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## An ab initio study of the magnetocrystalline anisotropy and magnetoelastic coupling of half-metallic CrO<sub>2</sub>

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## Abstract

First-principles density functional calculations of the total energy, magnetic moments and magnetocrystalline anisotropy energy (MAE) of  $CrO_2$  as a function of both volume and uniaxial strain along the *c*-axis have been performed. The highly accurate all-electron full-potential linearized augmented plane wave method and the generalized gradient approximation to the exchange–correlation potential are used. The calculated structural properties (lattice constants and unit cell volume) are in excellent agreement with experiments (with 0.5%). The calculated bulk and Young's modulii are 2.56 and 2.02 Mbar, respectively. The calculated MAE increases almost linearly with the uniaxial strain and remains positive in the strain range of -4-4%. Thus, the calculated anisotropy constant is about six times larger than the measured value. The calculated magnetoelastic coupling constant is  $1.2 \times 10^7 \text{ erg/cm}^3$  and the magnetostriction coefficient  $\lambda_{001}$  is  $-2.59 \times 10^{-5}$ .

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## 1. Introduction

 $CrO_2$  has been attracting considerable interest in recent years, in part due to the fundamental interest in its half-metallic electronic band structure [1] and its applications of this, and in part because of its practical importance in magnetic

Because of its uniaxial crystalline structure, it is expected to have a large magnetic anisotropy which makes it the favoured material for magneto-optical

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recording. Being a half-metallic ferromagnet, with only one spin band at the Fermi level,  $CrO_2$  has the highest measured spin polarization of all materials to date [2,3]. Together with a high Curie temperature of 390 K [4],  $CrO_2$  provides excellent prospects for magnetoelectronic devices at room temperature.

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recording applications. Despite a large number of published theoretical calculations (see Refs. [1,5-8] and references therein), no ab initio calculation of the magnetic anisotropy energy has been reported yet. Here in this paper, we present the results of our systematic theoretical calculations of the magneto-crystalline anisotropy energy (MAE) and also its strain dependence for CrO<sub>2</sub>.

CrO<sub>2</sub> crystallizes in the rutile structure (space group  $D_{4h}^{14}$ : P4<sub>2</sub>/mnm) with a tetragonal symmetry. The primitive unit cell contains two molecular formula. The two chromium atoms are located at the positions (0, 0, 0) and  $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ , and the four oxygen atoms are at (u, u, 0), (1 - u, 1 - u, 0),  $(\frac{1}{2} + u, \frac{1}{2} - u, \frac{1}{2})$ , and  $(\frac{1}{2} - u, \frac{1}{2} + u, \frac{1}{2})$ . The measured lattice constants a and c are 4.419 and 2.912 Å, respectively [9]. The internal coordinate of the oxygen atoms u is 0.303 [9]. The electronic structure and total energy of CrO<sub>2</sub> were calculated by using the highly accurate full-potential linearized augmented plane wave (FLAPW) method, as encoded in WIEN97 [10]. The calculations were based on the first-principles density functional theory (DFT) with the generalized gradient approximation (GGA) [11].

In the present calculations, the muffin-tin sphere radii  $R_{\rm mt}$  of 1.9 a.u. for Cr and 1.5 a.u. for O were used. The parameter  $R_{\rm mt}K_{\rm max}$  was set to 7.0, i.e., a large number of augmented plane waves (PW), about 110 PWs/atom, were used. In the total energy calculations, the number of k-points in the irreduciable Brillouin zone wedge (IBZW) used is 290. However, because the MAE is generally very small, a much finer grid for the Brillouin zone integration is needed. Thus, a large number of the k-points in the IBZW (2896) was used.

The calculated total energy of  $\text{CrO}_2$  as a function of volume is shown in Fig. 1. Here c/a ratio and u are fixed to the experimental values [9], respectively. By fitting this total energy vs. volume curve to the equation of state, we obtain the theoretical unit cell volume  $V_0$  of 57.7Å<sup>3</sup> or 389.2 a.u.<sup>3</sup> and bulk modulus B of 2.56 Mbar. The calculated total and local Cr spin-magnetic moments in CrO<sub>2</sub> as a function of volume are also shown in Fig. 1. As mentioned before, CrO<sub>2</sub> is a half-metallic ferromagnet at ambient pressure. Its spin-magnetic moment is therefore quantized,



Fig 1. Total energy (lower), total and local Cr spin magnetic moments (upper) of  $CrO_2$  as a function of volume, c/a is fixed at 0.664. The total energy is relative to -4805.0 Ry/unit cell. The experimental unit cell volume is  $385 \text{ a.u.}^3$ .

being equal to  $2.0 \,\mu_{\rm B}/{\rm f.u.}$  Fig. 1 shows that the total magnetic moment of  ${\rm CrO}_2$  remains constant ( $2.0 \,\mu_{\rm B}/{\rm f.u.}$ ), indicating that it is half-metallic throughout the volume range studied. Nevertheless, the local magnetic moment in the Cr atom does increase monotonically with volume (Fig. 1).

