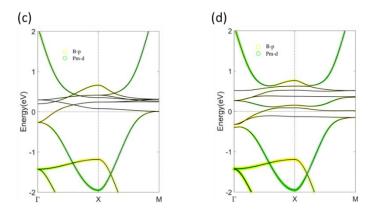


Figure 10. PBE band structure of PmB₆ without SOI (**a**) and with SOI (**b**). The size of blue, green and yellow circles show contributions from Pm-f, Pm-d and B-p orbitals, respectively. (**c**) Zoom-in of (**a**). (**d**) Zoom-in of (**b**). (**c**,**d**) demonstrate SOI-induced band inversion and gap opening.

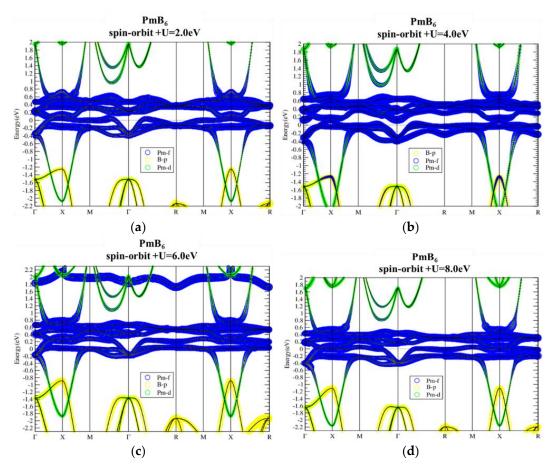


Figure 11. Band structures of PmB_6 with SOI and U = 2, 4, 6, 8 eV (**a–d**, respectively). As U is tuned larger, the highest f band is lifted but the band property is not changed near the Fermi level.

Band structures of NdB_6 as shown in Figure 12 also demonstrate topologically nontrivial phase. The SOI not only opens up a continuous energy gap around E_f but also gives rise to band inversion around X point. Similar to PmB_6 , the electronic structure and topological behavior of NdB_6 near the Fermi level are insensitive to on-site U value, as can be seen in Figure 13. Only the highest unoccupied f band is noticeably modified by U, which is irrelevant to its topology. Consequently, NdB_6 is also a topological Kondo insulator.

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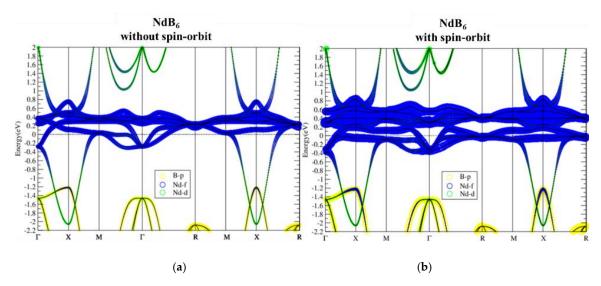


Figure 12. Band structures of NdB₆ without (a) and with (b) spin-orbit interaction.

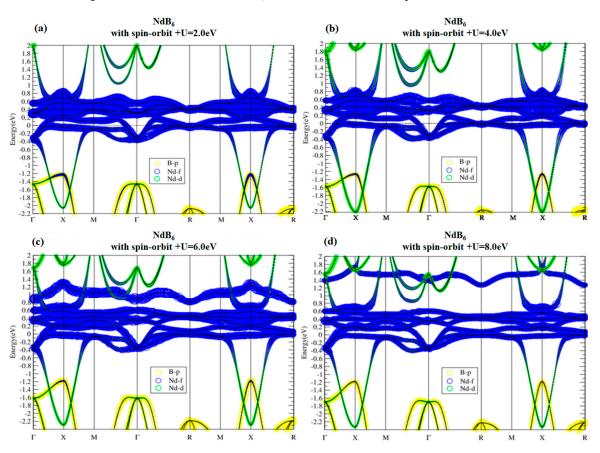


Figure 13. Band structures of NdB₆ with SOI using U = 2, 4, 6, and 8 eV (**a**–**d**, respectively). As U is tuned larger, the highest f band is lifted but the band property is not changed near the Fermi level.

Figure 14 shows PBE (U = 0 eV) band structures of EuB_6 without and with SOI as well as PBE + U band structures with U = 2 eV and 6 eV. As can be seen in Figure 14a, the f bands are located at E_f with a localized flat band character. In the periodic table, Eu is the neighbor of Sm with one more electron. The additional electron raises the Fermi level of EuB_6 near the half-filling metallic regime. When SOI is included, the f bands separate themselves into two groups with an SOI-induced continuous gap in between. Furthermore, band inversion emerges around the high symmetry point EuB_6 is not sensitive

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to U, as shown in Figure 14b–d, with U = 0-6 eV, leading EuB₆ to robust topological Kondo insulator against strong correlations.

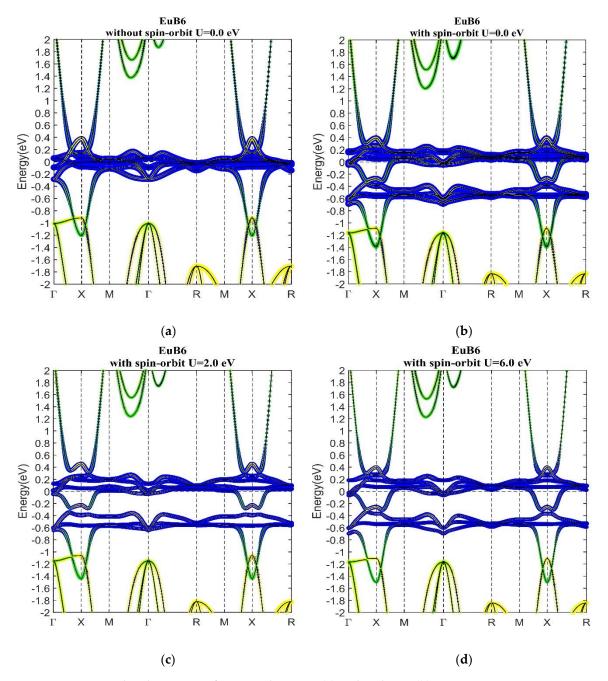


Figure 14. PBE band structure of EuB₆ without SOI (a) and with SOI (b). SOI opens up an energy gap around E_f and induces band inversion around X point. PBE + U band structure of EuB₆ with on-site U = 2.0 eV (c) and U = 6.0 eV (d). Similar to SmB₆, the Hubbard U does not change the band structure noticeably.

4. Conclusions

We have systematically analyzed the electronic structures of rare-earth hexaborides to investigate their topological properties and examine the robustness of the topological phase against strong correlations by varying the Coulomb repulsion U. SmB₆ is a topological Kondo insulator due to the hybridization gap, and it will not experience topological phase transition by tuning the Coulomb interaction. YbB₆, which has a hybridization gap, on the contrary, will experience a topology phase

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transition from a topological Kondo insulator to a topological insulator, and finally become a trivial insulator. Our results of SmB_6 and YbB_6 are in good agreement with previous results [1]. Our study also shows that PmB_6 , NdB_6 , EuB_6 and SmB_6 exhibit SOI-induced continuous gaps with band inversion, revealing nontrivial topological properties. On the other hand, the weaker SOI in relatively lighter. Lanthanides La, Ce and Pr fail to open up a continuous gap in LaB_6 , CeB_6 and PrB_6 . Thus LaB_6 , CeB_6 and PrB_6 are topologically trivial normal metals with correlated conduction electrons.

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Conflicts of Interest: There are no conflicts of interest to declare.

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