Now, we calculate the total energy as a function of c/a ratio with the volume fixed to 57.7 Å<sup>3</sup>. This is equivalent to applying a uniaxial elastic strain  $\varepsilon$  to  $CrO_2$  along the *c*-axis. The strain  $\varepsilon$  is defined as  $a = a_0(1 + \varepsilon)$  and is given by  $[(c_0/a_0)/(c/a)]^{1/3} - 1$ . The results are displayed in Fig. 2a. Clearly, the total energy minimum is fairly close to the zero strain. By fitting a polynomial to the total energy vs. strain curve, we get the theoretical c/a ratio of 0.659 and young modulus  $Y_{001}$  of 2.02 Mbar. Thus, the theoretical lattice constants a and c are 4.439 and 2.926 Å, respectively. Clearly, the theoretical lattice constants and unit cell volume are in good agreement with the experimental ones (within 0.5%), suggesting that the present GGA calculations describe the structural properties of CrO<sub>2</sub> very well. It should be noted that in the strain range



Fig 2. Total energy (a) and magnetocrystalline anisotropy energy of  $CrO_2$  as a function of uniaxial strain along *c-axis*. In (a), the total energy is relative to -65385.727 eV/unit cell.

studied here, the total spin-magnetic moment of  $CrO_2$  remains constant (2.0  $\mu_B/f.u.$ ), again suggesting that the strained  $CrO_2$  is still half-metallic.

The calculated MAE  $\Delta E$  of CrO<sub>2</sub> as a function of the strain  $\varepsilon$  is shown in Fig. 2b. Here the MAE is defined as the difference in the total energy between the magnetization parallel to the *c*-axis and that parallel to one of the two a-axes. Fig. 2b shows that the MAE increases almost linearly with the strain. Furthermore, the MAE remain positive in the entire strain range studied here, i.e., the *c*-axis remains to be the easy axis and there is no spin-reorientation transition in this strain range. By fitting  $\Delta E = K_{\text{MA}} + 3B^*(\varepsilon - \varepsilon_0)$  [12–14] to the curve, we obtain the magneto-elastic coupling constant B of  $0.425 \,\mathrm{meV/unit}$  cell or  $1.18 \times$  $10^7 \text{ erg/m}^3$  and the uniaxial anisotropy constant  $K_{\rm MA}$  of  $23.2 \times 10^5 \, {\rm erg/cm^3}$ . From these numbers, we also obtain the magnetostriction coefficient  $\lambda_{001} = -2.59 \times 10^{-5}$  by making use of magnetoelastic theory [15,16].

Experimental investigations of the magnetic anisotropy of bulk and thin film CrO<sub>2</sub> have been carried out by several research groups [17-21]. Because of its tetragonal symmetry, the leading terms of the magnetization orientation dependence energy of the bulk CrO<sub>2</sub> are  $\Delta E = K_1 \sin^2 \theta + K_2 \sin^4 \theta + K_2' \sin^4 \theta$  $\cos 4\phi$ . The  $K'_2$  is much smaller than  $K_1$  and  $K_2$  and is thus ignored for the bulk samples. Clearly, the above theoretical  $K_{MA}$  is equal to  $K_1 + K_2$ . Ferromagnetic resonance (FMR) experiments show that both  $K_1$  and  $K_2$  of bulk CrO<sub>2</sub> fine grains are positive from just below the Curie temperature down to low termperatures of a few Ks [17,18]. The measured  $K_1$ and  $K_2$  at about 120 K are  $33 \times 10^4$  and  $6 \times 10^4$  erg/ cm<sup>3</sup>, respectively [18]. Therefore, both the experiments and the present calculations show that the caxis is the easy magnetization axis for CrO<sub>2</sub>. Nonetheless, the theoretical anisotropy constant is nearly six times larger than the measured value. The large discrepancy between experiment and theory could be attributed in some extent to the fact that the measurements were made on fine grains. No measurements on single crystalline CrO<sub>2</sub> have been reported so far.

In summary, we have performed first-principles density functional calculations of the total energy, magnetic moments and MAE of tetragonal CrO<sub>2</sub> as a function of both volume and uniaxial strain along the *c*-axis. We used the highly accurate allelectron full-potential linearized augmented plane wave method and the GGA to the exchangecorrelation potential. The calculated lattice constants are in excellent agreement with the experiments (with 0.5%). The calculated bulk and Young's modulii are 2.56 and 2.02 Mbar, respectively. The calculated MAE increases almost linearly with the uniaxial strain and remains positive in the strain range of -4-4%. Thus, the calculations predict that the easy magnetization axis is along the *c*-axis, in agreement with experiments. However, the calculated uniaxial anisotropy constant is about six times larger than the measured value. The calculated magnetoelastic coupling constant is  $1.2 \times 10^7 \text{ erg/cm}^3$  and the magnetostriction coefficient is  $-2.59 \times 10^{-5}$ . We hope that these results will stimulate further experimental investigations of the MAE, magnetoelastic coupling and magnetostriction of CrO<sub>2</sub>.

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